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THE PARADOX OF LIQUIDITY

Stewart C. Myers Raghuram G. Rajan

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THE PARADOX OF LIQUIDITY

ABSTRACT

The more liquid a company's assets, the greater their value in a short-notice liquidation. Liquid assets are generally viewed as increasing debt capacity, other things being equal. This paper focusses on the dark side of liquidity: greater liquidity reduces the ability of borrowers to commit to a specific course of action. It examines the effects of differences in asset liquidity on debt capacity. It suggests an alternative theory of financial intermediation and disintermediation.

Stewart C. Myers Alfred P. Sloan School of Management Room E52-451 MIT Cambridge, MA 02139 and NBER Raghuram G. Rajan Graduate School of Business University of Chicago 1101 East 58th Street Chicago, IL 60637 and NBER

The Paradox of Liquidity

The liquidity of an asset means the ease with which it can be traded. The more liquid a company's assets, the greater their value in short-notice sales. Liquid assets are generally viewed as increasing debt capacity, other things equal.² and in some contexts illiquid assets are significantly less valuable than readily marketable ones.³

Asset liquidity is almost always a plus for nonfinancial corporations or individual investors. For financial institutions, however, increased liquidity can paradoxically be bad. Although more liquid assets increase an institution's ability to raise cash on short notice, it also reduces its management's ability to commit credibly to an investment strategy that protects the institution's creditors. The problem becomes more acute when the institution is in the business of making markets or trading for its own account.

This paradox of liquidity can be seen in the following example. Consider a company formed to make markets in government and corporate bonds. It starts with an inventory of Treasuries. If these specific securities could be irrevocably assigned as collateral, the company could finance its inventory with almost 100 percent debt (assuming matched maturities). But then the inventory would be locked up and of no use in trading.

Such a company cannot commit not to trade and therefore cannot lock up specific assets as collateral. Uncertainty about duration (and default risk) is built into the business, and so the value of any initial securities position as collateral is limited. In fact, a nonfinancial company, which did not need the Treasuries as operating assets, could lock them up and borrow much more against them.

A financial institution which invested mainly in illiquid business, personal and real estate loans would find long-term financing easier to arrange. Granted, illiquidity gives creditors less value if they seize the assets, but it also gives them more time to assess interest rate exposures and credit risks. They

²See Shleifer and Vishny (1992), for example.

³ Valuations of securities lacking an active public market are marked down for estate and gift tax purposes. Also shares of "letter stock" may sell in private transactions for 20 to 40 percent less than otherwise identical registered shares.

also have the assurance that today's risks would change slowly -- illiquid portfolios do not change overnight.

Creditors of an institution holding and trading mostly liquid assets have no way to predict values or risk for the next month or next year. When retaining flexibility over the disposition of assets is essential, the firm may end up too liquid for its creditors.

In short, liquid assets give creditors greater value in liquidation, but they also give borrowers more freedom to act at creditors' expense. While both issues have been separately recognized,4 their interactions are largely unexplored.

We show that a firm which starts with liquid core assets has an absolute advantage in obtaining external financing for less liquid projects. The incremental debt capacity the firm generates by taking on the less liquid project exceeds the debt capacity the project has on its own. By contrast, two projects (or firms) that are less liquid can have less debt capacity combined than stand-alone.

We show that firms unusually liquid core businesses are best suited to channel financing to other firms in the economy. This leads to a theory of financial intermediation which is consistent with the historical origins of the rise of banks. Our theory can also explain why disintermediation — in which the most creditworthy firms bypass banks to borrow directly from the markets — has increased recently, and why banks have increased their concentration on illiquid segments of the loan market.

Finally, we examine the effect of adverse shocks to firms with excessively liquid assets. The possibility that such firms can transform assets leads to quicker responses by creditors than for less liquid firms. This affects the kinds of assets the firm liquidates. A rational firm may sell an asset whose liquidity is temporarily depressed, even though the asset's liquidity is expected to recover, and even though the firm has assets of higher current liquidity. To the extent that selling is caused by a systematic shock, this could account for "herd selling" or "rush to the exit" by financial institutions.

⁴ For the first issue, see Diamond (1991), Hart and Moore (1992), Myers (1977), and Shleifer and Vishny (1992). For the second, see Diamond and Dybvig (1986), Esty (1993), Flannery (1994), Huberman (1984), Kahn (1992) and an extensive literature on risk-shifting moral hazards, dating to Jensen and Meckling (1976).

The rest of the paper is as follows. In section 1, we analyze a simple model in a world of certainty. In section 2, we consider implications for banking and intermediation. In section 3, we turn to some aspects of uncertainty. We conclude with policy conjectures and suggestions for future research.

Section 1

1.1. Investment and Asset Liquidity.

Consider a firm which wants to undertake a positive NPV project with initial investment \$1. If the investment is made at date 0, the project returns a cashflow of C_1 at date 1, and C_2 at date 2. The cashflows from the project are known but not verifiable. The firm will finance part of the investment by borrowing amount B supported by promised payments P_1 and P_2 . The lender can extract repayment from the borrower by threatening to liquidate the assets (see Hart and Moore (1992)).

The depreciated value of the assets at dates 1 and 2 are d_1 and d_2 . These are "intrinsic" values – gross values in the next best alternative use – and take no account of illiquidity. We assume risk neutrality and a zero interest rate. Positive NPV requires that $C_1 + C_2 + d_2 > 1$. We also assume that $C_2 + d_2 \ge \alpha d_1$, so that it pays to continue the project at date 1.

Of course a positive d_2 implies subsequent cash flows. We could keep track of one more cash flow C_3 , for example. But we will assume $d_3 = 0$. As we will show, the lender then has no bargaining power after date 2 and cannot extract any payment P_3 . We therefore consider only two-period lending.

Liquidity. Both borrower and lender contemplate liquidation. The lender may have to seize and sell the assets. The borrower may choose to sell or transform the assets before the lender can get them. The value obtained on liquidation is αd_i , where $\alpha \in [0,1]$ is the intrinsic liquidity of the asset. Intrinsic liquidity depends on the degree to which the asset suffers from a "lemons" problem, the transactions costs or bid-asked spreads in selling, the number of potential buyers in the market and the degree to which they may be wealth constrained (see Shleifer and Vishny (1992)). Later, we will also allow the value obtained on liquidation to depend on who liquidates the asset, and on the institutional environment.

The borrower can consume or transform assets at date 1/2 or at date 1 1/2. (From now on we will just say "transformation risk".) The lender can liquidate the assets at date 1 or 2 if the borrower does not make the (potentially renegotiated) required repayment and the borrower has not already taken the assets.⁵

This first model has no legal or contractual constraints on transformation — no debt covenants, no enforcement of laws against theft or misappropriation. We ignore these things to clarify the problems created by liquidity. More complex models come later in the paper. For now, lenders *only* have the power to seize assets.

The timing of borrower's and lender's decisions is:

Date 0	Date 1,	/2 Date 1	Date 1		Date 2
Investment undertaken.	Management decides whether to consume/ transform assets and realize αd ₁ .	C ₁ realized. Lender can liquidate assets if management does not make contractual payment and borrower has not consumed/transformed assets.	Management decides whether to consume/ transform assets and realize αd ₂ .	C ₂ realiquida manage contral borrow transfo	lized. Lender can ate assets if gement does not make ctual payment and wer has not consumed/ormed assets. If wer retains possession ets, she realizes d ₁ .

1.2. Financing.

The lender makes a loan of B to finance part of the initial investment. The borrower makes up any shortfall with E dollars of his own funds. The loan contract specifies the initial sum lent, as well as the repayments P₁ and P₂ due at dates 1 and 2. We assume the lender cannot get his hands on the earnings the borrower generates because it is in the form of cash which is the most easily appropriated asset. The lender can, however, threaten to seize the assets, which are essential to producing earnings, if the

⁵We assume initially that the assets cannot be partially transformed or liquidated. This assumption will be discussed later.

⁶ E+B can be greater than I, giving the borrower some cash to make payments even if P_1 is greater than C_1 . Cash cannot be seized by the lender.

required payments are not made.

We allow for loan renegotiation, following Hart and Moore's (1992) framework: at each date, the borrower either makes the specified payment or offers to make a lower payment. If the lender turns down the offer, he can either liquidate the firm or continue the renegotiation process. If he continues negotiating, he gives up the right to liquidate the firm for the rest of the period.

If the lender negotiates, he has a probability a — a measure of his bargaining power — of making the next (and final) offer. With probability (l-a) the borrower gets to make this offer. If the final offer is turned down, the next period's cashflow (for example, cashflow C_2 at date 1) is not produced. This could be though of as the costs of financial distress.

We will determine the maximum amount that can be financed by borrowing. The project will never be inefficiently liquidated at this "debt capacity" provided the firm has enough cash to make the payments that can be credibly extracted by the lender. We will show that debt capacity is not monotonic in the intrinsic liquidity of the assets. Liquidity can be a double-edged sword.

1.3. Solving for debt capacity.

We first determine the outcome of any renegotiation at date 2. If the borrower makes the payment P_2 (which may have been renegotiated at date 1), she keeps the assets and gets d_2 . If she does not make the payment, the lender can, at best, liquidate the assets. So the outcome of the bargaining at date 2 is simply that the debt claim P_2 is renegotiated down to Min $[P_2, \alpha d_2]$ which the borrower always pays if she has the cash (because it is always weakly less than d_2). In order to focus on the debt capacity associated with the assets, we assume at first that the borrower has enough cash to make debt payments at date 2.

Now move back to date 1 1/2, when the borrower has to decide whether to transform the assets, realizing αd_2 , or continue in business, generating cashflow C_2 and the terminal value d_2 . She continues if

$$C_2 + d_2 - Min[P_2, \alpha d_2] \geq \alpha d_2$$
 (1)

⁷ If negotiations break down, the unpaid debt cumulates to the next date when negotiations resume.

This implies that the maximum date-2 repayment the lender can get is

$$V_2^L = Min [C_2 + d_2 - \alpha d_2, \alpha d_2]$$
 (2)

Now consider what happens when the debt is renegotiated at date 1. This is a simple extension of lemma 1 in Hart and Moore (1992).

<u>Lemma 1:</u> If the borrower asks to reschedule payments at date 1, the lender can get at maximum $V_1^L = Max [aC_2 + V_2^L, \alpha d_1]$. So at date 1, the borrower will get $C_1 + C_2 + d_2 - V_1^L$ from the project if condition (A) holds, and nothing if condition (A) does not hold. Condition (A) requires P_1^* , P_2^* such that:

$$P_{l}^{\bullet}+P_{l}^{\bullet}=V_{l}^{L} \tag{3}$$

$$P_{2}^{\bullet} = V_{2}^{L} \tag{4}$$

$$E+B-I+C_i\geq P^*, \tag{5}$$

Consider the negotiation that takes place at date 1 if the borrower does not make the required repayment. Suppose the borrower makes an offer which the lender turns down. With probability a, the lender gets to make a take it or leave it offer. The lender will demand C_2 , the entire cashflow that is to be produced over the period. The borrower can do no better than accept, because if the offer is rejected, the assets remain idle over the period. With probability (I-a), the borrower gets to make a take it or leave it offer, and will demand the entire cashflow from the project C_2 . Again, the lender can do no better than accept. On average, the lender and borrower split the cashflow according to their relative bargaining power. So the total stream of payments the lender can credibly get (the continuation value) is $aC_2 + V_2^L$. In addition, the lender can force liquidation, so $V_1^L = Max \left[aC_2 + V_2^L, \alpha d_1 \right]$, with liquidation placing a lower bound on what the lender can get. If the borrower has the cash, this is what he will offer to pay, and the offer will be accepted.

Condition (A) is simply that a credible payment schedule exists which gives the lender the

⁸ If the terminal value of the asset, d₂, comes from a future (unmodelled) cashflow C₃ from the asset, then it is possible the lender may be able to extract more than αd_2 by threatening to seize the asset. But the lender cannot get more than αd_2 if $aC_1 < \alpha d_2$. This is implicit in our solution to the renegotiation outcome at date 2.

incentive to not liquidate the project. Inequality (5) says that the sum of the cash left over after the initial investment and the cash inflow at date 1 are enough to make the required payment. In order to focus on debt capacity stemming from the nature of the assets themselves rather than the timing of cashflows, we will initially assume a high enough value of equity E that (5) is satisfied.

We now know what happens at date 1 if the borrower attempts to renegotiate the loan contract. But the borrower can consume or transform the assets at date 1/2. This puts a further constraint on the amount she can promise. If $V_{1/2}^L$ is the amount that the borrower expects to pay the lender over the course of the loan contract (after allowing for the equilibrium outcomes of any possible renegotiation at dates 1 and 2), for the borrower to be able to commit to not consume the assets, it must be that

$$C_1 + C_2 + d_2 - V_{1/2}^L > \alpha d_1.$$
 (6)

Finally, for it to be individually rational for the lender to make the loan at date 0, it must be that

$$V_{12}^{L} \ge B \tag{7}$$

The maximum debt that the borrower can credibly commit to repay is then the solution to the following linear programming problem. Each constraint is keyed to a renegotiation or possible transformation.

Transformation risk at date 1/2. We concentrate first on constraints (8) and (9). Constraints (10) and (11) will not bind if C_2 is large enough, and if enough cash is available at date 1 to front-load debt payments in P_1^* , rather than P_2^* . Constraint (9) reduces to

⁹ This also ensures condition (A) is satisfied.

$$P_1 + P_2 \le \text{Max } [aC_1 + \alpha d_1, \alpha d_1]$$
(9a)

If only constraint (9a) were relevant, debt capacity would be (weakly) monotonically increasing in the intrinsic liquidity of assets α . This is plotted in Figure 1. Monotonicity no longer holds when the transformation risk constraint (8) is added. Debt capacity decreases in asset liquidity when this constraint is binding (see Figure 2).

Constraint (8) binds if $C_1 + C_2 + d_2 - \alpha d_1 < \text{Max } [aC_2 + \alpha d_2, \alpha d_1]$ for $\alpha < 1$. This occurs when the cashflows C_1 and C_2 are not too high relative to the liquidation value.

1.4 Debt capacity contributed by a project.

Previous literature has focussed on situations where the borrower does not transform or consume the assets, whence the assertion that debt capacity increases in asset liquidity. We now examine the effects of liquidity on debt capacity when a firm with a specific asset structure wants to undertake a new project. We show that debt capacities do not necessarily add up. Debt capacity can be substantially greater (or less) when two projects are undertaken together rather than separately.¹⁰

Example: Consider a project with $C_1^P = 1$, $C_2^P = 1$, $d_1^P = 2$, $d_2^P = 1$, $a^P = .5$, $\alpha^P = .3$. Assume the date-0 investment required is 2. The project can take on debt up to its "going concern" debt capacity, $a^P C_2^P + \alpha^P d_2^P = .8$. Because the cash flows are large relative to liquidation value, transformation risk does not bind. But because liquidation value is low relative to the cash flows, the cash flows do not contribute much to debt capacity because the lender cannot enforce payment. The project has insufficient collateral — it is "illiquid".

Let a firm have parameters $C_1^F = 1$, $C_2^F = 1$, $d_1^F = 5$, $d_2^F = 4$, $a^F = .5$, $\alpha^F = .6$. The investment required is 5. The intrinsic liquidity of the firm's assets is higher than the project's, though its cashflows are relatively small compared to the asset value. Its debt capacity, determined by the

¹⁰ This is different from the well-known result that diversification reduces bankruptcy costs and increases debt capacity. That result is uni-directional (more diversification always increases debt capacity). Our result can go either way. Furthermore, we obtain this result in a world of certainty. With uncertainty, it is easy to show that diversification helps the borrower commit to not consume or transform the assets.

Kahn (1992) also describes interactions between projects. We differ in our emphasis on liquidity.

liquidation value of its assets, is $\alpha^F d_1^F = 3$.

Now consider what happens when the firm undertakes the project in-house. Debt capacity for the combined entity turns out to be the going concern debt capacity, which is $a^pC_2^p + a^pC_2^p + \alpha^pd_2^p + \alpha^pd_$

But let the firm's assets be more liquid, so that $\alpha^F = 1$. Transformation risk now limits the firm's stand-alone debt capacity to $C_1^F + C_2^F + d_2^F - \alpha^F d_1^F = 1$, even though the liquidation value of the assets is higher at $\alpha^F d_1^F = 5$. This implies that the firm has liquid assets which cannot be pledged because the firm cannot commit to staying around (after date 1/2) if it borrows too much. The firm is "overly liquid".

When the overly liquid firm undertakes the project, combined debt capacity is determined by the lower of liquidation value and transformation risk, which is 3.4. This is much higher than the sum of stand-alone debt capacities (1.8). The project has cash flows, but not enough liquidation value for the lenders to extract repayment. The firm has excess liquidation value but too little cash flow to commit not to transform the assets. When the firm undertakes the project, the project's cashflow insures the lender against transformation risk (alleviates the transformation risk constraint), while the firm's liquidation value enables the lender to credibly extract repayment. Combining the firm and project increases debt capacity.

An important assumption in this example is that assets cannot be liquidated or transformed separately. We will discuss this shortly. But first we formalize this example. Each constraint in the linear program can bind over a range of intrinsic liquidity α . The three ranges are

- (a) $0 \le \alpha \le \alpha_L$, where $B = aC_2 + \alpha d_2$
- (b) $\alpha_L < \alpha \le \alpha_{LL}$, where $B = \alpha d_t$
- (c) $\alpha_{LL} < \alpha \le 1$, where $B = C_1 + C_2 + d_2 \alpha d_1$

If condition (a) holds, we call the firm or project *illiquid* because debt capacity depends cashflows. If condition (b) holds, we call it *liquid* because debt capacity is fully determined by the liquidation value of the assets. If condition (c) holds, we call it *overly liquid* because its debt capacity is reduced by its excessive liquidity. We plot the relevant ranges in Figure 2. When a firm takes on a project, if the assets cannot be liquidated or transformed separately,

Proposition 1

- a) The incremental debt capacity an <u>illiquid</u>, <u>liquid</u> or <u>overly liquid</u> firm gets when it takes on an illiquid, liquid or overly liquid project, respectively, is equal to the project's debt capacity when financed independently.
- b) The incremental debt capacity a <u>liquid</u> firm gets when it takes on an illiquid project is less than the project's debt capacity when financed independently.
- c) There always exists a range of illiquid and liquid projects such that the incremental debt capacity the overly liquid firm obtains with those projects strictly exceeds the project's debt capacity when financed independently.

Proof: See Appendix.

If debt financing is the cheapest form of finance, it makes more sense for the <u>overly liquid</u> firm to raise money for a range of less liquid projects than for such projects to raise finance directly from lenders. The overly liquid firm has an excess of liquid assets which cannot be collateralized because they are too liquid, that is, too easily transformed. The illiquid project has an excess of cashflows and a deficit of liquid asset value. The excess liquid assets of the overly liquid firm serve to collateralize the illiquid project while the illiquid project's cashflows serve to bind assets in place and reduce transformation risk. By contrast, the illiquid project brings insufficient assets to a combination with a <u>liquid</u> firm, while the firm brings insufficient cashflows to the combination, so they are worse off borrowing together than

borrowing separately.11

As the liquidity of the assets of an overly liquid firm increases, its ability to finance projects of lower liquidity generally increases. Let $[\underline{\alpha}^p, \overline{\alpha}^p]$ be the range of intrinsic liquidity of projects for which there is a greater increment in debt capacity in doing the project in-house relative to doing it independently. Furthermore, let α^{p-} be the intrinsic project liquidity for which the advantage is largest (if this is a range, let it be the maximum of the range). Proposition 1 implies:

<u>Corollary 1:</u> An increase in the intrinsic liquidity of the overly liquid firm's assets leads to a (weak) decline in $\underline{\alpha}^{P}$, no change in $\overline{\alpha}^{P}$ and a (weak) decline in $\alpha^{P^{*}}$.

Proof: See appendix.

1.5. The Borrower's Flexibility.

Thus far, we have assumed no difference between transformation by the borrower and liquidation by the lender. This is implausible. First, asset transformation may involve not just liquidating the assets, but also reinvesting the proceeds elsewhere. The additional frictions in the process of reinvestment, and the possibility that the borrower will not be able to keep all the reinvested amount out of the hands of the lender, will reduce the amount the borrower can realize. Second, the flexibility to transform assets hurts the borrower's ability to borrow. So a borrower may attempt to give up this flexibility. Third, there will

If this were possible, the project and the firm would not insure each other. The assumption is plausible if the assets complement each other in the production of cashflows, so that when one is transformed or liquidated, the cashflow or liquidation value of the other falls dramatically. A similar interpretation is that the assets of the "firm" and the "project" are so closely tied together (as in a merger of two companies) that there are high transactions costs of disentangling them (preventing selective liquidation) or delays in doing so (giving the lender the time to react to selective transformation). Liquidation in the model may be a metaphor for bankruptcy. If so, cross-default clauses may make it impossible to renegotiate on one set of assets outside of bankruptcy, and another set in bankruptcy. Another rationale for why partial transformation may not be possible is that there may be an intangible asset such as business reputation which is destroyed when any asset is transformed. If this intangible asset is necessary for any physical asset to generate cashflows, partial transformation will not take place. We return to this issue in Section 2.

be institutional and legal impediments to transformation. 12

Suppose the borrower gets only $b\alpha d_1$ from transforming assets, where $b \in [0,1]$ is the borrower's flexibility. The borrower can reduce b by writing contracts pledging assets to lenders or third parties; allowing monitoring, if it is informative and not too expensive, and allowing the lender the chance to seize the asset before it is transformed.

The institutional and legal environment clearly also matters. For example, diligent and impartial outside board members and stricter ethical and legal standards for borrowers will result in a low b. On the other hand, opening up derivatives markets must increase b: a company can readily "sell" an asset by the appropriate derivative trade.

There are constraints, however, on the extent to which the borrower can reduce b. There may be some assets that are virtually impossible to monitor or pledge. For example, we have assumed the borrower's liquidation factor for cash is b=1; the borrower can take all the cash if he wants to. In real life, cash's b will not be one, but often close to it: cash can readily be absorbed in perks and bonuses, for example.

Some assets can be transformed into cash during the normal course of operations; borrowers can "liquidate" working capital by not plowing the optimal amount of revenue back into new inventory. The intrinsic liquidity of inventory is irrelevant because it regularly turns into cash. Such underinvestment¹³ is difficult to contract against, because optimal inventories keep changing depending on future business conditions, which borrowers can usually forecast better than lenders.

Borrowers can also transform assets by risk-shifting, that is, changing assets or operating strategies to increase the volatility of payoffs. With limited liability, this transfers value from lender to

¹² The manager of a U.S. savings and loan in the early 1980s had a strong incentive to transform its assets into riskier ones (see Esty (1993), for example). In medieval Spain, life was not as simple. As Usher (1943) documents, the bankrupt banker was kept on a diet of bread and water till such time as he paid off his debt or was beheaded, whichever came first. The value of transformation for the Spanish banker was probably smaller than for the modern American one.

¹³ Note the parallel to Myers's (1977) underinvestment problem.

borrower.

All these ways of transforming assets can be controlled to some extent by contracting or monitoring. But even when low b's are feasible they are not always desirable, because the cashflows generated by the assets will also depend on the flexibility the borrower has in accepting appropriate risks and opportunities. For instance, in some businesses, profits depend on assets remaining secret. A securities trader's position will fluctuate minute by minute. Allowing a lender to track the positions would be costly, and would also reveal the trader's expectations (and tempt the lender to front-run the borrower). Partial or selective disclosure by the trader to the lender is unlikely to help: the position may be safe and sound given the trader's derivatives positions and overall risk management strategy, and yet appear very risky to a partially informed lender. The trader will not allow the lender to witness and monitor all aspects of operations on a continuous basis, and therefore the trader's inventories of securities will inevitably have high flexibility.¹⁴

Wholesale securities traders and dealers face the paradox of liquidity in its most extreme form. They hold highly liquid assets in rapidly changing mixtures, and undertake complex derivatives positions. They cannot reveal short-run strategies. The combination of liquidity and opaqueness puts the highest credit ratings out of reach unless the debt ratio is pushed down or other less liquid assets are combined with the securities operations (as in universal banks).

Choice of flexibility. All the costs of reducing the borrower's flexibility can be netted against the cash flows C_1 and C_2 . We reduce the cash flows by the fraction $f(b, \alpha)$, with $f_b > 0$ (subscripts indicate partials) and $f(1, \alpha) = 1$. So cashflows increase in the flexibility the borrower retains, and reach their maximum value when the borrower has complete flexibility. The borrower trades off the effect of flexibility on cash flows against its effect on debt capacity. We assume here that the transformation constraint binds for all relevant values of b. Then the borrower maximizes

¹⁴ Of course, *some* securities can be pledged. Securities firms borrow constantly through "repos" which are essentially collateralized borrowing. However, since the trader's business is trading, a substantial fraction of the assets cannot be pledged.

$$f(b,\alpha)(C_1 + C_2) - \theta[1 - (f(b,\alpha)(C_1 + C_2) + d_2 - b\alpha d_1)]$$
 (13)

with respect to b. The first term in (13) is the (reduced) cashflow generated by the project, while the second term (in square brackets) is the shortfall from desired funding of \$ 1 which has to be met through additional equity. The shadow cost per dollar of having to put in additional equity is θ . Differentiating with respect to b,

$$(1+\theta)f_{b}(b,\alpha)(C_{1}+C_{2})-\theta \alpha d_{1}$$
 (14)

If f_b is high enough so that flexibility is very important for the generation of cashflows — as in the example of the securities trader — the borrower will set b = 1. If cashflows do not depend much on flexibility — as in the case of a piece of machinery built into an assembly line — the borrower will set b as low as possible. We proceed further by assuming that f is concave. From the first order condition, it is easily seen that if there is an interior optimum, b^* , it increases with cashflows, decreases with θ , the excess cost of equity, and decreases with the date-1 value of assets, d_1 .

The effect of a change in intrinsic liquidity on b^* is more subtle. Implicitly differentiating after setting (14) equal to zero, we get

$$\frac{db^*}{d\alpha} = -\frac{[(1+\theta)f_{ba}(b^*,\alpha) (C_1 + C_2) - \theta d_1]}{(1+\theta)f_{bb}(b^*,\alpha) (C_1 + C_2)}$$

Because f is concave, the relationship between optimal flexibility and liquidity depends on the sign of the expression in square brackets. For businesses that tend to "buy and hold" assets, liquidity is likely to have small effects on cashflows, and $f_{b\alpha}$ will be small. In this case, an increase in asset liquidity primarily increases the marginal impact of flexibility on debt capacity; by agreeing to lower flexibility, the borrower can increase debt capacity by substantially more when asset liquidity is high. Thus $db^*/d\alpha$ is negative. But if a firm is in the business of trading the assets, periods of high asset liquidity are precisely when the assets are least costly to trade, and the most money can be made. The impact of flexibility on cashflow is highest when liquidity is high. For such businesses, it is possible that $f_{b\alpha} >> 0$, and

increased asset liquidity can imply higher optimal flexibility.

We emphasize that firms not in the business of trading assets have no use for flexibility. They will set b as low as they can. But trading makes flexibility important, and excessive asset liquidity can have an adverse effect on debt capacity. This is a more difficult tradeoff: by reducing b the firm increases debt capacity at the expense of lower profits.

Though b is endogenous, we will take it for simplicity as a constant, predetermined by law and the debt contract.¹⁵

1.6. Effect of transformation risk at date 1 1/2 and multiple periods.

Thus far, we assumed that the date-2 cashflows are high enough relative to date-2 liquidation value that transformation risk does not bind at date 1 1/2. There is nothing conceptually new when this assumption is relaxed. In the absence of cashflow constraints, second period debt capacity is given by Min $[C_2 + d_2 - b\alpha d_2, \alpha d_2]$. The first term is the transformation risk constraint at date 1 1/2; the second is the liquidation value of the assets. So the essential results hold: debt capacity does not increase monotonically with the intrinsic liquidity of the assets, and overly liquid firms have a comparative advantage in financing a range of liquid and illiquid projects. "Overly liquid" now implies that transformation risk binds on both periods. "Liquid" and "illiquid" mean that transformation risk does *not* bind in one or both periods. This suggests there is nothing intrinsically different in extending the model to more periods than two.

What about the maturity of debt capacity? Hart and Moore (1992) show that slower asset depreciation means longer maturity debt. When assets retain value, the lender retains the ability to extract repayment, and can lend longer term. Assets such as land, which do not depreciate $(d_1 = d_2 = 1)$, can support the longest term debt.

Land is easily pledged. It is impossible to make away with land and sell it without title, or to transform it. So flexibility can be made very low, and liquidation value will determine debt capacity at

¹⁵ All our earlier results can be generalized using transformation values of bαd.

date 2. Ceteris paribus, an increase in the intrinsic liquidity of land will (weakly) increase the ratio of second-period debt capacity to total debt capacity, i.e., increase the maturity of debt capacity.¹⁶

But other assets, such as accounts receivable and inventories, which do not depreciate because they are continuously replaced, do not support long term debt. Accounts receivable and inventories are easily converted into cash by the simple expedient of not re-investing in them. It is hard to guard against this without unduly limiting borrower flexibility, or incurring high monitoring costs. Optimal flexibility is high for these assets. Also, the transformation risk constraint is substantially tighter in the second period when these assets continue to retain value and liquidity, but early cashflows have been harvested.¹⁷ So while non-depreciating assets with low borrower liquidation factors can support a constant level of debt each period, non-depreciating assets with high borrower liquidation values support a decreasing amount of debt in later periods, and have a lower maturity for debt capacity. Moreover, the maturity shortens even further with increases in intrinsic asset liquidity.¹⁸

Before we turn to applications, it is useful to review the basic insights developed so far. As a consequence of transformation risk, debt capacity is not monotonic in the intrinsic liquidity of assets. Because the assets of an overly liquid firm cannot be fully utilized as collateral, the firm can bind the assets by taking on less liquid projects that are cash flow-rich but asset-poor.

Section 2

One of the most interesting applications of our model is to the theory of banking. Why is it that banks have illiquid loans as assets and short-term deposits as liabilities? Consider our

¹⁶ If the firm is illiquid in the first period, this ratio is $\alpha/(aC_2 + \alpha)$ which increases with asset liquidity, α . If the firm is liquid in the first period, the ratio is $\alpha/\alpha = 1$, which does not change with asset liquidity.

¹⁷ The transformation constraint at date 1/2 is $C_1 + C_2 + d_2 - b\alpha$, while at date 1 1/2, it is only $C_2 + d_2 - b\alpha$.

¹⁸ If transformation risk binds at date 1 1/2, second period debt capacity is given by $C_2 + d_2 - b\alpha$, and it is clear that the maturity of debt capacity decreases with increases in asset liquidity so long as the firm is illiquid or liquid in the first period. But this is true even if transformation risk binds in the first period. The ratio of second period debt capacity to first period debt capacity is then $(C_2 + d_2 - b\alpha)/(C_1 + C_2 + d_2 - b\alpha)$ which decreases in α .

explanation.¹⁹ Suppose there exists an economic need for deposits repayable on demand. Such a need may arise because individuals have an uncertain demand for funds (see Diamond and Dybvig (1983)) or because deposit banking substitutes for payment by coin or bills and thus fulfills a payment system function (see below). Depositors can demand cash, so part of the bank's assets has to be cash or a very liquid close substitute. If these core assets are liquid, and transformation risk binds the bank's debt capacity, then it has a comparative advantage in financing less liquid projects. Such projects' debt capacities would be less if financed stand-alone or taken on by less liquid firms.

We could interpret the project as a financial asset, that is an (illiquid) loan. Therefore, if financial intermediation is efficient, and there is no good secondary market for loans, our theory predicts that companies that (for any reason) have overly liquid core assets will be the intermediaries.

Now the \$64 question: does our model predict that intermediation is more efficient than direct financing? To answer we have to consider the contribution of a loan to the bank's debt capacity. Does aggregate debt capacity increase if investors lend to banks who in turn loan to other firms or projects?

2.1. Intermediation.

Thus far we have analyzed direct lending by investors to firms. We have not specified who these investors are. What if each investor makes only a small fraction of a loan? A firm which pools the money lent to it by many small investors, and lends it on, has natural advantages. It brings scale economies to monitoring and does not suffer from the problems of organizing collective action that would plague the group of small investors. Hence, it will have greater voice over the actions of the borrower. The institutional lender's greater ability to monitor and control the borrower should allow it to get a greater portion of the cashflows the borrower generates.

These advantages do not always increase aggregate debt capacity, however. That depends on whether individual investors can extract a sufficient fraction of the cash flows received by the institutional

¹⁹ Our theory is not completely unrelated to the role of banks as monitors (see, for example, Boyd and Prescott (1986), Campbell and Kracaw (1980), Diamond (1984), Fama (1985), Leyland and Pyle (1977), and Ramakrishnan and Thakor (1984)). But it also provides an independent reason for intermediation.

lender.

We analyze a firm that borrows from individual investors for its own core business and to lend on a project. The firm has enhanced bargaining power over the cashflows of the project, so that $a_F^P > a_I^P$. The subscript denotes lender type, where I represents "individual investor" and F the firm, that is the financial intermediary.

We are interested in the debt capacity of the firm. We will focus on an illiquid project, but the results are readily extended to other kinds of projects. The debt capacity of the project when individual investors loan directly to it is $a_1^P C_2 + \alpha^P d_2^P$. The debt capacity of the project when the firm lends to it is $a_F^P C_2 + \alpha^P d_2^P$. Let this be the amount the firm lends and let the contracted, enforceable repayments be P_1^P and P_2^P . Because $a_F^P > a_I^P$ the firm can extract higher repayments from the project than can individual investors. But can the firm finance the loan by borrowing from individual investors? If it can, then intermediation can dominate direct lending.

In order to determine the additional debt capacity the loan adds to the firm's core assets, we have to find the liquidation value of the loan. If a loan sales market does not exist, it will be hard for the firm to transform the loan. So we will first assume zero transformation value for the loan (b = 0). But the loan may still have liquidation value in the hands of individuals who invest in the firm. If the firm defaults, lenders can seize the loan. The "liquidation" value then depends on how much individual investors can extract from the ultimate borrower, the project. The loan claim is worth $a_1^P C_2 + \alpha^P d_2^P$ if seized before date 1, Min $[a_1^P C_2 + \alpha^P d_2^P, P_2^P]$ if seized at date 1 (after the project has made the initial repayment), $Min[\alpha^P d_2^P, P_2^P]$ if seized after date 1 but before date 2, and 0 at date 2.

Lemma 2: If there is no secondary market for the loan, the amount of debt that can be raised against the

²⁰ In practice, a bank can also transform the quality of its loan portfolio by demanding early repayment and reinvesting the money in poorer quality assets. Or it can cut side deals with its borrowers, asking for early payment in return for debt forgiveness. This implies that the effective transformation possibilities in a loan portfolio increase as the ultimate borrowers obtain more access to funds. For now we assume debt payments leave the borrower with no residual free cash at date 1.

loan on a stand-alone basis is strictly less than the face value of the loan.

<u>Proof:</u> There is no loan sales market, so transformation risk does not influence the debt capacity of the loan. Its liquidation value if seized at date 1 is $Min [a_1^P C_2 + \alpha^P d_2^P, P_2^P]$. As $P_2^P \le \alpha^P d_2^P$, this evaluates to P_2^P . Because the date-2 liquidation value of the loan is zero, the going concern debt capacity of the loan is $a_1^P P_2^P$. So the debt capacity of the loan on a stand alone basis is the greater of the liquidation value and the going concern value, which is P_2^P . But this is less than the face value $P_1^P + P_2^P$, hence the lemma.

<u>Corollary 2:</u> When a firm with core assets and a loan transforms the core assets, lenders to the firm are better off seizing the loan than renegotiating the debt.

<u>Proof:</u> If the assets are transformed at date 1/2, the value obtained from seizing the loan before date 1 is $a_1^P C_2 + \alpha^P d_2^P$. This is greater than the repayment that can be extracted from a firm with the loan as its only asset, P_2^P . The value obtained from seizing the loan after date 1 and before date 2 is $Min[\alpha^P d_2^P]$, which exceeds 0, the amount the individual investors can extract by waiting till date 2 (the loan has no value at date 2 since it is fully repaid). Hence the corollary.

Lemma 2 and corollary 2 imply

Proposition 2: If there is no secondary market for a loan to an illiquid project, then

- (i) Regardless of the firm's bargaining power over the project's cashflows, a_F^P , the incremental debt capacity an illiquid or liquid firm adds with a loan to a project is always less than the amount the project can raise by borrowing directly from investors.
- (ii) The debt capacity the overly liquid firm adds by making a loan to a project may exceed the debt capacity the project has borrowing directly from investors. If so,
 - (a) If the overly liquid firm cannot commit not to transform assets selectively, it will have higher debt capacity by making a loan to a project than by undertaking the project in-

house.

(b) The debt capacity of the overly liquid firm (weakly) increases in its bargaining power over the project's cashflows, a_F^P .

Proof: See appendix.

The firm's greater bargaining power over the project ensures that the repayments it can extract from the project exceed the repayments individual investors can obtain by lending directly to the project. So it can lend more. Unfortunately, as lemma 2 indicates, individual lenders to the firm cannot extract this money in its entirety from the firm if the loan is the only asset the firm possesses. Creditors can threaten to liquidate other assets held by the firm. But it is only when these assets are overly liquid that they have liquidation value which is not already supporting debt. Therefore, liquid or illiquid firms' bargaining power increases the amount they can lend to the project, but does not change how much they can borrow from the ultimate investors. Hence proposition 2 (i). But for overly liquid firms, the greater cash inflow from loans will bind more of the (overly) liquid core assets, and can increase the firm's ability to borrow proportionately. Hence proposition 2 (ii). So a firm whose core assets are overly liquid has a comparative advantage over liquid and illiquid firms in intermediating credit because it can borrow more of the amount needed to make loans.

In Section 1, where we considered a firm conducting a project in-house, we required that the firm could not transform its assets selectively. Absent this restriction, a firm could transform its most liquid assets and then force its creditors to renegotiate. The creditors would have to write down their debt to the capacity of the remaining assets. So the illiquid projects would never co-insure overly liquid assets, and debt capacities of the firm and project would, at best, be additive. But when the firm lends to the project the assumption is no longer necessary. As corollary 2 shows, the firm exposes its loan to certain liquidation if it transforms its other liquid assets. So a firm will not transform its assets selectively, and the loan and physical assets can co-insure each other. Thus proposition 2 (ii) a.

Example (continued): In our earlier example, we assumed that the overly liquid firm could

commit to not transforming assets selectively. Suppose it cannot. Then taking on the project in-house does not add to debt capacity. But we can show that by making a loan to the project, rather than doing the project in-house, the firm can expand debt capacity. Let $a_F^P = .7 > a_I^P = .5$. The firm can make a \$ 1 loan to the project, with enforceable payments $P_{i}^{P} = .7$ and $P_{2}^{P} = .3$. The project, borrowing directly from individual investors, can raise only .8 (because $a_t^P < a_F^P$). Similarly, on a stand-alone basis, the loan is not a good asset to borrow against because its liquidation value is low; because $C_1^L = P_1^P = .7$, C_2^L = P_2^P = .3, d_1^L = .3, d_2^L = 0, and a_1^P = .5, debt capacity when the loan is the sole asset is only .3. But because the liquidation value of the loan is small compared to the cashflows it produces, the project loan is a great asset for an overly liquid firm. Such a firm can borrow \$1 against every loan of \$1 it makes to a project. In fact, given its stock of (overly) liquid core assets, it can loan to five projects before it loses its comparative advantage in making loans. Intermediation pays, because the projects each get \$ 1 in loans from the firm rather than the \$.8 they can raise directly from individuals. The firm can raise this money directly from individual investors because they can enforce payments by threatening to liquidate assets (and the firm's liquid core assets provide enough value to make this credible). It is also easy to check that the firm will not transform its core assets selectively, because the loans will then be seized by creditors with the attendant loss in value.

All the above is predicated on loans having no secondary market. What if there is one, so that the firm's loans can be sold to other institutional investors? Not only does this open up transformation possibilities for the firm, but also allows individual lenders to seize loans and sell them to other institutions. For simplicity, we will assume an intrinsic liquidity of 1 for the loan and flexibility of 1 so that the loan can be sold for $a_F^P C_2 + \alpha^P d_2^P$ if seized before date 1, $Min[a_F^P C_2 + \alpha^P d_2^P, P_2^P]$ if seized at date 1. $Min[\alpha^P d_2^P, P_2^P]$ if seized after date 1 but before date 2, and 0 after date 2.

<u>Corollary 3:</u> When a secondary loan market opens, the incremental debt capacity an overly liquid firm obtains by making a loan is zero.

Proof: See appendix.

When a secondary market opens up, loans can be sold for their intrinsic value. There is a dramatic shift in comparative advantage in financing loans. Loans are too liquid, so the transformation risk constraint is not relaxed at all. The overly liquid firm does not get any additional debt capacity by making the liquid loan. Overly liquid firms will be disintermediated.

2.2. The origins of banking.

It is interesting to examine the historical origins of banks (defined as deposit taking intermediaries who also make loans) with our model in mind. De Roover (1948), in his classic history of the evolution of money, banking and credit in medieval Bruges, describes three types of financial institutions.²¹

- 1. The merchant-bankers were the local representatives of far-flung trading empires. The firms were partnerships, financed largely through personal capital and long-term deposits from wealthy Italian families. Because their primary business was trading, and not banking, these firms did not generally take in local demand deposits. They did, however, make short term credit available in the course of their international transfers of funds.
- 2. Pawn-brokers made collateralized loans, with security ranging from clothes and agricultural implements to jewellery. But the pawnbrokers did not work with other people's money; they depended largely on their own financial resources. When they did take in time deposits, they had to offer a return which was well above that on other investments of comparable security.
- 3. Third were the *moneychangers*, the true precursors of the modern bank. The activity of moneychangers was originally confined to trade in bullion and the exchange of coins. But coins in the Middle Ages were not uniform (because coinage was imperfect), and their quality was hard to evaluate.²² It made sense to minimize the amount of transactions done using coins. Moneychangers started taking in demand deposits primarily to create a payments system. They facilitated trade by making

²¹ Lane and Mueller (1985) argue that this classification held generally throughout mediaeval Europe.

²² Gresham's Law ensured that the best coins were kept back while the worst coins -- the most worn, clipped or debased ones -- were culled and offered for trade. An intimate knowledge of coins and the state of finances of the local issuing authority (so as to predict the direction of seigniorage) was a great advantage. This lead to considerable asymmetric information about the worth of money.

transfers between individuals (or firms) with simple accounting adjustments, without going through the actual process of transferring real (and suspect) money.

Moneychangers maintained reserves of over 30 percent. Our model suggests that the liquidity of their assets gave them a comparative advantage in making illiquid investments, for example unsecured overdrafts to depositors. The overdrafts were not self-liquidating loans. They could stay open on the books for an indefinite period. Thus borrowers could obtain long-term working capital which was hard for the moneylenders to liquidate surreptiously in times of stress.

The other main outlet for the moneychanger's funds was direct investment in business. For instance, Collard de Marke, a prominent moneychanger of Bruges, was also engaged in the trade of cloth. Our model suggests that these illiquid loans and investments served to bind the considerable liquid assets the moneychanger had to maintain to service deposits.²³

Our theory can also explain why the moneychangers subjected themselves to the risk of illiquidity and left more liquid secured loan opportunities to pawnbrokers. De Roover offers regulation and the opprobrium associated with usury as explanations. But regulations are endogenous, and moneychangers could have disguised the interest in their loans. We say that, given the overhang of liquidity from the deposit business, moneychangers had a comparative disadvantage in holding the liquid collateral from pawnbroker loans. Conversely, given the liquidity of their loans, pawnbrokers had a comparative disadvantage in maintaining the liquidity needed to service demand deposits, and had a hard time attracting time deposits. Consequently, they were largely self-financed.²⁴

Our explanation of the association between demand deposits and illiquid loans contrasts with the existing literature. Diamond and Dybvig (1983) argue that banks exist because individuals, faced with

²³ It is also possible for the owners of illiquid assets to accept liquid cash deposits for safe-keeping. For instance, the innkeepers of Bruges used to perform this function, perhaps offering their illiquid reputation or inns implicitly as collateral. Similarly, Usher (1943, p. 19) reports that "in many instances, individuals and families [in fourteenth and fifteenth century Europe] owned both a trading and a banking enterprise...it is difficult to decide which of the enterprises was the more important."

²⁴ Not all early bankers abstained entirely from pawnbroking. The goldsmith bankers in Britain did make loans against jewelry, probably because knowledge derived from their main business.

uncertain consumption needs, want to be able to withdraw savings on demand. By diversifying the idiosyncratic consumption demands of individuals over a large number of such investors, banks can fund long-term projects with short-term deposits. Thus banks' essential role is liquidity transformation.²⁵ This, however, presupposes an excess supply of illiquid projects relative to savings that are not subject to liquidity demands. Our model says that banks can make illiquid loans even when this is not true. As our evidence from mediaeval Europe shows, there were profitable collateralized liquid investments that banks chose to forego.²⁶

Another strand of the literature starts with the notion that firms need long-term illiquid funding. Because firms are subject to moral hazard, the loans need to be monitored. Free-rider problems and the high costs for individuals of personally monitoring firms result in delegating bank monitoring. The liabilities of the bank are then structured to minimize the cost of monitoring the bank. Calomiris and Kahn (1991) argue that the first-come, first-served nature of bank deposits will give large depositors an incentive to monitor the bank on behalf of small depositors. This will keep bank management on the straight and narrow path at low cost.

Our theory is not inconsistent with this, but we differ in emphasis and causality. It is because banks have to maintain liquid reserves to service demand deposits that they make illiquid loans. An incidental (though not inconsequential) effect of the demandable nature of deposits is to keep bank management honest. By contrast, the primary role of banks in the papers just discussed is to make loans, and the optimal structure of bank liabilities is, only as a consequence, short term.

²⁵ The logical conclusion of the Diamond-Dybvig model is that the government is best suited to transform liquidity. There is some evidence that the deposit and transfer business was deemed so important that city governments stepped in to offer the service at public banks when private banks were in trouble. An example of this is the Taula in Barcelona (Lane and Mueller (1985)). But to a large extent, the funds deposited were not transformed to private loans but into loans to the city government.

²⁶ The average interest rate for the relatively risk-free pawnbroker loan was approximately 43 percent.

²⁷ See Diamond (1984), Calomiris and Kahn (1991) and Flannery (1994).

2.3. ... and disintermediation.

Banks have come a long way from mediaeval Europe. With the advent of central banks, reserves no longer had to be maintained on the bank premises. The fear of the banker running away with the money is obviously lower. But at the same time, most large banks are no longer locked in to local community loans that are publicly observable and illiquid. Bank loans have become much more liquid and fungible. As a result, transformation risk emanates from the assets that used to insure against it. This change causes, or at least abets, disintermediation, the movement of more creditworthy firms away from borrowing from financial intermediaries to direct market financing.

Disintermediation dates from the early 1960s in the United States and the early 1980s in Japan.²³ One possible explanation is technological — that somehow the technology of public monitoring and control improved to allow public investors to monitor firms at low cost, and thus led to disintermediation. But why did technological change not also reduce banks' cost of monitoring, retaining their relative advantage over investors? Furthermore, why does disintermediation seem to be episodic rather than secular? Kroszner and Rajan (1994) document a similar movement of firms away from banks to markets in the U.S. in the 1920s. Japanese firms seem to be returning to bank borrowing after the collapse of the stock market in the early 1990s. (Does the cost of accessing the public market fall as the securities market rises? But then why does the cost of bank funding also not fall simultaneously?)

Consider our explanation. We have shown that an increase in the intrinsic liquidity of an overly liquid firm's assets increases the liquidity overhang and makes it profitable for the firm to finance even more illiquid projects. Thus the spectrum of possibilities the firm can profitably exploit expands at the illiquid end.

How does this explain disintermediation? Bank loans to large public corporations are especially liquid — easily repaid or sold — when the access for these corporations to public markets improves. The increased liquidity of these loans makes them unattractive assets for the overly liquid bank. In addition,

²⁸ See Hoshi, Kashyap and Scharfstein (1990).

profitable opportunities open up for the bank at the lower end of the liquidity spectrum — among small firms and the middle market. Thus, the asset liquidity stemming from a rising market shifts bank loan portfolios from focussing on large firms to smaller, potentially riskier firms. The "best" firms appear to disintermediate. However, this is not always permanent: a decline in the ease of access to public markets, or a decrease in the liquidity of the loan sales market, can restore intermediation.²⁹

Secular trends in disintermediation can be consistent with our theory. We argue that the role of the bank in making illiquid loans depends on a profitable franchise servicing demand deposits (or some other liquid asset). If this franchise's value dissipates, the bank's comparative advantage in making loans will also decline.

In many developing countries, deposit rates are set by a government-blessed cartel. This creates substantial franchise value in deposit taking, and consequently a strong incentive to make loans.³⁰ Our model suggests that liberalization of deposit rates will have a strong adverse effect on bank lending simply because the bank's comparative advantage in lending derives from the deposit franchise.

2.4. The Feedback between Liquidity and Flexibility.

We expect intermediaries to offset an increase in the liquidity of core assets with more illiquid assets or businesses. This may explain the desire of banks to become *universal banks*. If, however, flexibility is not important, the borrower can hive liquid assets off into a separate corporate entity, and

²⁹ Note that our explanation does not directly impose a time-varying cost differential between the cost of direct funds and the cost of intermediated funds. Instead, the differential is obtained through changes in liquidity, which is the exogenous variable throughout this paper. Other explanations for the increases in the liquidity of bank loans are loan sales (see Greenbaum and Thakor (1987), Santomero and Tester (1994)). Also, if loans to the best clients are overly liquid, illiquid firms will have a comparative advantage in making them. This would suggest that finance companies with the relatively illiquid reputations or businesses of their parents as assets, will increasingly attract the banks' best clients. In response to this banks themselves might try to develop illiquid businesses or profitable franchises that help them keep good clients. The higher the value of these franchises, the higher the potential credit rating of the bank. This would suggest a positive correlation between the rating of a bank and the rating of clients it can lend to.

³⁰ Keeley (1990) advances the related "charter value" hypothesis: the greater the value of bank ownership, the stronger are the incentives for banks to protect bank solvency and charter values through increased capitalization. We differ in emphasizing the role of liquidity; charter value provided by overly liquid operations cannot bond other liquid assets.

set its flexibility to zero. This, in a sense, is the process of securitization. For instance, a bank originating mortgages does not benefit greatly from trading them. It makes sense to set up a special purpose vehicle to hold these mortgages, and limit the flexibility of the vehicles to transform or consume the assets. The special purpose vehicle can obtain financing more easily than the bank could if it held onto the liquid loans. Similarly, money market mutual funds are constrained through legal means and regulatory oversight, and can hold liquid assets that banks cannot hold.

A substantial legal, regulatory, and monitoring apparatus is required to enable the bank to give up flexibility and allow securitization to take place. While thus far we have focussed on exogenous changes in asset liquidity on portfolio holdings, we could also ask about the effects of exogenous changes in flexibility. For instance, greater regulatory or external scrutiny of banks is tantamount to reducing bank flexibility. A lower b reduces the extent to which banks are "excessively liquid", and reduces their comparative advantage in holding illiquid assets. Thus periods of extensive regulatory scrutiny of bank assets will be accompanied by a portfolio shift towards more liquid assets, even if regulators do not actively encourage such a shift.³¹

Section 3

We have not considered the effects of uncertain shocks or cash constraints. In this section, we examine some aspects of both. We also examine liquidation policies when the firm has multiple assets.

3.1. Uncertainty about cashflows.

Suppose there is a publicly observable shock at date 1/4. The shock changes future cash flows

³¹ While there are more recent examples, consider the evolution of bank lending in New England depicted in Lamoureaux (1994). The early banks in New England were limited in making outside loans because of substantial asymmetric information between them and potential borrowers. The bank owners, therefore, retained considerable flexibility in making loans to their own businesses. Given this flexibility, only businessmen with substantial illiquid reputations (and illiquid businesses) to stake could open banks. Furthermore, the assets of these banks were long term investments rather than loans. Towards the end of the 19th century, a reform movement sprang up to make bank management more "professional" and less entrepreneurial. Outsiders were brought on to bank boards. Regulators, who were previously ineffectual, rode on the coattails of this movement and subjected banks to greater scrutiny. Bank loans became much shorter term and self-liquidating. We would argue that this increased liquidity of bank assets was partly facilitated by the exogenous decrease in flexibility imposed by the reform movement. Lamoureaux also suggests that the reform movement hurt bank financing of businesses.

or depreciated asset values, so that the debt repayment schedule agreed to at date 0 no longer works. The face value of the initially contracted debt cannot be made contingent on the shock, though we assume that the lender can write in a "material change" clause, so that the debt becomes payable if the shock hits. By date 1/4, it is too late for the lender to prevent C₁ from being produced at date 1, but the lender has the ability to liquidate the assets.

Let $T = C_1 + C_2 + d_2 - b\alpha d_1$ be the debt capacity as determined by the transformation constraint, $L = \alpha d_1$ be that determined by the liquidation constraint. $B = P_1 + P_2$ is the contracted face value.

Lemma 3:

- (i) If $T \ge B$ the shock has no effect on debt payments.
- (ii) If Min $[B, L] \ge T$, the sum of debt payments at date 1 and date 2 is renegotiated down to T. and the borrower has to make an immediate payment of Min [B, L] T or face liquidation of some assets.
- (iii) If $B \ge T \ge L$, the sum of debt payments at date 1 and date 2 is renegotiated down to T, and no immediate payment is made.

It is only when the limit on debt imposed by transformation risk, $C_1 + C_2 + d_2 - b\alpha d_1$, is lower than the required payments $P_1 + P_2$ that the shock forces immediate renegotiation at date 1/4 (else all renegotiation can be postponed to date 1). There is an important difference between the renegotiation at date 1/4 described by lemma 3 and the renegotiation at date 1 described by lemma 1. As lemma 3 indicates, the going concern debt capacity, aC_2+d_2 , has no bearing on the renegotiations at date 1/4. Unlike liquidation value, which can be realized immediately, going concern debt capacity is based on future threats to affect cashflows which the lender cannot credibly commit to at date 1/4. Therefore, it has no impact on the renegotiation.³²

This may explain why lending against cashflows is riskier than lending against assets even though, in principle, both give the lender the ability to extract repayments. The problem with lending against cashflows is that the threat to destroy future cashflows is not credible when the borrower has the more pressing threat of transforming assets. So the "cashflow lender" has to renegotiate the value of his claims down even if the going concern debt capacity of the firm is unchanged. By contrast, a lender who lends against liquidation value always has a credible immediate threat.

The wedge between liquidation value and transformation risk forces immediate repayment (lemma 3, (ii)). In essence, the lender cannot trust the borrower to wait till date 1 without transforming the assets. The level of debt that the borrower can be trusted with, T, is less that what the lender can get by liquidating the assets Min [B,L]. So the lender will agree to a renegotiated face value of T only if the borrower also pays Min [B,L] -T in cash immediately.

Thus far we have assumed that the firm has unlimited access to cash and can make all enforceable payments. We now relax this assumption also. If the firm has to make enforceable payments (as in the situation described by lemma 3, (ii)) and it is cash constrained, the lender may force the borrower to liquidate assets to repay debt. This is costly. So rather than borrowing all that the lender is willing to offer at date 0, the borrower may voluntarily limit debt in order to minimize liquidation costs. This is what we now examine.

3.2. Cash Constraints and Optimal Leverage.

Consider the case when the borrower has no cash at date 1/4. When Min [B, L] \geq T, the lender will force the borrower to liquidate assets.³³ If γ is the fraction liquidated, it can be shown that

$$\gamma L + (1 - \gamma)T = Min\{L, B\}$$

Thus $\gamma = 1$ if $B \ge L$ and $\gamma = (B-T)/(L-T)$ when B < L. The welfare cost of this liquidation is $\gamma (C_1 + C_2 + d_2 - \alpha d_1)$.

After the renegotiation at date 1/4, it is quite possible that payments are further renegotiated at date 1 or 2. To highlight the important effects, we assume that after the renegotiation and potential liquidation at date 1/4, cashflows are enough to meet subsequent debt payments so that no further liquidation (or renegotiation) is warranted. Furthermore, we restrict uncertainty at date 0 to C₁. Uncertainty about other variables is equally easily analyzed.

³³ When assets are to be liquidated to pay down debt, we assume they are chosen by the borrower after which the borrower and lender jointly liquidate them. Therefore, liquidation value does not depend on flexibility. We maintain the assumption that the borrower has to transform all the assets or none.

Let the distribution of C_1 have density g and support $[\underline{C_1}, \overline{C_1}]$. Only T depends on C_1 (see Figure 3). Therefore at date 0, the firm expects a welfare loss due to liquidation at date 1/4 of

$$\int_{C_{1}}^{\pi C_{1} \to B} \left(\frac{B - T(C_{1})}{L - T(C_{1})} \right) \left(C_{1} + C_{2} + d_{2} - \alpha d_{1} \right) g(C_{1}) dC_{1} \qquad if \quad B < L \\
\int_{C_{1}}^{\pi C_{1} \to L} \left(C_{1} + C_{2} + d_{2} - \alpha d_{1} \right) g(C_{1}) dC_{1} \qquad if \quad B \ge L$$

where $C_1^{T(C_1)^{-B}}$ is the minimum value of C_1 such that the debt capacity determined by transformation risk equals the contracted payments B. So long as the contracted payments are less than the date-1 liquidation value, L, an increase in B increases the welfare loss due to liquidation, because it increases the range of cashflow realizations for which liquidation takes place (i.e., increases $C_1^{T(C_1)^{-B}}$), and it increases the fraction γ of assets that have to be liquidated to satisfy the lender. An increase in B when it is above L does not affect the welfare loss because the lender can enforce only L.

The lender will make a loan equal to the amount he expects to get back. At date 0, and under the assumption that liquidation debt capacity dominates going concern debt capacity (the reverse case is equally easy), this is B, if B < L, and L if $B \ge L$.

When B < L, an increase in the face value of debt by a dollar reduces the internal equity that has to be committed by \$1, thus reducing the cost of financing by θ . In determining the optimal amount to borrow, B*, the firm trades off the increased cost of liquidation with additional debt against the reduced need for costly internal equity. Since the liquidation loss with an additional dollar in face value of debt increases with B so long as B < L, the firm will take on debt until the marginal liquidation loss with an additional dollar is θ , or B=L, whichever occurs first.

Example continued: Recall that the overly liquid firm in our example could make loans to five identical projects. The combined entity had $C_2 = 2.5$, $d_1 = 6.5$ and $d_2 = 4$. The date-1 cashflow, C_1 , was 4.5, but now we assume it to be uniformly distributed between 0 and 9. Finally, assume the excess cost of equity, θ , equals 2. The optimal debt levels are plotted in Figure 3 for different levels of asset

liquidity. Optimal debt increases in asset liquidity (because the cost of inefficient liquidation is less as assets become more liquid) until transformation risk starts binding, when optimal debt decreases in liquidity.

3.3. Multiple assets.

Thus far, we have examined renegotiation and liquidation at date 1/4 assuming that the renegotiated value of the debt is paid in full at dates 1 and 2. Of course, it is quite possible that further renegotiation take place at date 1 and date 2. We will not go over this ground again. But it is worth pointing out that when asset liquidity varies over time, it is not necessarily the asset with the highest current liquidity that is sold to pay down debt. To see this, assume the initial investment is in two assets, A and B, each of value 1/2. The assets are indexed by superscript i. We allow the intrinsic liquidity of the assets, α_t^i , to change over time. Let us assume the lender can enforce a greater payment than the borrower has the cash to make at date 1. We are interested in the borrower's marginal incentive to liquidate each asset. If future considerations are unimportant, it is trivial that the most liquid asset is liquidated to raise cash to pay debt. But asset liquidation affects future debt capacity. It is easily shown that

<u>Lemma 4:</u> If transformation risk does not bind at date 1 1/2, the marginal asset liquidated will be asset

A if

$$\alpha_1^A d_1 - \alpha_2^A d_2 > \alpha_1^B d_1 - \alpha_2^B d_2 \tag{18}$$

and asset B otherwise. If transformation risk binds at date 1 1/2, the marginal asset liquidated will be asset A if

$$\alpha_1^A d_1 + b \alpha_2^A d_2 > \alpha_1^B d_1 + b \alpha_2^B d_2$$
 (19)

and asset B otherwise.

Proof: See appendix.

By liquidating an asset, the borrower raises cash to pay down debt. So it is natural that the borrower cares about current intrinsic liquidity of the asset. But she cares about future liquidity also, even

if the asset will not be liquidated at the margin in the future. This is because liquidity affects future debt capacity. Total asset liquidation is minimized by liquidating the asset which raises the most cash for the least loss in future debt capacity. If liquidation value determines debt capacity, (18) suggests that a borrower may not liquidate an asset with high current and future liquidity, preferring instead to liquidate an asset with low current but even lower future liquidity.

But when transformation risk binds, the borrower minimizes liquidation by selling an asset with the highest sum of current and future liquidity. Thus the best asset to sell may be one whose liquidity is temporarily depressed. It is true that the borrower raises less cash by selling it. But because the borrower has a liquidity overhang, this loss may be more than made up by the increase in debt capacity as the future balance sheet becomes less liquid. The total amount of liquidation is consequently lower.

Lemma 4 could therefore define the different responses of liquid and overly liquid firms to a systematic adverse shock. For liquid firms, perceptions of lower future liquidity for an asset leads to current sales, which in turn may push down perceptions of liquidity even further. This is an unstable equilibrium, reminiscent of Fisher's debt-deflation theory (also see Kiyotaki and Moore (1993)).

But the overly liquid firm is motivated to sell different assets and the equilibrium is self-correcting: if the adverse shock affects a large number of overly liquid firms in the economy, they all have the incentive to sell their most liquid assets in order to reduce debt levels. If firms in the same line of business have similar liquid assets, mass selling will temporarily depress the liquidation value of the most liquid asset. But it is precisely because firms know that liquidity will recover in the future that they continue to sell. This rational rush to the exit will further depress liquidation values, and increase the amount of liquidation. Eventually, of course, the liquidation value will be depressed so far that it makes sense to sell another asset. It is in this sense that systematic shocks to overly liquid firms can lead to a temporary depression in asset values.

Of course, selling the asset at a depressed price does not make much sense. So the overly liquid firm has a strong incentive to deal with a temporary crisis by reducing its flexibility, either by pledging assets or getting out of activities that involve high transformation risk.

Conclusion.

Much of the earlier literature has taken the assets of a firm as given and focussed on the liability side. In this paper, we explore how a firm's choice of additional assets may depend on the assets used in its core business. Our theory offers a different way of thinking about intermediation and disintermediation. Policymakers, for example, should note that exogenous changes in liquidity, — the development of a secondary market for bank loans, for example, or expansion of trading of derivatives correlated with banks' traditional assets — may have substantial impacts on the comparative advantage of financial institutions. The increasing movement of banks into illiquid businesses may be a natural response to changes in the liquidity of banks' core businesses. Changes in regulations affecting the intrinsic liquidity of financial institutions — such as changes in reserve requirements, changes in the cost of access to the discount window, and changes in the franchise value of liquid businesses like servicing demand deposits — can affect the other businesses that institutions undertake.

Various implications for firm and creditor behavior have been left unexplored. For instance, having contracted longer maturity debt, firms have an incentive to reduce the liquidity of their assets in order to reduce the value of the debt they will have to repay. Conversely, existing creditors have an incentive to encourage firms to take on more liquid new assets (assuming this does not trigger transformation) because this enhances the value of their claim. This is analogous to the underinvestment problem (Myers (1977)), the difference being that the assets themselves have spillover effects. Collateralizing the new assets may be a way of preventing the liquidity of the new assets from spilling over and enhancing the power of old creditors (also see Stulz and Johnson (1985)).

While our theory has been developed in the context of assets that are hard to pledge because they are needed for operations, it is easy to extend this to conglomerates. A conglomerate can be thought of as a trader of companies. The conglomerate will be unwilling to accept limits on its freedom to trade companies because this will make it harder to take advantage of market opportunities. In other words, a need for strategic flexibility may make it impossible to pledge assets. Our theory can then be extended to understanding the kinds of assets that are held together in a conglomerate (also see Kahn (1992)).

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Appendix

Proof of proposition 1.

It is possible that some of the three constraints, (a), (b), and (c), that precede proposition 1 may not bind for any $\alpha \in [0,1]$. To make the problem interesting (and coincidentally, to reduce the number of cases examined), we assume that each constraint binds over a non-empty range so that $0 < \alpha_L < \alpha_{LL} < 1$ for both the project and the firm. To demonstrate the generality of these propositions, we prove them with an arbitrary b. See Section 1.5.

(i) Denote the stand alone debt capacity for the firm by B^F, for the project by B^P, and for the combined entity by B^{F+P}. We know that debt capacity for any entity is given by

Min { Max
$$[aC_1 + \alpha d_2, \alpha d_1]$$
, $C_1 + C_2 + d_2 - b\alpha d_1$ }

Supposing both firm and project are illiquid so that $B^F = a^F C_2^F + \alpha^F d_2^F$ and $B^P = a^P C_2^P + \alpha^P d_2^P$. Then it is clear that debt capacities for the combined firm will be additive. In other words, because neither liquidation value, αd_i , nor transformation risk, $C_1 + C_2 + d_2 - b\alpha d_i$, bind for the stand alone firm or project, they should not bind for the combined entity. Similarly for the other cases.

(ii) In this case
$$B^F = Max [a^F C_2^F + \alpha^F d_2^F, \alpha^F d_I^F] = \alpha^F d_I^F$$

$$B^P = Max [a^P C_2^P + \alpha^P d_2^P, \alpha^P d_I^P] = a^P C_2^P + \alpha^P d_2^P$$
Therefore, $B^{F+P} = Max [a^F C_2^F + \alpha^F d_2^F + a^P C_2^P + \alpha^P d_2^P, \alpha^F d_I^F + \alpha^P d_I^P]$

$$\leq \alpha^F d_I^F + a^P C_2^P + \alpha^P d_2^P$$

$$\leq B^F + B^P$$

Note that transformation risk does not bind on a stand alone basis, and consequently does not bind when the project and firm are combined. Another way of seeing this result is that the maximum of the sums is less than the sum of the maximums.

(iii) Let the range of projects that the overly liquid firm have an absolute advantage in financing in-house be $[\underline{\alpha}^P, \overline{\alpha}^P]$. We start by arguing that the overly liquid firm can obtain strictly more finance for all liquid projects than they can get on a stand alone basis. By definition, we know that for an overly liquid firm

$$B^{F} = C_{1}^{F} + C_{2}^{F} + d_{2}^{F} - b^{F} \alpha^{F} d_{1}^{F} < \alpha^{F} d_{1}^{F}$$
 (20)

Also, because $\alpha_L < \alpha_{LL}$, the liquidation value rather than continuation value would determine debt capacity if transformation risk were not binding. So

Max
$$[a^FC_2^F + \alpha^Fd_2^F, \alpha^Fd_I^F] = \alpha^Fd_I^F$$
 (21)

For a liquid project,

$$B^{P} = \text{Max} \left[a^{P} C_{1}^{P} + \alpha^{P} d_{2}^{P}, \alpha^{P} d_{I}^{P} \right] = \alpha^{P} d_{I}^{P} < C_{1}^{P} + C_{2}^{P} + d_{2}^{P} - b^{P} \alpha^{P} d_{I}^{P}$$
 (22)

Because continuation value does not determine debt capacity for either project or firm on a stand alone basis, it should not determine debt capacity when the two are combined. This implies that the combined firm and project is either liquid or overly liquid.

If liquid,
$$B^{F+P} = \alpha^F d_1^F + \alpha^P d_1^P > C_1^F + C_2^F + d_2^F - b^F \alpha^F d_1^F + \alpha^P d_1^P$$
 (from (20)).
 $\geq B^F + B^P$.

If overly liquid,
$$B^{F+P} = C_1^F + C_2^F + d_2^F - b^F \alpha^F d_1^F + C_1^P + C_2^P + d_2^P - b^P \alpha^P d_1^P$$

 $> C_1^F + C_2^F + d_2^F - b^F \alpha^F d_1^F + \alpha^P d_1^P$ (from (22)).
 $\geq B^F + B^P$.

This proves that there exist projects for which the overly liquid firm can raise more finance when the projects are done in-house than on a stand alone basis. Also, because the overly liquid firm has no comparative advantage in funding overly liquid projects, the highest intrinsic liquidity that can be advantageously financed in-house is the liquid project with the highest intrinsic liquidity. Therefore,

$$\overline{\alpha}^{P} = \alpha_{r}^{P}$$
.

Now we determine the lowest quality project that can advantageously be funded by the overly liquid firm. The proof is by construction. Note that from what we have just proved, this project has to be a illiquid one, i.e., $0 \le \underline{\alpha}^P < \alpha_L$. We first find the lowest project intrinsic liquidity such that the combined entity is just overly liquid. Let this be p. It is the smallest α^P that solves

Min { Max [
$$a^{F}C_{2}^{F} + \alpha^{F}d_{2}^{F} + a^{P}C_{2}^{P} + \alpha^{P}d_{2}^{P}, \alpha^{F}d_{1}^{F} + \alpha^{P}d_{1}^{P}], C_{1}^{F} + C_{2}^{F} + d_{2}^{F} - b^{F}\alpha^{F}d_{1}^{F} + C_{1}^{P} + C_{2}^{P} + d_{2}^{P} - b^{P}\alpha^{P}d_{1}^{P}]$$

$$= C_{1}^{F} + C_{2}^{F} + d_{2}^{F} - b^{F}\alpha^{F}d_{1}^{F} + C_{1}^{P} + C_{2}^{P} + d_{2}^{P} - b^{P}\alpha^{P}d_{1}^{P}$$
(23)

Since (23) is satisfied for $\alpha^P = \alpha_{LL}^P$, by continuity either a positive l exists, or (23) is satisfied even when $\alpha^P = 0$. If so, all illiquid projects can be more advantageously financed within the firm. This is because for the illiquid project, $C_1^P + C_2^P + d_2^P - b^P \alpha^P d_1^P \ge a^P C_2^P + \alpha^P d_2^P$, so the right hand side of (23) is greater than $B^F + B^P$.

If $0 < l < \alpha_{LL}^P$, then let $\underline{l} < l$ be the lowest project intrinsic liquidity such that the combined entity is just liquid, i.e.,

$$\underline{l} = (a^{F}C_{2}^{F} + \alpha^{F}d_{2}^{F} + a^{P}C_{2}^{P} + \alpha^{P}d_{2}^{P} - \alpha^{F}d_{1}^{F})/d_{1}^{P}$$

If this number is less than zero, set $\underline{l} = 0$.

We now check if $B^{F+P} > B^F + B^P$ at $\alpha^P = \underline{l}$.

If yes, then a reduction in the liquidity of the project changes neither side of the above inequality (since the combined entity and the stand alone project are both illiquid, their debt capacities vary in the same way with project liquidity). Consequently, all projects of lower liquidity can be advantageously financed in-house and $\underline{\alpha}^P = 0$.

If no, we look for the minimum α^P such that $\underline{l} < \alpha^P < l$ and

$$\alpha^{F}d_{1}^{F} + \alpha^{P}d_{1}^{P} \ge C_{1}^{F} + C_{2}^{F} + d_{2}^{F} - b^{F}\alpha^{F}d_{1}^{F} + a^{P}C_{2}^{P} + \alpha^{P}d_{2}^{P}$$

$$\text{Thus } \alpha^{P} = [C_{1}^{F} + C_{2}^{F} + d_{2}^{F} - b^{F}\alpha^{F}d_{1}^{F} - \alpha^{F}d_{1}^{F} + a^{P}C_{2}^{P} + \alpha^{P}d_{2}^{P}]/d_{1}^{P}$$

Since (24) is certainly true at $\alpha^P = l$, and the left hand side of (24) increases at a faster rate with α^P than the right hand side, by continuity, α^P must exist. Q.E.D.

Proof of corollary 1:

From the construction in the proof to Proposition 1 (iii), we know that

$$\overline{\alpha}^{P} = \alpha_{11}$$

which does not depend on the intrinsic liquidity of the firm.

Also
$$\underline{\alpha}^P = 0$$
 or $\underline{\alpha}^P = [C_1^F + C_2^F + d_2^F - b^F \alpha^F d_1^F - \alpha^F d_1^F + a^P C_2^P + \alpha^P d_2^P]/d_1^P$
So α^P (weakly) decreases in α^F .

We have not yet determined α^{P} . We determine it by construction.

First we make the following assertions which follow directly from definitions:

- 1. If for a given α^P , the combination of the (liquid or illiquid) project and the firm is overly liquid, then the difference between combined debt capacity and the sum of stand-alone debt capacities can be increased by decreasing α^P (unless $\alpha^P = 0$). This is because a marginal decrease in intrinsic liquidity of the project will (weakly) decrease its stand-alone debt capacity and increase combined debt capacity. If the combined entity is overly liquid even when $\alpha^P = 0$, then $\alpha^{P^*} = 0$. Otherwise, α^{P^*} cannot be such that the combined entity is overly liquid.
- 2. Over the range of project liquidity where both the project and the combined entity are liquid, there is no change in the difference between combined debt capacity and the sum of stand-alone debt capacities with changes in project liquidity. This is because an increase in the liquidity of the project increases both combined debt capacity and stand-alone debt capacity by the same amount.
- 3. If the combined entity is liquid when the project is illiquid, the difference between combined debt capacity and the sum of stand-alone debt capacities increases in the intrinsic liquidity of the project. This

is because an increase in the liquidity of the project increases combined debt capacity by more than it increases stand-alone debt capacity.

- 4. The combined entity cannot be illiquid when the project is liquid (because the firm is overly liquid). So the final possibility is that the combined entity is illiquid when the project is illiquid, in which case there is no change in the difference between combined debt capacity and the sum of stand-alone debt capacities with a change in project liquidity.
- From 1, 2, 3, and 4, the effect of changes in project liquidity on the difference between combined debt capacity and the sum of stand-alone debt capacities depend on whether the project is liquid or illiquid, and on whether the combined entity is overly liquid, liquid or illiquid. The project liquidity that results in the largest difference is easily found by considering the combined debt capacity when $\alpha^p = \alpha_L$. Recall that this is the level of intrinsic project liquidity that separates liquid projects from illiquid projects.

Case 1: If B^{F+P} is overly liquid when $\alpha^P = \alpha_L$, the difference between combined debt capacity and stand alone capacity can be increased by reducing α^P (assertion 1) upto the point that the combined entity is just overly liquid. As defined in the proof to proposition 1, this is $\alpha^P = l$. Note that the project is illiquid when α^P is below α_L , so the difference cannot be enhanced by decreasing project liquidity further (assertion 3 and 4).

Therefore $\alpha^{P^{\bullet}}$ is the highest intrinsic liquidity that equates

$$\max \left[a^{F}C_{2}^{F} + \alpha^{F}d_{2}^{F} + a^{P}C_{2}^{P} + \alpha^{P}d_{2}^{P}, \alpha^{F}d_{1}^{F} + \alpha^{P}d_{1}^{P} \right] = C_{1}^{F} + C_{2}^{F} + d_{2}^{F} - b^{F}\alpha^{F}d_{1}^{F} + C_{1}^{P} + C_{2}^{P} + d_{2}^{P} - b^{P}\alpha^{P}d_{1}^{P}$$

or 0, whichever is higher.

Case 2: If B^{F+P} is liquid when $\alpha^P = \alpha_L$, from assertion (2) and assertion (3), there is a range of project liquidity $\alpha^{P^*} \in [\alpha_L, I]$ where the difference between combined debt capacity and stand alone capacity is maximized. I which is defined above is the maximum project liquidity such that the combined entity is liquid.

Finally, the combined entity cannot be illiquid, given that the firm is overly liquid, and the project is on the borderline.

Thus α^{P^*} is either a unique value or a range, and it is easily checked that if unique, it is weakly decreasing in α^F , and if a range, the upper limit is decreasing in α^F . Q.E.D.

Proof of proposition 2:

(i) By borrowing directly from investors, the project can raise $a^p_{\ l}C_2 + \alpha^p d^p_{\ l}$. When a firm with liquid or illiquid assets borrows against a loan to the project, it will be able to raise at most the higher of the liquidation value or going concern value of the loan. But according to lemma 2, this is $P_{\ l}^{\ p}$ which is less

than $\alpha^{\rho} d^{\rho}_{2}$. So a liquid or illiquid firm will be able to borrow less against the loan than the project can borrow directly.

(ii) We only have to show that it is possible for an overly liquid firm to add more debt capacity making a loan to a project than the project's stand alone debt capacity. Let the assets of the overly liquid firm be such that

$$C_1^F + C_2^F + d_2^F - 2\alpha^F d_1^P + (a_F^P C_2^P + \alpha^P d_2^P) < 0$$
 (25)

This implies that the core assets of the overly liquid firm are large compared to the cashflows of the firm or the project. The project loan increases the cashflows to the firm by $P_1^P + P_2^P = a^P_F C_2^P + \alpha^P d^P_2$, and loosens the transformation constraint by exactly this amount. But (25) ensures that debt capacity is still determined by transformation risk, even after the loan to the project is added to assets. So the incremental debt capacity the loan adds to the firm is $P_1^P + P_2^P = a^P_F C_2 + \alpha^P d^P_2 > a^P_1 C_2 + \alpha^P d^P_2$ where the last term in the inequality is the debt capacity of the project on a stand alone basis.

- (iii) Follows directly from corollary 2.
- (iv) Follows because $P_1^P + P_2^P$ increases in a_F^P .

Proof of corollary 3:

When the loan can be sold for its full face, the transformation value of the loan is exactly equal to the repayments that are due on it. So the loan does not reduce the transformation constraint at all. Hence the debt capacity contributed by the loan to a firm with overly liquid core assets is zero.

Proof of Lemma 4:

When liquidation value limits debt capacity, by liquidating a unit of asset i, the borrower generates $\alpha^i_1 d_1$ of cash and reduces future debt capacity by $\alpha^i_2 d_2$. So liquidation is minimized when i is chosen such that $\alpha^i_1 d_1 - \alpha^i_2 d_2$ is highest. When transformation risk limits debt capacity, by liquidating a unit of asset i, the borrower generates $\alpha^i_1 d_1$ of cash and increases future debt capacity by $b\alpha^i_2 d_2$. Hence the lemma.





