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ABSTRACT

The paper characterizes predictable components in excess rates of returns on major equity and foreign exchange markets using lagged excess returns, dividend yields, and forward premiums as instruments. Vector autoregressive techniques demonstrate one-step-ahead predictability and provide implied long-horizon statistics. We estimate latent variable models as constrained counterparts to the VARs. The predictability of returns is related to asset pricing models by examining the volatility bounds on intertemporal marginal rates of substitution.

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There is now considerable evidence that excess returns on a variety of assets are predictable. In equity markets, predictable returns have been documented using dividend yields, short-term interest rates, default spreads and yields in the term structure of interest rates as predictors.[1] In foreign exchange markets, predictable returns have been documented using the forward premium as a predictor.[2]

This paper integrates these literatures by characterizing the predictable components in excess returns in the equity markets of the U.S., Japan, the U.K. and Germany and in the foreign exchange markets of the dollar relative to the yen, the pound, and the deutschemark. We use dividend yields, forward premiums and lagged excess returns as predictors.[3] Our innovation is to investigate the equity and foreign exchange excess returns with vector autoregressive techniques, which allows us to calculate various long-horizon statistics. The importance of long-horizon predictability in equity returns has been stressed by Fama and French (1988a,b), Campbell and Shiller (1988), and in an international context by Cutler, Poterba and Summers (1989).

Our analysis answers questions like the following: "What is the variability of expected returns in equity and foreign exchange markets?" "Are equity markets characterized by mean reversion in stock prices?" "Do dividend yields predict long-horizon equity returns?" "Do exchange rates exhibit mean reversion at long horizons?" "Does a forward premium on the foreign currency predict appreciation of the domestic currency at all horizons?" Answers to questions such as these provide useful inputs for money managers who practice international asset allocation. Such individuals must forecast equity returns in different countries and must forecast changes in exchange rates.[4]

Once excess return predictability is established, one would like to know if the predictability is due to time varying risk premiums. If it is, a low dimensional factor structure may characterize co-movements in excess returns. We therefore investigate several "latent variable" models in an effort to determine the empirical plausibility of this argument and to document the integration of these markets.[5]

Variation in expected returns poses a challenge for asset pricing theory. One way to quantify this challenge is to examine volatility bounds on the intertemporal marginal rate of substitution implicit in an investor's Euler equation. Hansen and Jagannathan (1991) derive such bounds, and we extend their analysis to the international excess returns used in the paper.

The paper is organized as follows. Section I contains a discussion of the data and some summary statistics. Section II provides the estimation of the VARs. In this section we also consider an alternative formulation of the VARs in which we enter the two nominal interest rates rather than the forward premium which is the interest differential. The calculations of the long-horizon statistics are also reported here. Section III considers the latent variable models, and section IV contains estimation of the Hansen-Jagannathan (1991) bounds. The last section contains concluding remarks.

I. Data and Summary Statistics

To facilitate the presentation and discussion of our empirical analysis, consider the following definitions. We subscript variables of the four countries with numbers: 1 for the U.S., 2 for Japan, 3 for the U.K. and 4 for Germany. Let the one-month nominal interest rate denominated in currency j that is set at time t for delivery at time t+1 be i_{jt}. Define r_{jt+1} to be the continuously compounded one-month rate of return denominated in currency j in the equity market of country j in excess of i_{jt}. In the vector autoregressions we include the U.S. excess rate of return, r_{1t+1}, and a second country's excess equity rate of return denominated in currency j, r_{jt+1} for j equal to either 2, 3, or 4. Let the rate of return in dollars on an uncovered investment in the currency j money market in excess of the U.S. nominal interest rate be rs_{jt+1}, for j = 2, 3, 4. Including rs_{jt+1} in the VAR with r_{1t+1} and r_{jt+1} allows calculation of the excess rate of return on a country j equity investment from a dollar investor's perspective as $r_{jt+1} + rs_{jt+1}$.[6] Similarly, the currency j rate of return on a U.S. equity investment in excess of i_{jt} is obtained as $r_{1t+1} - rs_{jt+1}$.

To understand these calculations, consider the following analysis. Let S_{jt} be the dollar price of currency j. Then, the continuously compounded rate of depreciation of the dollar relative to currency j is $s_{jt+1} - s_{jt} = \ln(S_{jt+1}/S_{jt})$. The uncovered dollar return on a continuously compounded currency j money market investment is $\exp(i_{jt})(S_{jt+1}/S_{jt}) = \exp(i_{jt} + s_{jt+1} - s_{jt})$. Hence, the excess dollar rate of return on a currency j money market investment is

$$rs_{jt+1} = i_{jt} + s_{jt+1} - s_{jt} - i_{1t}. \tag{1}$$

Analogously, if the continuously compounded rate of return denominated in currency j in the country j equity market is R_{jt+1}, the dollar return in this equity market is $\exp(R_{jt+1} + s_{jt+1} - s_{jt})$. Hence, the excess rate of return from the U.S. perspective on a foreign equity market investment is $R_{jt+1} + s_{jt+1} - s_{jt} - i_{1t}$. Using equation (1) and the fact that $r_{jt+1} = R_{jt+1} - i_{jt}$, the excess rate of return from the U.S. perspective on a foreign equity market investment is $r_{jt+1} + rs_{jt+1}$.

From interest rate parity, the dollar return on a foreign money market investment that is covered in the forward foreign exchange market to eliminate foreign exchange risk is the U.S. nominal return. Hence,

$$i_{1t} = i_{jt} + f_{jt} - s_{jt} \tag{2}$$

where $f_{jt} - s_{jt} = \ln(F_{jt}/S_{jt})$ is the continuously compounded forward premium on the foreign currency, which we denote fp_{jt}. Substituting from equation (2) into equation (1) notice that $rs_{jt+1} = s_{jt+1} - f_{jt}$. This is how we measure the excess money market rates of return, and we will refer to them as returns in the foreign exchange market.

Morgan Stanley Capital International (MSCI) constructs monthly equity returns, and we obtained our data from Ibbotson Associates, who report a total return, capital appreciation, and an income return. Capital appreciation is the actual percentage change in price, but income return is an estimate of annualized dividends divided by the previous price. We use these series to calculate dividend yields as annualized dividends divided by current price for the U.S., Japan and the U.K.. Observations on dividend yields were compared to data from the Financial Times Actuaries, and two outlier observations for the U.K. and two for Japan were corrected. The German dividend yield series is taken from various issues of the Monthly Report of the Deutsche Bundesbank, Section VI., Table 6, from the column labelled "yields on shares including tax credit." We chose this series because beginning in January 1977, domestic investors in German equities receive a tax credit for the corporate tax paid on dividends, which eliminates the double taxation of dividends. The dividend yield in country j is denoted dy_{jt}.

Daily bid and ask exchange rate data were obtained from Citicorp Database Services. The data are captured from a Reuter's screen and represent quoted market prices. We ran several filter tests on the data to check for errors, and we corrected several with observations from the International Monetary Market Yearbook or the Wall Street Journal. Eurocurrency interest rate data, which are market determined interest rates, are from Data Resources, Inc.[7] Exchange rate and interest rate data are sampled at the end of the month, and we construct true returns by incorporating the market rules governing delivery on foreign exchange contracts. We also incorporate transactions costs by buying a currency at the bank's ask price and selling a currency at the bank's bid price for foreign exchange.

Some summary statistics on the data are reported in Table I. The monthly data are scaled by 1200 to express returns in percent per annum. The means of the excess equity rates of returns estimate the unconditional equity risk premiums in the different countries. The estimates are 5% for the U.S., 9% for the U.K., 10% for Germany, and 15% for Japan. The estimates of the unconditional means of the excess foreign exchange returns are -1% for the dollar-yen, -4% for the dollar-pound, and -3% for the dollar-DM.

The excess rates of returns are quite variable. The standard deviations of the annualized monthly data range from 57% for both the U.S. and Japan to 68% for the U.K. and 71% for Germany. The comparable statistics for the foreign exchange market excess returns indicate slightly less variability with standard deviations between 42% and 46%.[8]

The estimated autocorrelations of the excess rates of return are all small, while the autocorrelations of the dividend yields are all quite large. The autocorrelations for the forward premiums and interest rates are also large. The standard deviations of the dividend yields, the forward premiums and the interest rates are more than an order of magnitude smaller than those of the excess rates of return.

II. A Vector-Autoregressive Approach

One way to examine predictability of excess returns is to estimate a vector autoregression. We report two-country VARs for the United States and either Japan, the United Kingdom or Germany. In each VAR we include the U.S. equity market excess return, the companion country equity market excess return, the relevant foreign exchange market excess return, the two dividend yields, and the forward premium. For example, the U.S.-Japan VAR contains $Z_t = [r_{1t}, r_{2t}, rs_{2t}, dy_{1t}, dy_{2t}, fp_{2t}]'$.

If Z_t follows a first-order VAR,

$$Z_{t+1} = \alpha_0 + AZ_t + u_{t+1}, \tag{3}$$

where α_0 is a vector of constants, A is a (6 by 6) matrix, and u_{t+1} is the vector of innovations in Z_{t+1} relative to its past history. Higher order systems can be handled in exactly the same way by stacking the VAR into first-order companion form as in Campbell and Shiller (1988). In the three panels of Table II we report the values of the Schwarz (1978) criteria for the choice of lag length in a VAR. In all cases the minimized value of the criterion is associated with the first-order system.

We estimate equations (3) with ordinary least squares and report heteroskedasticity consistent standard errors for the parameters. We test one-step-ahead predictability of excess returns with a joint test of the six coefficients in the appropriate row of A. We also report the Cumby-Huizinga (1990) l-tests for serial correlation in the error processes.

Estimation of the parameters of the VAR completely characterizes the unconditional mean, variance and covariances of the Z_t process since the series are assumed to be covariance stationary. In this case, the moving-average representation of Z_{t+1} is

$$Z_{t+1} = \mu_0 + \sum_{j=0}^{\infty} A^j u_{t+1-j}. \tag{4}$$

The unconditional mean of Z_t is $\mu_0 = (I - A)^{-1}\alpha_0$, where I is the six-dimensional identity matrix. If the innovation variance of u_t is V, the unconditional variance of the Z_t process can be derived from equation (4) to be $C(0) = \sum_{j=0}^{\infty} A^j V A^{j\prime}$, since u_t is serially uncorrelated.[9] The jth order autocovariance of Z_t can similarly be derived to be $C(j) = A^j C(0)$.

A. Implied Long-Horizon Statistics

There is considerable academic interest in the characteristics of asset prices and returns at long horizons. For example, Fama and French (1988a) and Poterba and Summers (1988) examine variances and covariances of long-horizon stock returns to determine whether there are mean-reverting components in stock prices. Huizinga (1988) performs analogous computations for real currency depreciations. These authors note that when using short horizon or high frequency data it is often difficult to reject the hypothesis of no serial correlation in the logarithmic changes in asset prices, which are the primary part of an asset's return.[10]

One advantage of the VAR approach is that it uses additional variables that should be able to forecast returns under alternative hypotheses, which can improve the power of tests.[11] Furthermore, if there is long-horizon predictability in asset prices, there must be short-horizon predictability as well, since the long run is just a sequence of short runs. Characterizing long-run predictability can therefore be done with statistics that are functions of the autocovariances of the Z_t process. We consequently employ VAR methods to examine a number of implied long-horizon statistics.

The variance ratio for excess returns is defined to be the ratio of the variance of the sum of k one-period returns to k times the variance of the one-period return. The variance ratio equals one if returns are serially uncorrelated; it is greater than one if returns are positively autocorrelated; and it is less than one if the returns are negatively autocorrelated.

Rather than calculate variance ratios using sample variances of the returns over various horizons k, we calculate an implied variance ratio.[12] To determine an implied variance ratio for U.S. excess returns, first consider the sum of k consecutive Z_t's. From equation (4) the variance of the sum of k Z_t's can be derived to be

$$V_k = kC(0) + (k-1)[C(1) + C(1)'] + \dots + [C(k-1) + C(k-1)']. \quad (5)$$

Define ei to be a six element vector of zeros except for the ith element which is one. Consequently, the total variance of the sum of k consecutive U.S. excess returns is $e1'V_k e1$. The variance ratio for the U.S. excess rate of return is therefore

$$VR(k) = \frac{e1'V_k e1}{k e1'C(0)e1}. \quad (6)$$

The analogous variance ratios for the foreign country excess rate of return and the foreign exchange market excess return substitute e2 and e3, respectively, for e1 in equation (6).

We are also interested in variance ratios for dollar denominated rates of return to U.S. investors in the foreign equity markets and for foreign currency denominated rates of return to foreign investors in the U.S. equity market. As noted above in Section I, these excess rates of returns are just linear combinations of the elements of Z_t, the first uses $e7' = e2' + e3'$ and the second uses $e8' = e1' - e3'$. The final variance ratio we report is for depreciation of the dollar relative to the foreign currency, which is $e3'Z_{t+1} + e6'Z_t$.

Other long-horizon statistics can also be easily calculated. For example, Fama and French (1988b) regress long-horizon equity returns on the current dividend yield. The slope coefficient in such a regression is the covariance of the sum of returns from t+1 to t+k and the dividend yield at t divided by the variance of the dividend yield. Since a covariance involving a sum equals the sum of the covariances of the individual elements, an alternative estimator of this regression coefficient is

$$\beta_1(k) = \frac{e1'[C(1) + \dots + C(k)]e4}{e4'C(0)e4}. \quad (7)$$

Analogous coefficients for regressions of long-horizon foreign equity market returns on the foreign dividend yield are found by substituting e2 for e1 and e5 for e4 in equation (7). We also calculate the implied coefficient in the regression of the long-horizon foreign exchange market excess return on the forward premium. This is found by substituting e3 for e1 and e6 for e4 in equation (7).

Although the R^2's in regressions of one-step-ahead returns on current information are often quite small, the R^2's in long-horizon studies are often quite large, which reflects the negative serial correlation in long horizon returns. The explanatory power of the VAR at long horizons can also be assessed by examining the ratio of the explained variance of the sum of k returns to the total variance of the sum of k returns. These long-horizon R^2 coefficients can be calculated as one minus the ratio of the innovation variance in the sum of k returns to the total variance of the sum of k returns.

The innovation variance of the sum of k consecutive Z_t's can be found from equation (4) to be

$$W_k = \Sigma_{j=1}^{k} (I - A)^{-1}(I - A^{j})V(I - A^{j})'(I - A)^{-1'}. \tag{8}$$

Hence, the implied long-horizon R^2 from the VAR for the U.S. equity return is

$$R^2(k) = 1 - \frac{e1'W_k e1}{e1'V_k e1}. \tag{9}$$

Analogous long-horizon R^2's can be produced for foreign excess equity returns and for the foreign exchange market by appropriate substitution for the indicator vector in equation (9).

B. Asymptotic Distributions for the Statistics

Each of the long-horizon statistics derived above is a function of the parameters of α_0, A, and V. Let η_0 represent the vector of these distinct parameters, and let η_T be an estimate of η_0 from a sample of size T. Estimation of the parameters of the VAR can be thought of as an application of Hansen's (1982) GMM and can be done as a just-identified system. We use 63 orthogonality conditions in a GMM estimation to obtain the asymptotic distribution of η_T. This is a just-identified system because there are 42 coefficients in α_0 and A and 21 distinct parameters in V. The first 42 orthogonality conditions are the usual ordinary least squares conditions that the residuals are orthogonal to the right-hand-side instruments, $E(u_{t+1} \otimes Z_t) = 0$. The last 21 orthogonality conditions are given by stacking the distinct elements of $E(u_{t+1}u_{t+1}' - V) = 0$ into a vector.

In constructing the GMM weighting matrix, we allow a Newey-West (1987) lag of three (the .25 root of the sample size) for all of the orthogonality conditions since the deviations of the cross-products of the residuals from the elements of V can be arbitrarily serially correlated. The asymptotic distribution theory of GMM implies that $\sqrt{T}(\eta_T - \eta_0) \sim N(0, \Omega)$, where $\Omega = (D_0'S_0^{-1}D_0)^{-1}$, D_0 is the expectation of the gradient of the orthogonality conditions with respect to the parameters, and S_0 is the spectral density of the orthogonality conditions evaluated at frequency zero.

Let $H(\eta_0)$ represent the true value of one of the implied long-horizon statistics. The asymptotic distribution of the estimated function can be derived from a Taylor's series approximation to be

$$\sqrt{T}[H(\eta_T) - H(\eta_0)] \sim N(0, \nabla H \Omega \nabla H'). \tag{10}$$

Numerical derivatives can be used to calculate the gradient of H evaluated at η_T, which is denoted ∇H.

C. Interpretation of the Results of the VARs

The estimated VARs are reported in Panels A-C of Table II. The sample period is January 1981 to December 1989 for 108 observations. We use this sample because of the deregulation of international capital markets that took place at the end of the 1970's and the beginning of the 1980's, particularly in the U.K. and Japan.[13]

We first analyze one-step-ahead predictability. A test that any of the excess returns is forecastable is a joint test that the six coefficients on the lagged variables are each zero. If we interpret the results of such tests as classical statisticians, we would reject the null hypothesis of no predictability if the value of the test statistic is greater than the prespecified critical value of a chi-square statistic with six degrees of freedom that is associated with a desired probability of a Type I error. Since we have no idea of the power of these tests, and because Type II errors are also costly, we do not discuss the results in such terms. Instead, we report the confidence values of the test statistics which allows a quasi-Bayesian interpretation. We interpret large values of the test statistics as evidence against the hypothesis of no predictability.

Consider the results for the U.S.-Japan data in Panel A of Table II. For the U.S. equity market the test statistic is 24.245 with a confidence level of .999, for the Japanese equity market the test statistic is 13.955 with a confidence level of .970 and for the dollar-yen foreign exchange market the test statistic is 16.117 with a confidence level of .987. In each case there is some predictability of excess returns, but the returns are quite noisy, and the adjusted R^2's are not large. The lagged variables explain 6.3% of the U.S. excess equity return, 5.2% of the Japanese excess equity return, and 10.9% of the dollar-yen foreign exchange market return.

The Cumby-Huizinga (1990) l-tests generally provide no strong evidence against the hypothesis that the residuals are serially uncorrelated. There is also no strong evidence against the hypothesis that the coefficients on the three lagged returns in each of the equations are zero. These results are in the row labelled Ret. Tests. Nevertheless, there are several coefficients on lagged returns in the return equations that are large relative to their standard errors. The point estimates indicate that expected excess returns in the U.S. and Japan respond positively to lagged U.S. returns and negatively to lagged Japanese returns. The forward premium enters all excess return equations with a negative sign, and the dividend yields enter the equity return equations with positive signs in the own-country equation and negative signs in the cross-country equation.

The U.S.-U.K. data are investigated in Panel B of Table II, and the U.S.-German data are in Panel C. We view the results as qualitatively similar to those of the U.S.-Japan system. The confidence level of the test statistic that examines predictability of the excess return in the U.K. equity market is not as large as those of the U.S. and Japan, but the adjusted R^2 in this equation is comparable to the others, as are the coefficient estimates on the dividend yields and the forward premium. Similarly, the adjusted R^2 for U.S. equity return in the U.S.-Germany VAR falls to zero, but the coefficient estimates on the dividend yields and the forward premium are very similar to the analogous coefficients in the other VARs, and the confidence level for the test of return predictability is .872. There is very strong evidence of predictability of the dollar-pound and dollar-mark excess returns. The confidence levels are never smaller than .999, and the adjusted R^2's are 17.2% and 17.8%, respectively.[14]

Only for the dollar-DM forward premium does the Cumby-Huizinga (1990) l-test indicate strong evidence against the hypothesis that the residuals are serially uncorrelated. In contrast to the U.S.-Japan VAR, the tests for the significance of lagged returns as predictors indicate that past returns are useful for forecasting the dollar-pound and the dollar-DM foreign exchange market returns.

D. Sensitivity Analysis on the VAR

In the VARs reported above we employ the forward premium as a predictor. From equation (2) notice that the forward premium is the nominal interest rate differential between the U.S. and the other country. Fama and Schwert (1977) used the nominal interest rate to predict equity returns and found a negative coefficient. Here, we examine whether the VAR would be better specified if the two nominal interest rates are entered separately rather than being forced to enter with coefficients that are equal and opposite in sign.

If the true values of the coefficients are equal and opposite in sign, failure to impose a true constraint in a finite sample unnecessarily reduces degrees of freedom and lowers the power of tests. Even if the true values are different, the principle of parsimony (especially in a VAR) dictates imposition of a false constraint if the absolute values are not too different.

A second issue is the presence of persistence in the variables of the VAR. It is often argued that nominal interest rates are integrated processes (see King, Plosser, Stock and Watson (1991)). From Table I it is clear that dividend yields are also highly persistent. If two interest rates are included with the two dividend yields, too many variables with near unit roots may be present in the VAR, which might negate the validity of the usual asymptotic distribution theory that we use to generate standard errors and test statistics.

We address these issues in Table III. Panels A-C report three sets of tests for the three VARs. Since our primary focus is return predictability, we discuss the evidence for these equations. The first columns report coefficient estimates on the nominal interest rates for each of the three excess returns. The coefficient estimates for the U.S. interest rate are always negative, and the coefficients on the other country interest rate are always positive. The $\chi^2(1)$ statistics test the constraints that the coefficients are equal and opposite in sign. In the U.S.-Japan system there is no evidence against this constraint. In the other two-country systems, only in the U.S. equity market equation is the test statistic sufficiently large to reject the restriction at the 5% level. The next columns report the $\chi^2(7)$ statistics testing overall predictability of returns and the adjusted R^2 statistics. The values of these statistics are not very different from their respective values in Table II. These statistics are all calculated under the assumption that interest rates are stationary.

In order to address the issue of highly persistent variables in the VAR, the last four columns of Table III report a χ^2 statistic and an adjusted R^2 for two VARs in which the four highly persistent variables enter in a quasi-differenced form. For dividend yields we subtract a moving average of the past twenty-four months from the current dividend yield variable in both specifications. For nominal interest rates we enter the interest differential in both specifications and one quasi-differenced interest rate obtained by subtracting 0.9 times the previous interest rate from the current interest rate. Unless the results on predictability of returns that are reported above, are due to spurious predictability, the quasi-differenced variables should continue to explain returns although perhaps not with the same explanatory power.

The results are qualitatively quite similar to the specifications reported in levels for the U.S.-Japan and U.S.-U.K. systems. For the U.S.-German system, there is a decline in the statistical significance in all three equations and a substantial reduction in the R^2 of the excess foreign exchange market return.

Given this evidence, we think that the original specification of the VAR is superior to the alternatives. Hence, the next section investigates long-horizon statistics calculated from the VARs of Table II.

E. Estimated Long-Horizon Statistics from the VAR

Tables IV, V and VI report estimates of the implied long-horizon statistics derived in Section II.A with their associated asymptotic standard errors for the VARs of the U.S.-Japan, the U.S.-U.K. and the U.S.-Germany, respectively. Panel A of each table reports the implied unconditional means, standard deviations and correlations of the series; Panel B reports several slope coefficients from implied OLS regressions; Panel C reports implied variance ratios; and Panel D reports implied R^2's.

The results for Panel A are very similar across the three sets of countries. The point estimates of the unconditional mean excess returns implied by the VARs are similar in magnitude to the unconditional means calculated directly, but their standard errors are very large.[15] The volatilities of the equity returns are larger than those of the foreign exchange market returns (between 50% and 70% for equities and between 40% and 50% for foreign exchange), and the correlations of the foreign exchange market returns with the equity returns are less than ±14% and are insignificantly different from zero.[16]

The dollar forward premiums on the foreign currencies are always negatively correlated with all excess returns. Dividend yields are almost always negatively correlated with all excess returns, and, unsurprisingly, the statistical significance of the correlation of dividend yields with returns is concentrated primarily, but not exclusively, in the own-country equity market. Dividend yields are highly positively correlated across countries (at least 78% in all cases), and they are always positively correlated with the forward premiums.

Each Panel B of Tables IV-VI reports implied slope coefficients, calculated analogously to equation (7), for the three sets of regressions. In the first two cases the own-country excess equity return compounded over various horizons is implicitly regressed on the own-country dividend yield. In the third case, the compound excess foreign exchange return is implicitly regressed on the forward premium. Unfortunately, the large standard errors imply that the statistical significance of the estimates of the implied dividend yield coefficients is generally not as strong as that found in Hodrick (1991).[17] The point estimates reported here are approximately the same size or slightly smaller than their standard errors for the U.S., the U.K. and Germany, and they are generally smaller than their standard errors for Japan.

Interpretation of the point estimates from these implied regressions is facilitated by dividing by the time horizon. The resulting coefficient is the increase in an annualized expected excess return for a 100 basis point increase in a dividend yield. For example, the estimates imply that a 1% increase in the own country dividend yield forecasts an increase in expected returns over the next 48 months of 2% per annum for the U.S., 3% p.a. for Japan, 3.5% p.a. for Germany, and 4% p.a. for the U.K.. These results are comparable to those of Fama and French (1988b) whose coefficient estimates imply that U.S. real returns increase by 4% p.a. over 48 months when the U.S. dividend yield increases by 1%.

The last sets of implied coefficients in Panel B of Tables IV-VI are from the implicit regressions of long-horizon excess foreign exchange returns on the own-market forward premiums. These coefficients are quite significantly different from zero. The coefficients at the one, three, six, and twelve month horizon are two to five times their standard errors. To interpret these coefficients, remember that the exchange rates are expressed as dollars per foreign currency and the excess rates of return are for uncovered investments in the foreign currency money markets in excess of the U.S. interest rate.

The coefficients at the one month horizon imply that a one percentage point increase in the forward premium is associated with a 6% p.a. decrease in the expected excess rate of return to investing in yen or pounds and an 8% p.a. decrease to investing in deutschemarks. At the twelve month horizon, the coefficients imply that a one percentage point increase in the forward premium is associated with a 4% p.a. decrease in the compound expected excess return from investing in the yen money market. Similar coefficients are found for the other currencies as well.

Each Panel C of Tables IV-VI reports the implied long-horizon variance ratios. For the U.S. and the U.K. the point estimates indicate mean reversion in stock prices at long horizons, with the U.S. evidence being the strongest in the U.S.-Japan VAR. The 48 and 60 month variance ratios fall to 0.50 or 0.60, which is consistent with the results of Poterba and Summers (1988) and Hodrick (1991). There is no evidence of mean reversion in Japanese or German excess returns. There is slight evidence that German excess equity returns are positively correlated at short horizons since the variance ratios rise to 1.2 at six months. For the excess returns in the foreign exchange market the point estimates indicate that returns are highly positively serially correlated. The variance ratios increase monotonically to above 2.9 for all currencies.

Each Panel D of Tables IV-VI reports the implied long-horizon R^2's for the three excess returns. The U.S., Japanese and German excess returns show some predictability at long horizons, but the ratio of explained variance to total variance never rises above 15.1% for these countries. In contrast, the implied R^2 at the 60 month horizon for the U.K. is 31%. The excess returns in the foreign exchange market are more predictable. At the twelve month horizon the implied R^2's are 26% for the yen, 40% for the pound, and 30% for the mark.

III. Latent Variable Models

This section examines several latent variable models that are constrained counterparts of the equations for the excess returns of the VARs. As in Hansen and Hodrick (1983), we note that these models are not tests of a particular equilibrium theory of international asset pricing.[18] Rather, they are best interpreted as empirical investigations of parsimonious characterizations of the expected excess returns. If Θ is the (N by M) matrix of reduced form coefficients for N excess returns regressed on M explanatory variables, the K dimensional latent variable model is the restriction that the rank of Θ is K. Campbell and Hamao (1990) report latent variable models for the U.S. and Japanese equity markets with returns denominated in dollars and yen. We include the dollar-yen money market as well.

Table VII reports models with a single latent variable for each of the three country pairs, U.S.-Japan in Panel A, U.S.-U.K. in Panel B and U.S.-Germany in Panel C. In each case, the three excess returns are the U.S. equity return, the foreign country equity return, and the relevant foreign exchange market return. In the VAR there are seven forecasting variables including a constant in each equation. Hence, there are twenty-one free coefficients in the three excess return equations. The single latent variable model constrains the explanatory power of the seven variables to be proportional across the three excess returns.

For example, with Z_t augmented to include a constant, the U.S.-Japan system is

$$r_{1t+1} = \alpha' Z_t + \varepsilon_{1t+1} \tag{11}$$

$$r_{2t+1} = \beta_1 \alpha' Z_t + \varepsilon_{2t+1} \tag{12}$$

$$rs_{2t+1} = \beta_2 \alpha' Z_t + \varepsilon_{3t+1} \tag{13}$$

which results in nine free parameters or twelve constraints on the VAR coefficients. The nonlinear system of three equations is estimated with GMM using the 21 orthogonality conditions $E_t(\varepsilon_{it+1}Z_t) = 0$, for i = 1-3. Table VII reports the estimated β's as well as the constrained reduced form coefficients.

Models with two latent variables are reported in Table VIII. These may be written as

$$r_{1t+1} = \alpha_1' Z_t + \varepsilon_{1t+1} \tag{14}$$

$$r_{2t+1} = \alpha_2' Z_t + \varepsilon_{2t+1} \tag{15}$$

$$rs_{2t+1} = (\beta_1 \alpha_1' + \beta_2 \alpha_2') Z_t + \varepsilon_{3t+1} \tag{16}$$

which allows sixteen free parameters with twenty-one orthogonality conditions. We report several chi-square statistics that examine the adequacy of the models. If the models are good representations of the data, the chi-square statistics that test the overidentifying restrictions should be small. On the other hand, since there is evidence that each of the excess returns is forecastable in the unconstrained systems, the chi-square statistics for a particular equation that test the explanatory power of the constrained variables ought to be large.

For the U.S.-Japan system, a confidence level of .941 for the test of the overidentifying restrictions indicates evidence against the single latent variable model that is about as strong as the evidence in Campbell and Hamao (1990), who examine just the two excess equity returns. Hence, adding the foreign exchange market with its strong predictability did not strengthen the evidence against the model. Examination of the reduced form coefficients in Table II suggests one reason why the model is inconsistent with the data. In the unconstrained VAR, the own dividend yield enters the own country equity return equation with a positive coefficient and the foreign country excess return equation with a negative coefficient. Since the single latent variable model constrains all of the coefficients of a particular forecasting variable to be the same sign across equations, it clearly cannot fit the data.

In the models with two latent variables in Table VIII, there is essentially the same evidence against the constrained U.S.-Japan system as found above, even though there are now only five constraints. The confidence level of the overall test is .92. The constrained reduced form coefficients now fit the pattern of the unconstrained system described above, but the explanatory power of the variables in the foreign exchange market equation is not as statistically significant as in the unconstrained system.

For the U.S.-U.K. single latent variable system, the dollar-pound foreign exchange market excess return is not well explained. In the constrained model, the beta for the foreign exchange market is essentially zero. The substantive evidence against the model as evidenced by the confidence level of the overall test statistic of .988 appears to be driven by feedback effects from lagged returns to current returns present in the unconstrained model that cannot be captured in the constrained case.

The model with two latent variables for the U.S.-U.K. system works very well. The value of the chi-square statistic that tests the overidentifying restrictions is less than its mean. Notice that if equations (14) and (15) were estimated as unconstrained equations, β_1 and β_2 in equation (16) would measure the influence of predictable components of the U.S. and U.K. equity returns on the predictable part of the foreign exchange return. Because estimation of the system is done in a constrained way, this interpretation is not literally valid, but the positive β_1 and negative β_2 do suggest the following interpretation. Market forces that increase the U.S. equity risk premium also increase the risk premium on uncovered pound money market investments, and market forces that increase the U.K. equity risk premium also increase the risk premium on uncovered dollar money market investments made with pounds. The statistical significance of the betas suggests that the former effect is more important than the latter.

For the U.S.-German data, the model with two latent variables also works better than the single latent variable model. In the unconstrained VAR there is strong positive feedback from U.S. equity returns to German equity returns but negative feedback from U.S. equity returns to the excess return in the foreign exchange market. This forces the betas in the single latent variable model to have opposite signs and causes the coefficient on the forward premium, which is negative in the unconstrained foreign exchange market equation to be positive in the constrained case. The model with two latent variables works quite well. The test statistics of the overidentifying restrictions has a confidence level of .62, and the joint statistical significance of the constrained reduced form coefficients is almost as large as in the unconstrained systems. The estimates of β_1 and β_2 are positive and negative, respectively, although neither is precisely estimated.

A. A Three-Country System

The results of two three-country latent variable models are reported in Table IX (one latent variable in Panel A and two latent variables in Panel B). We include the excess returns of the U.S., Japan, and the U.K. for a five equation system, and we use a constant, the three dividend yields and the two forward premiums as instruments. Hence, there are thirty orthogonality conditions with ten parameters in the single latent variable model and eighteen parameters in the two latent variables model.[19]

There is evidence against the two models, since the confidence levels for the overall test statistics are .980 and .893. Nevertheless, in the two latent variable model there is also strong evidence of statistically significant forecasting power for all excess returns but the U.K. equity market. Examination of the significance of the individual coefficients in the constrained reduced form in Panel B reveals an interesting pattern, which should also be interpreted with care given the high correlation of the instruments. The forward premiums almost always have negative signs in all equations and are important in forecasting the U.S. equity return and the two foreign exchange returns. The U.S. dividend yield has an important negative influence on the Japanese and the U.K. equity returns but is insignificant in the U.S. equity equation. The Japanese dividend yield enters all equations positively and is most important in the Japanese and U.K. equity equations.

IV. Hansen-Jagannathan (1991) Bounds

The linear predictability of equity and foreign exchange returns across several countries documented above is not necessarily inconsistent with equilibrium asset pricing models although there is currently no equilibrium model which is consistent with it. One way to determine the implications of this predictability for a rich class of dynamic models is to investigate volatility bounds on investors' intertemporal marginal rates of substitution (IMRS) as pioneered by Hansen and Jagannathan (1991).

In models of rational maximizing behavior, investment decisions are dictated by intertemporal Euler equations that relate the loss in marginal utility from sacrificing a dollar at time t in purchasing an asset to the expected gain in marginal utility from holding the asset and selling it at time t+1. Let Q_{t+1} be the intertemporal marginal rate of substitution of a dollar between period t and t+1, and let R_{t+1} to be a return at t+1 on a dollar invested at t. The typical Euler equation is

$$E_t(Q_{t+1}R_{t+1}) = 1. \tag{17}$$

Equation (17) is the foundation of many theoretical and empirical investigations of asset pricing. In the most basic representative agent model, e.g. Lucas (1982), the IMRS is

$$Q_{t+1} = \beta U'(C_{t+1})\pi_{t+1}/U'(C_t)\pi_t, \tag{18}$$

which is the agent's discount factor times the ratio of the marginal utility of consumption at time t+1 multiplied by the purchasing power of a dollar at time t+1 to the product of these variables at time t.

Hansen and Jagannathan (1991) use data on returns to compute bounds on the variability of an agent's real IMRS that any model implying an Euler equation like (17) must satisfy. Whereas Hansen and Jagannathan (1991) investigate real returns using only U.S. dollar assets, we consider the nominal IMRS and use dollar returns on domestic and international investments to see if this makes the bounds more restrictive.

Bounds on the variability of Q_{t+1} using excess returns are derived as follows. Let x_{t+1} denote a vector of n excess returns, which are dollar payoffs that have zero prices. From equation (17) we know that $E_t(x_{t+1}Q_{t+1}) = 0$. Let P denote the space spanned by x_{t+1}, and let P^a be the space P augmented with a unit payoff. Although Q_{t+1} is not observable, a linear projection of Q_{t+1} onto P^a would be $\alpha + \beta' x_{t+1}$. Let the unconditional covariance matrix of x_{t+1} be Σ. Then, the projection coefficient is $\beta = \Sigma^{-1}[E(x_{t+1}Q_{t+1}) - E(x_{t+1})E(Q_{t+1})] = -\Sigma^{-1}E(x_{t+1})E(Q_{t+1})$. Because there will typically be a projection error, the variance of the nominal IMRS, the dependent variable in the regression, must be greater than $\beta'\Sigma\beta$, the variance of the explained part of Q_{t+1}. By substituting for β, it is straightforward to derive a bound on the variance of Q_{t+1}:

$$\sigma^2(Q_{t+1}) > [E(Q_{t+1})]^2 E(x_{t+1})' \Sigma^{-1} E(x_{t+1}) \tag{19}$$

Since $E(Q_{t+1})$ is unobservable, we obtain a bound on the coefficient of variation of the nominal IMRS implied by the mean and the variance of excess dollar returns:

$$\frac{\sigma(Q_{t+1})}{E(Q_{t+1})} > (E(x_{t+1})' \Sigma^{-1} E(x_{t+1}))^{1/2} \tag{20}$$

Notice that if only one excess return is used, the bound is immediately given by rewriting equation (17) as $cov(Q_{t+1}, x_{t+1}) + E(Q_{t+1})E(x_{t+1}) = 0$ and using the Cauchy-Schwarz inequality. The bound then restricts the coefficient of variation of the nominal IMRS to be greater than or equal to the Sharpe ratio of the excess return, i.e. $|E(x_{t+1})|/\sigma(x_{t+1})$. Some calculations of bounds implied by a model such as equation (18) are provided below after we discuss the estimation of the bounds.

Table X estimates a variety of volatility bounds for the dollar IMRS calculated from our dollar denominated domestic and foreign excess returns. The column labelled (unscaled) contains bounds derived using only the raw excess returns listed in the first column. The bounds estimated only with foreign exchange investments are not very demanding (never larger than 0.07), nor are they precisely estimated. The volatility bounds implied by all the equity market investments is 0.237. Using all of the foreign exchange returns with all of the equity market returns increases the bound to 0.331, which is not much larger than the bound implied by considering the Japanese foreign exchange and equity returns with the U.S. excess equity return.

Hansen and Jagannathan (1991) note that the payoff space can be increased by considering returns that are scaled by elements in the agents' information set. Essentially, scaling a return is the same as investing a different amount in an asset based on the realization of a random variable as in a trading rule. The empirical results from this paper suggest that incorporating conditioning information should be important because the returns are forecastable.[20]

The column of Table X labelled (scaled) reports bounds generated from the original unscaled excess returns and the scaled excess returns. The scaling factors are the own dividend yields for equity returns and the own forward premiums for the foreign exchange returns. The column labelled (cross-scaled) adds additional pseudo returns constructed by scaling the equity returns with the dollar-yen forward premium and the foreign exchange returns with the U.S. dividend yield.

For the scaled bounds, except for Germany, the use of dividend yields tends not to increase the volatility bounds, while the effect of using the forward premiums with the foreign exchange returns is dramatic. Whenever a foreign exchange return that is scaled by its forward premium is included in the analysis, the bound invariably exceeds 0.30 with a standard error less than 0.10. The volatility bound implied by all of our excess returns including the scaled ones is 0.641 with a standard error of 0.088.

Cross-scaling the equity returns with the dollar-yen forward premium tends to increase the volatility bounds quite substantially, but the effect of scaling the foreign exchange returns with the U.S. dividend yield is minimal. The volatility bound implied by all assets rises to 0.776 with a standard error of 0.083.

These bounds can be compared to some benchmarks provided in Bekaert (1991) who simulates a two country, general equilibrium model of the Lucas (1982) variety using an estimated VAR of money and consumption growth rates to provide realistic exogenous processes.[21] Utility is parameterized with standard constant relative risk aversion (CRRA) preferences, and equation (18) applies with consumption measured as a geometric average of foreign and home goods. With equal weights on the two goods and a risk aversion coefficient of 2, the coefficient of variation of Q_{t+1} is of the order 0.010. To obtain bounds on the coefficient of variation of Q_{t+1} of around 0.2, the CRRA coefficient must be increased to over 40. Obtaining a bound of 0.78 requires a CRRA coefficient over 140.

Hansen and Jagannathan (1991) report bounds that are less restrictive than the ones we report, except when they examine returns from the U.S. Treasury bill market. They argue that such restrictive bounds may be incorrectly estimated since Treasury bills may provide liquidity services to investors who hold them to maturity as cash substitutes. While this argument may apply to money market investments, we find bounds that are equally restrictive using only equity returns. The bound from the four equity returns, including the scaled and cross-scaled pseudo returns, is 0.585 with a standard error of 0.080.

V. Conclusions

In this paper we characterize the linear predictability of excess returns in major equity and foreign exchange markets. Variables such as dividend yields, that were known to predict excess equity returns, are demonstrated to have predictive power for excess returns in the foreign exchange market. Similarly, variables such as forward premiums, that were known to predict excess returns in the foreign exchange market, are demonstrated to have predictive power for excess equity returns. We establish these results in vector autoregressions that allow calculation of a variety of long-horizon statistics. This evidence has direct implications for the practice of international asset allocation.

We find evidence of long-horizon mean reversion in stock prices in the U.S. and the U.K., but not for Japan or Germany. The excess returns in the foreign exchange market are characterized by strong persistence. This implies, for example, that a U.S. investor faces mean reversion in the U.S. equity market but not in the dollar-denominated Japanese equity market, and from the Japanese perspective, there is no evidence of mean reversion on the yen-denominated return on the U.S. equity market.

We investigate the implications of a change in the dividend yield for long-horizon equity returns finding that a one per cent increase in dividend yields implies between a two and four per cent per annum increase in expected returns over the next forty-eight months. Increases in the forward premium on foreign currencies imply large decreases in excess returns in the foreign exchange market that are quite significant at shorter horizons. The forecasting power of the forward premium (that appears so puzzling to some researchers in the foreign exchange market) is also present in the equity excess returns. Increases in the forward premium (dollars/foreign currency) forecast lower expected excess equity returns in all countries.[22] Latent variable models, which are constrained counterparts to the VAR analysis, only capture the covariance structure of excess returns if models with two latent variables are estimated.

Our final results demonstrate that bounds on the nominal dollar IMRS derived from considering U.S. investments jointly with foreign money and stock market investments with appropriate conditioning information are considerably higher than those obtained when attention is restricted only to the U.S. excess equity return. Whether the predictability in returns and the derived volatility bounds represent evidence of highly variable risk premiums, regime switching, peso problems, learning about policy changes, or market inefficiencies remains an open question.

Footnotes

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1. For U.S. data, Fama and Schwert (1977) used nominal interest rates to predict stock returns. For recent uses of this instrument see Breen, Glosten and Jagannathan (1989) and Ferson (1989). Dividend yields have been used as predictors of stock returns either alone or in conjunction with other instruments by Rozeff (1984), Shiller (1984), Keim and Stambaugh (1986), Fama and French (1988b), Campbell and Shiller (1988), Campbell (1991), Cochrane (1990) and Hodrick (1991), among others. Gultekin (1983) and Solnik (1983) extended the Fama and Schwert results to other countries.

2. See Hodrick (1987) for a survey of the empirical literature in this area. More recent contributions include Cumby (1988), Kaminsky and Peruga (1990), Mark (1988), and Froot and Thaler (1990). Tryon (1979) and Bilson (1981) pioneered use of the forward premium in investigations of the efficiency of the foreign exchange market.

3. Related papers include Giovannini and Jorion (1987, 1989), who examine models of risk premiums in several foreign exchange markets simultaneously with the risk premium in the U.S. stock market; Campbell and Hamao (1989), who examine excess equity returns in the U. S. and Japan; Cumby (1990), who examines real equity returns in the U.S., Germany, the U.K., and Japan; and Harvey (1991), who examines dollar denominated excess equity returns on seventeen countries.

4. Recent studies on international asset allocation include Jorion (1989), Hardy (1990) and Solnik (1990).

5. Hansen and Hodrick (1983) developed the latent variable model and applied it to the foreign exchange market. Gibbons and Ferson (1985) developed the model independently in an application to the stock market. In recent applications of the approach, Cumby (1990) and Campbell and Hamao (1989) examine integration of equity markets across countries.

6. A focus on excess rates of return arises naturally in theoretical frameworks if returns are lognormally distributed. Use of gross excess returns in our empirical work would not change inference about return predictability, but it would complicate many of our calculations since they would no longer be linear.

7. We thank Bob Korajczyk for the eurocurrency interest rate data which were obtained at INSEAD and are used in Korajczyk and Viallet (1991).

8. The reported standard deviations are not estimates of the standard deviation of the annual holding period return. If returns are i.i.d., the variance of the annual return is twelve times the variance of the one month return. To estimate the standard deviation of the annual holding period return, divide our reported numbers by $\sqrt{12} = 3.464$.

9. In actual calculations we truncate the infinite sum in C(0) at 255.

10. Poterba and Summers (1988) perform Monte Carlo experiments to examine the power of autocorrelation based tests. In the presence of highly serially correlated transitory components in prices, autocorrelation based tests have very low power. For example, such tests often incorrectly fail to reject the null hypothesis of no serial correlation in the changes in prices with probabilities of at least .8 when as much as 75% of the unconditional variance of the change in prices is due to transitory components.

11. Kandel and Stambaugh (1988) and Campbell (1991) employ VAR methods to examine long-horizon equity returns, and Cumby and Huizinga (1990) employ the technique to examine long-horizon forecasts of real exchange rates. Hodrick (1991) reports Monte Carlo analyses of the VAR technique and finds that the asymptotic distribution theory works very well given that the order of the VAR is correct.

12. See Cochrane (1988), Lo and MacKinlay (1988) and Poterba and Summers (1988) for discussion of variance ratios.

13. The sample corresponds to a sub-sample of Campbell and Hamao (1989) who describe the deregulation of Japanese financial markets.

14. Harvey (1991) reports a higher R^2 for the U.S. equity return, but he includes a term structure premium and a default premium. His R^2's for other countries are approximately the same as ours even though his are denominated in dollars and ours are denominated in foreign currency. The R^2's for dollar denominated returns on foreign equity investments using our data and our predictive variables are 12.6%, 13.0%, and 7.8% for Japan, the U.K., and Germany, respectively.

15. The large standard errors reflect imprecise estimation of the constant terms in the regressions and the near non-stationarity of the VAR caused by the inclusion of the highly serially correlated dividend yields and forward premiums.

16. This latter observation forms the basis of recent interest in hedged foreign investment strategies in which the principal on a long term foreign equity or bond investment is sold in the short-term forward market.

17. Hodrick (1991) uses the three variable VAR of Campbell (1991) composed of real returns, dividend yields and the short term treasury bill rate relative to its one year moving average. For a sample of

monthly data from 1952 to 1987, the coefficients from the implied OLS regression of returns on dividend yields for comparable horizons to those of Tables 3-5 are often five to eight times their standard errors. Presumably, both the larger number of variables in the VAR (six vs. three) and the smaller sample size (108 vs. 431 observations) of this paper conspire to increase the standard errors here.

18. See Wheatley (1989) for a critique of the latent variable approach to testing asset pricing models.

19. We did not use the two German returns because we considered estimation of a model with seven returns using all dividend yields and all forward premiums as instruments in all equations to be inappropriate given our sample size.

20. Gallant, Hansen, and Tauchen (1990) discuss efficient use of conditioning information using seminonparametric methods.

21. The consumption data are quarterly non-durables and services for the U.S. and Japan obtained from the OECD, and the money stocks are measures of M2 from International Financial Statistics.

22. See Froot (1990) for a recent investigation of short-term nominal interest rates as predictors of returns on a variety of assets. Froot argues that risk premiums cannot be the source of the predictive power because the nominal interest rates have similar predictive power for the forecast errors from surveys of expected returns.

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Table I

Summary Statistics

The numerical subscripts denote countries: 1 for the U.S., 2 for Japan, 3 for the U.K. and 4 for Germany. The excess equity market rate of return in country j is r_{jt}, the foreign exchange market return between country j and the U.S. is rs_{jt}, the dividend yield in country j is dy_{jt}, the forward premium on currency j in terms of U.S. dollars is fp_{jt}, and the interest rate on currency j is i_{jt}. The sample period is 1981:1 to 1989:12. The standard error for the autocorrelations is 0.096.

Variable	Mean	Standard Dev.	Autocorrelations			
			ρ_1	ρ_2	ρ_3	ρ_4
r_{1t}	4.969	56.937	.081	-.048	-.061	-.048
r_{2t}	15.420	57.003	.016	-.057	-.036	-.010
r_{3t}	8.744	68.276	-.094	-.082	-.041	.040
r_{4t}	10.188	71.246	.125	-.001	.041	-.006
rs_{2t}	-0.894	42.251	.128	.051	.172	-.024
rs_{3t}	-3.620	45.884	.021	.165	.041	.070
rs_{4t}	-2.740	43.644	.059	.133	.086	.039
dy_{1t}	4.346	0.934	.964	.932	.901	.864
dy_{2t}	1.070	0.508	.970	.938	.912	.894
dy_{3t}	4.434	1.148	.949	.909	.876	.846
dy_{4t}	3.887	1.054	.922	.879	.823	.787
fp_{2t}	4.166	2.629	.897	.833	.758	.694
fp_{3t}	-1.438	2.877	.877	.780	.668	.559
fp_{4t}	3.630	1.622	.620	.456	.353	.226
i_{1t}	9.683	3.167	.935	.878	.835	.756
i_{2t}	5.785	1.195	.900	.829	.794	.731
i_{3t}	11.320	2.023	.893	.791	.688	.597
i_{4t}	6.176	2.496	.945	.886	.840	.792

Table II

First Order Vector Autoregressions of Excess Stock Returns, the Excess Foreign Exchange Return, Dividend Yields, and the Forward Premium

Heteroskedasticity consistent standard errors (s.e.) and associated confidence levels for the test that the coefficient is zero are below the estimates. The $\chi^2(6)$ statistic tests the joint hypothesis that the six lagged variables have no predictive power. The appropriate lag length for the VAR minimizes the Schwarz (1978) criterion. The Cumby-Huizinga (1990) l-test for serial correlation of the residuals is robust to conditional heteroskedasticity and lagged dependent variables. We test five correlation coefficients. The Ret. tests examine the joint hypothesis that the lagged returns have zero coefficients in the forecasting equations.

Dep. Var.	Coefficients on Regressors: Con. (s.e.) Conf.	r_{1t} (s.e.) Conf.	r_{2t} (s.e.) Conf.	rs_{2t} (s.e.) Conf.	dy_{1t} (s.e.) Conf.	dy_{2t} (s.e.) Conf.	fp_{2t} (s.e.) Conf.	$\chi^2(6)$ Conf.	R^2
Panel A: U.S. - Japan, 1981:1 to 1989:12, 108 Observations									
	-60.951	0.134	-0.150	-0.021	31.169	-35.619	-6.969	24.245	
r_{1t+1}	(54.118)	(0.124)	(0.087)	(0.121)	(17.462)	(21.215)	(2.368)	.999	.063
	.740	.720	.916	.138	.926	.907	.997		
	92.581	0.189	-0.116	0.053	-28.596	49.016	-1.083	13.955	
r_{2t+1}	(40.256)	(0.109)	(0.095)	(0.141)	(13.760)	(19.641)	(2.429)	.970	.052
	.979	.916	.777	.295	.962	.987	.344		
	60.259	-0.105	0.084	-0.044	-16.714	31.461	-5.475	16.117	
rs_{2t+1}	(26.046)	(0.089)	(0.069)	(0.089)	(9.436)	(15.644)	(1.971)	.987	.109
	.979	.762	.778	.382	.923	.956	.995		
	0.348	-0.0003	0.0006	0.0002	0.846	0.153	0.032	2025.7	
dy_{1t+1}	(0.198)	(0.0005)	(0.0003)	(0.0005)	(0.066)	(0.080)	(0.010)	.999	.950
	.920	.461	.928	.361	.999	.945	.999		
	-0.102	-0.0001	0.0001	0.0002	0.036	0.916	0.004	11807.	
dy_{2t+1}	(0.034)	(0.0001)	(0.0001)	(0.0001)	(0.013)	(0.023)	(0.003)	.999	.989
	.997	.782	.599	.759	.993	.999	.883		
	0.473	0.0008	0.002	-0.001	-0.076	0.190	0.891	380.21	
fp_{2t+1}	(0.852)	(0.002)	(0.002)	(0.003)	(0.327)	(0.475)	(0.058)	.999	.853
	.421	.344	.681	.382	.183	.311	.999		

l-tests	Eq. 1	Eq. 2	Eq. 3	Eq. 4	Eq. 5	Eq. 6	Schwarz Criteria
$\chi^2(5)$	3.585	3.500	7.132	10.289	4.106	6.372	
Conf.	.389	.377	.789	.933	.466	.728	1. 12.228
Ret. tests							2. 13.249
$\chi^2(3)$	4.700	3.120	2.159	4.479	4.517	2.562	3. 14.275
Conf.	.805	.627	.460	.786	.789	.536	4. 15.270

Panel B: U.S. - U.K., 1981:1 to 1989:12, 108 Observations

Dep. Var.	Con. (s.e.) Conf.	r_{1t} (s.e.) Conf.	r_{3t} (s.e.) Conf.	rs_{3t} (s.e.) Conf.	dy_{1t} (s.e.) Conf.	dy_{3t} (s.e.) Conf.	fp_{3t} (s.e.) Conf.	$\chi^2(6)$ Conf.	R^2
	Coefficients on Regressors								
	-79.838	0.129	-0.079	-0.159	27.548	-10.177	-7.222	18.674	
r_{1t+1}	(48.878)	(0.155)	(0.129)	(0.095)	(17.504)	(12.958)	(2.242)	.995	.041
	.898	.593	.462	.904	.884	.568	.999		
	-82.236	0.408	-0.317	0.013	12.740	6.623	-4.983	6.754	
r_{3t+1}	(49.914)	(0.205)	(0.165)	(0.125)	(14.510)	(13.274)	(2.643)	.656	.064
	.901	.954	.946	.082	.620	.382	.941		
	-23.497	-0.116	-0.039	-0.148	4.115	-1.928	-8.153	28.196	
rs_{3t+1}	(27.937)	(0.097)	(0.075)	(0.106)	(12.106)	(9.372)	(2.475)	.999	.172
	.600	.769	.399	.839	.266	.163	.999		
	0.449	-0.0003	0.0003	0.0006	0.843	0.059	0.032	2136.8	
dy_{1t+1}	(0.193)	(0.0006)	(0.0005)	(0.0004)	(0.086)	(0.057)	(0.009)	.999	.949
	.980	.419	.525	.874	.999	.695	.999		
	0.331	-0.0013	0.0011	0.0002	0.057	0.872	0.027	2030.6	
dy_{3t+1}	(0.167)	(0.0008)	(0.0006)	(0.0005)	(0.096)	(0.079)	(0.012)	.999	.943
	.953	.904	.919	.376	.447	.999	.979		
	-1.392	-0.0010	-.0005	0.002	0.443	-0.191	0.843	268.98	
fp_{3t+1}	(0.862)	(0.0034)	(0.0030)	(0.002)	(0.387)	(0.277)	(0.072)	.999	.814
	.894	.221	.126	.719	.748	.510	.999		

l-tests	Eq. 1	Eq. 2	Eq. 3	Eq. 4	Eq. 5	Eq. 6	Schwarz
$\chi^2(5)$	6.124	2.478	9.432	7.122	3.303	6.184	Criteria
Conf.	.706	.220	.907	.788	.347	.711	1. 16.256
Ret. tests							2. 17.149
$\chi^2(3)$	2.890	4.839	7.981	2.876	3.527	2.088	3. 18.427
Conf.	.591	.816	.954	.589	.683	.446	4. 19.481

Panel C: U.S. - Germany, 1981:1 to 1989:12, 108 Observations

Dep. Var.	Con. (s.e.) Conf.	r_{1t} (s.e.) Conf.	r_{4t} (s.e.) Conf.	rs_{4t} (s.e.) Conf.	dy_{1t} (s.e.) Conf.	dy_{4t} (s.e.) Conf.	fp_{4t} (s.e.) Conf.	$\chi^2(6)$ Conf.	R^2
	Coefficients on Regressors								
r_{1t+1}	-7.701 (34.356) .177	0.123 (0.105) .759	-0.080 (0.079) .690	0.019 (0.109) .139	17.664 (12.257) .850	-11.581 (7.290) .888	-5.039 (3.704) .826	9.932 .872	-.003
r_{4t+1}	-7.143 (35.178) .161	0.264 (0.160) .901	-0.011 (0.119) .076	-0.296 (0.167) .924	13.423 (12.396) .721	-2.135 (8.974) .188	-9.389 (3.830) .986	13.595 .965	.052
rs_{4t+1}	54.392 (17.969) .998	-0.203 (0.069) .997	-0.001 (0.049) .024	-0.137 (0.101) .826	6.296 (6.202) .690	-11.929 (5.555) .968	-10.073 (2.193) .999	38.915. 999	.178
dy_{1t+1}	0.121 (0.131) .643	-0.0003 (0.0004) .584	0.0004 (0.0003) .773	-0.0002 (0.0004) .361	0.908 (0.045) .999	0.048 (0.028) .913	0.021 (0.015) .827	1488.4 .999	.945
dy_{4t+1}	0.089 (0.145) .464	-0.0007 (0.0006) .820	0.0004 (0.0005) .495	0.0011 (0.0007) .900	0.041 (0.046) .626	0.889 (0.070) .999	0.039 (0.031) .789	935.36 .999	.902
fp_{4t+1}	0.232 (0.497) .360	-0.0013 (0.0019) .491	0.0016 (0.0014) .725	-0.0014 (0.0032) .342	0.264 (0.259) .692	0.034 (0.213) .128	0.564 (0.121) .999	90.125 .999	.493

I-tests	Eq. 1	Eq. 2	Eq. 3	Eq. 4	Eq. 5	Eq. 6	Schwarz
$\chi^2(5)$	5.469	0.689	4.279	7.557	10.410	15.981	Criterion
Conf.	.639	.016	.490	.818	.936	.993	1. 17.574
Ret. tests							2. 18.482
$\chi^2(3)$	2.924	5.881	12.395	2.940	3.714	1.240	3. 19.376
Conf.	.597	.882	.994	.599	.706	.257	4. 20.306

Table III

Sensitivity Analysis of the VAR

The second and third columns report the coefficient estimates and standard errors for the levels of interest rates which replace the forward premium in the basic VAR. The fourth column tests the hypothesis that the coefficients are equal and opposite in sign. The fifth and sixth columns report the tests of return predictability, which is now a $\chi^2(7)$, and the R^2. The quasi-differenced specifications enter dividend yields relative to a twenty-four month moving average, the interest differential and a variable constructed by subtracting .9 times the lagged interest rate from the current interest rate. The a columns use the quasi-differenced U.S. interest rate, and the b columns use the quasi-differenced foreign country interest rate.

	VAR with nominal interest rates					Quasi-Differenced Specifications			
Dep. Var.	Coef. i_{1t} (s.e.)	Coef. i_{jt} (s.e.)	$\chi^2(1)$ Conf.	$\chi^2(7)$ Conf.	R^2	$\chi^2(7)^a$ Conf.	R^{2a}	$\chi^2(7)^b$ Conf.	R^{2b}
				Panel A: U.S. - Japan					
r_{1t+1}	-8.298	12.439	0.502	29.247	.079	36.914	.074	35.752	.075
	(2.670)	(6.447)	.522	.999		.999		.999	
r_{2t+1}	-1.951	5.116	0.179	16.398	.047	15.462	.037	13.139	.037
	(2.489)	(8.063)	.317	.978		.961		.931	
rs_{2t+1}	-4.837	9.657	0.979	14.056	.092	13.933	.084	12.800	.083
	(2.164)	(5.202)	.678	.950		.948		.933	
				Panel B: U.S. - U.K.					
r_{1t+1}	-10.904	5.083	4.366	21.278	.072	17.611	.032	18.412	.027
	(2.873)	(2.613)	.963	.997		.986		.990	
r_{3t+1}	-6.431	2.607	1.052	6.613	.058	5.890	.024	5.793	.025
	(3.441)	(3.301)	.695	.530		.447		.436	
rs_{3t+1}	-8.003	9.430	0.321	30.771	.171	35.167	.196	34.382	.189
	(9.430)	(2.774)	.429	.999		.999		.999	
				Panel C: U.S. - Germany					
r_{1t+1}	-10.732	4.237	5.648	21.386	.040	14.333	.030	13.139	.017
	(4.320)	(4.554)	.983	.997		.954		.931	
r_{4t+1}	-8.493	3.274	1.483	13.074	.035	10.016	.038	9.910	.042
	(4.921)	(6.210)	.777	.930		.812		.806	
rs_{4t+1}	-10.969	13.057	0.877	37.070	.187	15.123	.051	14.222	.049
	(2.813)	(2.951)	.651	.999		.966		.953	

Table IV

Implied Long Horizon Statistics from the U.S.-Japan VAR

The implied long-horizon statistics are functions of the parameters of the vector autoregression. See the text for precise formulas. Panel A reports implied unconditional means, standard deviations and correlation coefficients. Panel B reports implied slope coefficients from the regression of a compound return for a given horizon onto a particular forecasting variable. Panel C reports the implied ratio of the variance of returns compounded over a given horizon k to k times the variance of the one period return. Panel D reports the implied R^2's from the VAR at horizon k which is one minus the ratio of the innovation variance to the total variance. The asymptotic standard errors are calculated as in equation (18).

Panel A: Means, Standard Deviations and Correlation Matrix:

	r_{1t}	r_{2t}	rs_{2t}	dy_{1t}	dy_{2t}	fp_{2t}
Means:	6.436	13.499	1.415	3.281	0.371	2.937
	(3712.769)	(6970.774)	(5523.402)	(668.686)	(565.037)	(353.428)

Standard Deviations and Correlation Matrix:

	r_{1t}	r_{2t}	rs_{2t}	dy_{1t}	dy_{2t}	fp_{2t}
r_{1t}	55.677	0.402	-0.028	-0.208	0.019	-0.207
	(7.097)	(0.088)	(0.086)	(0.067)	(0.047)	(0.067)
r_{2t}		56.935	0.132	-0.259	-0.152	-0.128
		(4.768)	(0.086)	(0.058)	(0.036)	(0.073)
rs_{2t}			41.839	-0.216	-0.097	-0.382
			(4.054)	(0.113)	(0.101)	(0.150)
dy_{1t}				0.661	0.811	0.533
				(0.224)	(0.114)	(0.168)
dy_{2t}					0.304	0.222
					(0.108)	(0.262)
fp_{2t}						2.125
						(0.541)

Panel B: Implied Slope Coefficients

Horizon in Months:

1	3	6	12	24	36	48	60	∞
U.S. return & U.S. dividend yield:								
7.218	23.302	39.549	57.580	73.096	80.952	86.197	89.965	100.328
(7.325)	(25.357)	(44.156)	(65.789)	(89.815)	(105.431)	(116.315)	(123.897)	(140.084)
Japanese return & Japanese dividend yield:								
0.161	2.313	9.271	29.685	71.450	104.494	129.104	147.235	197.458
(13.428)	(38.832)	(73.902)	(135.131)	(228.942)	(294.165)	(338.816)	(368.947)	(423.126)
forward bias & forward premium:								
-6.634	-18.807	-32.805	-49.211	-59.327	-60.572	-60.327	-59.626	-58.719
(1.843)	(5.348)	(10.272)	(18.891)	(31.339)	(39.789)	(46.048)	(50.858)	(64.827)

Panel C: Implied Variance Ratios

Horizon in Months:							
1	3	6	12	24	36	48	60
U.S. Return:							
1.000	1.023	0.919	0.768	0.625	0.559	0.521	0.496
(0.000)	(0.184)	(0.176)	(0.136)	(0.130)	(0.142)	(0.156)	(0.169)
Japanese Return:							
1.000	1.024	1.059	1.100	1.112	1.095	1.072	1.049
(0.000)	(0.102)	(0.175)	(0.288)	(0.425)	(0.504)	(0.557)	(0.597)
Forward Bias:							
1.000	1.246	1.594	2.114	2.679	2.936	3.068	3.145
(0.000)	(0.229)	(0.518)	(0.991)	(1.601)	(1.947)	(2.166)	(2.321)
Dollar-Yen Depreciation:							
1.000	1.186	1.460	1.872	2.317	2.513	2.608	2.660
(0.000)	(0.204)	(0.453)	(0.857)	(1.368)	(1.647)	(1.816)	(1.931)
Dollar Return on Japanese Equity:							
1.000	1.234	1.493	1.846	2.182	2.305	2.351	2.367
(0.000)	(0.197)	(0.418)	(0.770)	(1.213)	(1.463)	(1.623)	(1.738)
Yen Return on U.S. Equity:							
1.000	1.046	0.980	0.925	0.933	0.954	0.969	0.978
(0.000)	(0.223)	(0.279)	(0.369)	(0.532)	(0.633)	(0.697)	(0.741)

Panel D: Implied R^2's

Horizon in Months:							
1	3	6	12	24	36	48	60
U.S. Return:							
0.075	0.119	0.141	0.125	0.089	0.071	0.061	0.053
(0.044)	(0.079)	(0.100)	(0.101)	(0.100)	(0.100)	(0.098)	(0.094)
Japanese Return:							
0.103	0.128	0.151	0.142	0.093	0.063	0.048	0.039
(0.049)	(0.073)	(0.098)	(0.101)	(0.070)	(0.045)	(0.032)	(0.028)
Forward Bias:							
0.142	0.276	0.318	0.263	0.149	0.095	0.068	0.052
(0.100)	(0.165)	(0.172)	(0.149)	(0.105)	(0.077)	(0.061)	(0.050)

Table V

Implied Long Horizon Statistics from the U.S.-U.K. VAR

The implied long-horizon statistics are functions of the parameters of the vector autoregression. See the text for precise formulas. Panel A reports implied unconditional means, standard deviations and correlation coefficients. Panel B reports implied slope coefficients from the regression of a compound return for a given horizon onto a particular forecasting variable. Panel C reports the implied ratio of the variance of returns compounded over a given horizon k to k times the variance of the one period return. Panel D reports the implied R^2's from the VAR at horizon k which is one minus the ratio of the innovation variance to the total variance. The asymptotic standard errors are calculated as in equation (18).

Panel A: Means, Standard Deviations and Correlations

	r_{1t}	r_{3t}	rs_{3t}	dy_{1t}	dy_{3t}	fp_{3t}
Means:	4.386	3.173	6.592	3.646	3.646	-2.893
	(290.938)	(1212.588)	(797.780)	(42.020)	(116.444)	(133.042)

Standard Deviations and Correlation Matrix:

	r_{1t}	r_{3t}	rs_{3t}	dy_{1t}	dy_{3t}	fp_{3t}
r_{1t}	56.297	0.700	-0.005	-0.191	-0.122	-0.187
	(5.918)	(0.066)	(0.088)	(0.052)	(0.065)	(0.063)
r_{3t}		68.083	0.024	-0.079	-0.106	-0.028
		(6.029)	(0.093)	(0.089)	(0.087)	(0.071)
rs_{3t}			45.303	-0.228	-0.219	-0.342
			(3.779)	(0.147)	(0.150)	(0.128)
dy_{1t}				0.875	0.925	0.685
				(0.356)	(0.064)	(0.162)
dy_{3t}					1.006	0.567
					(0.348)	(0.225)
fp_{3t}						2.722
						(0.777)

Panel B: Implied Slope Coefficients

Horizon in Months:

1	3	6	12	24	36	48	60	∞
U.S. return & U.S. dividend yield:								
2.127	8.715	19.736	41.226	75.000	96.536	109.722	117.728	130.034
(5.672)	(20.072)	(41.450)	(77.962)	(124.343)	(145.204)	(152.639)	(153.944)	(143.896)
U.K. return & U.K. dividend yield:								
8.594	23.262	45.482	84.735	140.433	174.187	194.608	206.972	225.966
(6.719)	(19.184)	(36.960)	(64.600)	(93.862)	(105.533)	(111.603)	(116.245)	(132.688)
forward bias & forward premium:								
-6.333	-16.786	-29.315	-47.250	-69.008	-81.491	-88.971	-93.491	-100.432
(1.160)	(3.363)	(7.188)	(16.215)	(35.035)	(51.556)	(64.736)	(74.673)	(97.602)

Panel C: Implied Variance Ratios

Horizon in Months:	1	3	6	12	24	36	48	60
U.S. Return:								
	1.000	1.111	1.161	1.166	1.087	0.997	0.919	0.857
	(0.000)	(0.187)	(0.242)	(0.263)	(0.308)	(0.377)	(0.435)	(0.477)
U.K. Return:								
	1.000	0.880	0.847	0.792	0.700	0.630	0.577	0.537
	(0.000)	(0.111)	(0.142)	(0.157)	(0.167)	(0.180)	(0.189)	(0.194)
Forward Bias:								
	1.000	1.103	1.362	1.781	2.366	2.766	3.057	3.276
	(0.000)	(0.191)	(0.429)	(0.861)	(1.587)	(2.175)	(2.657)	(3.054)
Dollar-Pound Depreciation:								
	1.000	1.034	1.214	1.511	1.929	2.215	2.425	2.582
	(0.000)	(0.159)	(0.344)	(0.680)	(1.236)	(1.681)	(2.042)	(2.338)
Dollar Return on U.K. Equity:								
	1.000	0.872	0.927	1.014	1.084	1.108	1.119	1.125
	(0.000)	(0.119)	(0.199)	(0.318)	(0.489)	(0.618)	(0.719)	(0.799)
Pound Return on U.S. Equity:								
	1.000	1.178	1.217	1.221	1.211	1.202	1.196	1.190
	(0.000)	(0.185)	(0.268)	(0.368)	(0.545)	(0.688)	(0.798)	(0.883)

Panel D: Implied R^2's

Horizon in Months:	1	3	6	12	24	36	48	60
U.S. Return:								
	0.074	0.093	0.096	0.082	0.074	0.075	0.074	0.071
	(0.065)	(0.077)	(0.088)	(0.105)	(0.146)	(0.168)	(0.172)	(0.168)
U.K. Return:								
	0.111	0.118	0.151	0.196	0.267	0.304	0.314	0.307
	(0.102)	(0.112)	(0.151)	(0.215)	(0.305)	(0.341)	(0.346)	(0.339)
Forward Bias:								
	0.198	0.319	0.391	0.397	0.331	0.268	0.219	0.181
	(0.096)	(0.174)	(0.215)	(0.250)	(0.273)	(0.266)	(0.245)	(0.219)

Table VI

Implied Long Horizon Statistics from the U.S.-Germany VAR

The implied long-horizon statistics are functions of the parameters of the vector autoregression. See the text for precise formulas. Panel A reports implied unconditional means, standard deviations and correlation coefficients. Panel B reports implied slope coefficients from the regression of a compound return for a given horizon onto a particular forecasting variable. Panel C reports the implied ratio of the variance of returns compounded over a given horizon k to k times the variance of the one period return. Panel D reports the implied R^2's from the VAR at horizon k which is one minus the ratio of the innovation variance to the total variance. The asymptotic standard errors are calculated as in equation (18).

Panel A: Means, Standard Deviations and Correlations

	r_{1t}	r_{4t}	rs_{4t}	dy_{1t}	dy_{4t}	fp_{4t}
Means:	4.584	6.125	6.826	3.660	3.239	2.988
	(694.752)	(787.129)	(1801.187)	(119.146)	(172.255)	(88.183)

Standard Deviation and Correlation Matrix:

	r_{1t}	r_{4t}	rs_{4t}	dy_{1t}	dy_{4t}	fp_{4t}
r_{1t}	56.497	0.461	-0.046	-0.186	-0.126	-0.188
	(6.475)	(0.118)	(0.081)	(0.052)	(0.061)	(0.072)
r_{4t}		70.856	-0.101	-0.061	-0.177	-0.105
		(5.971)	(0.076)	(0.114)	(0.077)	(0.098)
rs_{4t}			42.602	-0.169	-0.222	-0.355
			(2.845)	(0.122)	(0.121)	(0.098)
dy_{1t}				0.877	0.776	0.510
				(0.386)	(0.161)	(0.205)
dy_{4t}					0.915	0.368
					(0.242)	(0.250)
fp_{4t}						1.537
						(0.391)

Panel B: Implied Slope Coefficients

Horizon in Months:

1	3	6	12	24	36	48	60	∞
U.S. return & U.S. dividend yield:								
2.538	9.881	20.191	39.010	67.890	87.105	99.686	107.895	123.269
(6.472)	(22.990)	(46.300)	(85.844)	(138.777)	(166.844)	(180.436)	(186.183)	(180.468)
German return & German dividend yield:								
3.202	13.467	29.098	59.700	109.612	143.626	166.007	180.626	208.014
(5.568)	(18.210)	(37.702)	(74.659)	(130.985)	(164.804)	(184.399)	(196.070)	(217.750)
forward bias & forward premium:								
-8.096	-18.702	-29.336	-45.237	-67.905	-82.638	-92.236	-98.492	-110.206
(1.918)	(6.183)	(12.772)	(25.865)	(50.230)	(71.238)	(102.146)	(102.146)	(140.820)

Panel C: Implied Variance Ratios

Horizon in Months:							
1	3	6	12	24	36	48	60
U.S. Return:							
1.000	1.089	1.089	1.062	0.982	0.907	0.845	0.794
(0.000)	(0.190)	(0.242)	(0.259)	(0.292)	(0.355)	(0.417)	(0.466)
German Return:							
1.000	1.162	1.192	1.194	1.150	1.099	1.054	1.017
(0.000)	(0.161)	(0.232)	(0.276)	(0.283)	(0.268)	(0.254)	(0.242)
Forward Bias:							
1.000	1.118	1.327	1.643	2.104	2.443	2.703	2.907
(0.000)	(0.173)	(0.346)	(0.643)	(1.151)	(1.586)	(1.960)	(2.282)
Dollar-DM Depreciation:							
1.000	1.083	1.258	1.529	1.927	2.220	2.444	2.620
(0.000)	(0.161)	(0.311)	(0.571)	(1.014)	(1.390)	(1.713)	(1.990)
Dollar Return on German Equity:							
1.000	1.081	1.190	1.308	1.421	1.479	1.515	1.540
(0.000)	(0.131)	(0.218)	(0.322)	(0.486)	(0.637)	(0.770)	(0.884)
DM Return on U.S. Equity:							
1.000	1.136	1.143	1.135	1.110	1.089	1.072	1.058
(0.000)	(0.166)	(0.222)	(0.267)	(0.344)	(0.419)	(0.483)	(0.536)

Panel D: Implied R^2's

Horizon in Months:							
1	3	6	12	24	36	48	60
U.S. Return:							
0.039	0.055	0.065	0.068	0.067	0.068	0.067	0.065
(0.044)	(0.067)	(0.091)	(0.126)	(0.173)	(0.197)	(0.205)	(0.202)
German Return:							
0.096	0.059	0.059	0.078	0.109	0.122	0.124	0.120
(0.081)	(0.075)	(0.104)	(0.164)	(0.232)	(0.252)	(0.250)	(0.238)
Forward Bias:							
0.185	0.214	0.256	0.298	0.298	0.265	0.229	0.196
(0.075)	(0.128)	(0.173)	(0.220)	(0.257)	(0.265)	(0.257)	(0.241)

Table VII

Models With One Latent Variable

The single latent variable model imposes twelve cross equation constraints on the three excess return equations of the VAR as in equations (19)-(21). The overall test of the model is the $\chi^2(12)$ statistic. The parameter estimates are the quasi-reduced-form coefficients. The test of return predictability is the $\chi^2(6)$ statistic.

Panel A:		betas	1.794	0.628		$\chi^2(12)$	20.474	
U.S.-Japan		(s.e.)	(0.571)	(0.358)		Conf.	.941	
Dep. Var.	Con.	r_{1t}	r_{jt}	rs_{jt}	dy_{1t}	dy_{jt}	fp_{jt}	$\chi^2(6)$
	(s.e.)	(s.e.)	(s.e.)	(s.e.)	(s.e.)	(s.e.)	(s.e.)	Conf.
	Conf.	Conf.	Conf.	Conf.	Conf.	Conf.	Conf.	
	54.812	0.047	-0.036	0.002	-13.947	23.357	-2.872	10.245
r_{1t+1}	(26.641)	(0.046)	(0.040)	(0.059)	(8.032)	(11.423)	(1.242)	.885
	0.960	0.699	0.622	0.022	0.918	0.959	0.979	
	98.323	0.085	-0.064	0.003	-25.019	41.899	-5.151	25.355
r_{2t+1}	(34.857)	(0.083)	(0.069)	(0.105)	(11.415)	(15.925)	(1.972)	.999
	0.995	0.691	0.645	0.022	0.972	0.991	0.991	
	34.439	0.030	-0.022	0.001	-8.763	14.676	-1.804	5.167
rs_{2t+1}	(17.113)	(0.032)	(0.025)	(0.037)	(4.987)	(7.743)	(1.041)	.360
	0.956	0.644	0.624	0.022	0.921	0.942	0.917	
Panel B:		betas	1.319	-0.003		$\chi^2(12)$	25.554	
U.S.- U.K.		(s.e.)	(0.231)	(0.246)		Conf.	.988	
	-92.228	0.179	-0.230	-0.065	28.764	-7.980	-5.790	19.833
r_{1t+1}	(36.611)	(0.140)	(0.116)	(0.085)	(10.465)	(9.607)	(1.771)	.997
	0.988	0.799	0.952	0.557	0.994	0.594	0.999	
	-121.615	0.236	-0.303	-0.086	37.929	-10.522	-7.635	20.043
r_{3t+1}	(46.227)	(0.190)	(0.152)	(0.110)	(13.284)	(12.685)	(2.320)	.997
	0.991	0.786	0.954	0.563	0.996	0.593	0.999	
	0.300	-0.001	0.001	0.0001	-0.094	0.026	0.019	0.001
rs_{3t+1}	(22.732)	(0.044)	(0.057)	(0.016)	(7.085)	(1.963)	(1.428)	.001
	0.011	0.011	0.011	0.010	0.011	0.011	0.011	
Panel C:		betas	2.856	-1.369		$\chi^2(12)$	16.183	
U.S.-Germany		(s.e.)	(1.178)	(0.826)		Conf.	.817	
	-10.608	0.119	-0.005	-0.070	4.937	-1.052	-1.130	4.409
r_{1t+1}	(9.745)	(0.067)	(0.026)	(0.053)	(3.857)	(2.479)	(1.100)	.268
	0.724	0.925	0.138	0.814	0.799	0.329	0.696	
	-30.733	0.341	-0.013	-0.200	14.103	-3.006	-3.227	21.361
r_{4t+1}	(25.839)	(0.118)	(0.076)	(0.125)	(8.958)	(6.783)	(2.795)	.997
	0.759	0.996	0.137	0.891	0.885	0.342	0.752	
	14.519	-0.163	0.006	0.096	-6.758	1.440	1.546	11.385
rs_{4t+1}	(11.726)	(0.057)	(0.036)	(0.065)	(4.662)	(3.327)	(1.526)	.877
	0.784	0.996	0.136	0.863	0.853	0.335	0.689	

Table VIII

Models With Two Latent Variables

The models with two latent variables impose five cross equation constraints on the three excess return equations of the VAR as in equations (22)-(24). The overall test of the model is the $\chi^2(5)$ statistic. The parameter estimates are the quasi-reduced-form coefficients. The test of return predictability is the $\chi^2(6)$ statistic.

Panel A:		betas	$\beta_1 = 0.052$	$\beta_2 = 0.366$		$\chi^2(5)$	9.840	
U.S.-Japan		(s.e.)	(0.236)	(0.190)		Conf.	.920	
Dep. Var.	Con.	r_{1t}	r_{jt}	rs_{jt}	dy_{1t}	dy_{jt}	fp_{jt}	$\chi^2(6)$
	(s.e.)	(s.e.)	(s.e.)	(s.e.)	(s.e.)	(s.e.)	(s.e.)	Conf.
	Conf.	Conf.	Conf.	Conf.	Conf.	Conf.	Conf.	
	-63.364	0.113	-0.137	-0.0001	32.113	-31.786	-8.533	31.786
r_{1t+1}	(47.969)	(0.113)	(0.079)	(0.114)	(15.514)	(18.805)	(2.174)	.999
	0.813	0.685	0.918	0.001	0.962	0.909	0.999	
	93.192	0.118	-0.037	-0.029	-28.146	54.880	-3.833	20.278
r_{2t+1}	(39.039)	(0.103)	(0.074)	(0.116)	(13.618)	(19.516)	(2.322)	.998
	0.983	0.745	0.379	0.197	0.961	0.995	0.901	
	30.788	0.049	-0.021	-0.011	-8.620	18.420	-1.849	5.360
rs_{2t+1}	(23.536)	(0.047)	(0.038)	(0.044)	(9.033)	(12.536)	(1.710)	.384
	0.809	0.700	0.415	0.189	0.660	0.858	0.720	
Panel B:		betas	$\beta_1 = 1.973$	$\beta_2 = -0.669$		$\chi^2(5)$	3.347	
U.S.- U.K.		(s.e.)	(0.758)	(0.505)		Conf.	.353	
	-43.575	0.091	-0.154	-0.094	10.142	-1.472	-6.242	17.988
r_{1t+1}	(23.223)	(0.089)	(0.085)	(0.062)	(7.542)	(6.016)	(1.660)	.994
	0.939	0.695	0.930	0.873	0.821	0.193	0.999	
	-70.814	0.373	-0.392	0.045	11.154	6.062	-4.497	10.447
r_{3t+1}	(37.333)	(0.171)	(0.140)	(0.114)	(12.644)	(10.980)	(2.354)	.893
	0.942	0.971	0.995	0.305	0.622	0.419	0.944	
	-38.571	-0.070	-0.041	-0.216	12.543	-6.960	-9.304	27.180
rs_{3t+1}	(26.695)	(0.083)	(0.072)	(0.093)	(11.644)	(8.023)	(2.463)	.999
	0.852	0.601	0.430	0.980	0.741	0.614	0.999	
Panel C:		betas	$\beta_1 = 4.308$	$\beta_2 = -1.593$		$\chi^2(5)$	5.300	
U.S.-Germany		(s.e.)	(4.402)	(1.743)		Conf.	.620	
	13.855	0.075	-0.027	-0.062	5.508	-3.886	-4.946	6.770
r_{1t+1}	(15.547)	(0.073)	(0.044)	(0.063)	(4.905)	(4.298)	(2.697)	.657
	0.627	0.699	0.454	0.679	0.739	0.634	0.933	
	8.448	0.310	-0.059	-0.121	10.138	-3.015	-7.442	15.881
r_{4t+1}	(32.230)	(0.148)	(0.120)	(0.150)	(10.895)	(8.469)	(3.509)	.986
	0.207	0.964	0.378	0.578	0.648	0.278	0.966	
	46.229	-0.169	-0.021	-0.077	7.579	-11.937	-9.453	37.349
rs_{4t+1}	(17.275)	(0.066)	(0.048)	(0.094)	(5.836)	(5.370)	(2.159)	.999
	0.993	0.989	0.339	0.589	0.806	0.974	0.999	

Table IX

U.S., Japan, U.K. Latent Variable Models

The dependent variables are the three equity and two foreign exchange excess returns. The instrumental variables are a constant, the three dividend yields and the two forward premiums. The model with one (two) latent variables imposes twenty (twelve) cross equation constraints.

Panel A:	betas	$\beta_1 = 1.216$	$\beta_2 = 1.312$	$\beta_3 = 0.416$	$\beta_4 = -0.489$	$\chi^2(20)$	35.019
One Latent Var.	(s.e.)	(0.486)	(0.412)	(0.363)	(0.360)	Conf.	.980

Dep. Var.	Con. (s.e.) Conf.	dy_{1t} (s.e.) Conf.	dy_{2t} (s.e.) Conf.	dy_{3t} (s.e.) Conf.	fp_{2t} (s.e.) Conf.	fp_{3t} (s.e.) Conf.	$\chi^2(5)$ Conf.
	-26.848	8.331	-0.888	4.122	-4.725	0.221	9.050
r_{1t+1}	(21.052)	(6.165)	(16.004)	(7.147)	(2.076)	(1.675)	.893
	0.798	0.823	0.044	0.436	0.977	0.105	
	-32.650	10.132	-1.080	5.013	-5.749	0.268	15.048
r_{2t+1}	(23.551)	(6.840)	(19.449)	(8.666)	(2.319)	(2.045)	.990
	0.834	0.861	0.044	0.437	0.987	0.104	
	-35.238	10.935	-1.166	5.410	-6.201	0.289	16.129
r_{3t+1}	(26.296)	(7.650)	(21.021)	(9.385)	(2.473)	(2.201)	.994
	0.820	0.847	0.044	0.436	0.988	0.105	
	-11.169	3.466	-0.370	1.715	-1.965	0.092	1.784
rs_{2t+1}	(11.337)	(3.541)	(6.608)	(3.007)	(1.584)	(0.699)	.122
	0.675	0.672	0.045	0.432	0.785	0.104	
	13.136	-4.076	0.435	-2.017	2.312	-0.108	3.083
rs_{3t+1}	(11.317)	(3.303)	(7.749)	(3.442)	(1.454)	(0.801)	.313
	0.754	0.783	0.045	0.442	0.888	0.107	

Panel B:	betas	$\beta_1 = 0.351$	$\beta_2 = 0.464$	$\beta_3 = 0.901$	$\beta_4 = -0.109$	$\beta_5 = 2.064$	$\beta_6 = -0.519$
Two Latent Var.	(s.e.)	(0.401)	(0.209)	(0.489)	(0.277)	(0.883)	(0.519)
$\chi^2(12) = 18.298$ Conf. = .893							

Dep. Var.	Con. (s.e.) Conf.	dy_{1t} (s.e.) Conf.	dy_{2t} (s.e.) Conf.	dy_{3t} (s.e.) Conf.	fp_{2t} (s.e.) Conf.	fp_{3t} (s.e.) Conf.	$\chi^2(5)$ Conf.
	5.363	2.370	22.905	-9.533	-0.171	-5.033	15.803
r_{1t+1}	(25.718)	(8.455)	(16.297)	(6.694)	(1.357)	(1.730)	.993
	0.165	0.221	0.840	0.846	0.100	0.996	
	101.477	-32.490	76.680	-5.839	-1.020	-3.653	17.617
r_{2t+1}	(40.318)	(12.415)	(33.145)	(16.918)	(3.371)	(3.183)	.997
	0.988	0.991	0.979	0.270	0.238	0.749	
	48.975	-14.248	43.616	-6.051	-0.533	-3.460	6.204
r_{3t+1}	(33.766)	(10.117)	(24.585)	(9.895)	(1.921)	(2.617)	.713
	0.853	0.841	0.924	0.459	0.219	0.814	
	-6.260	5.678	12.256	-7.951	-0.042	-4.136	12.650
rs_{2t+1}	(19.077)	(6.907)	(12.608)	(5.049)	(0.961)	(1.565)	.973
	0.257	0.590	0.669	0.885	0.035	0.992	
	-41.6627	21.765	7.464	-16.648	0.177	-8.493	26.623
rs_{3t+1}	(27.349)	(11.263)	(19.312)	(8.750)	(1.922)	(2.566)	.999
	0.872	0.947	0.301	0.943	0.073	0.999	

Table X

Hansen-Jagannathan (1991) Bounds on the Coefficient of Variation of the Nominal Dollar Intertemporal Marginal Rate of Substitution

All returns are dollar denominated. The unscaled bounds use excess returns. The scaled bounds use excess returns and pseudo excess returns generated by scaling an equity return with the own dividend yield and a foreign exchange return with the own forward premium. The cross-scaled bounds use excess returns, the previous scaled returns, and additional pseudo returns generated by scaling an equity return with the dollar-yen forward premium and a foreign exchange return with the U.S. dividend yield. Standard errors are in parenthesis and are calculated using a Taylor's series approximation and three Newey-West (1987) lags.

Excess Returns Included in the Tests	Bound (unscaled) (s.e.)	Bound (scaled) (s.e.)	Bound (cross-scaled) (s.e.)
U.S. Equity	0.112 (0.153)	0.116 (0.100)	0.337 (0.086)
Japanese Equity	0.225 (0.210)	0.239 (0.095)	0.410 (0.069)
U.K. Equity	0.100 (0.107)	0.103 (0.093)	0.271 (0.064)
German Equity	0.128 (0.148)	0.183 (0.101)	0.381 (0.074)
Japanese Foreign Exchange	0.004 (0.111)	0.320 (0.082)	0.320 (0.082)
U.K. Foreign Exchange	0.060 (0.133)	0.394 (0.068)	0.405 (0.075)
German Foreign Exchange	0.045 (0.127)	0.319 (0.066)	0.337 (0.073)
U.S. Equity, Japanese Equity and Foreign Exchange	0.305 (0.098)	0.474 (0.097)	0.598 (0.093)
U.S. Equity, U.K. Equity and Foreign Exchange	0.181 (0.111)	0.474 (0.068)	0.579 (0.089)
U.S. Equity, German Equity and Foreign Exchange	0.181 (0.124)	0.384 (0.093)	0.519 (0.097)
Japanese, U.K. and German Foreign Exchange	0.077 (0.104)	0.477 (0.075)	0.479 (0.077)
U.S., Japanese, U.K. and German Equity	0.237 (0.105)	0.301 (0.089)	0.585 (0.080)
U.S. Equity, Japanese, U.K., and German Equity and Foreign Exchange	0.331 (0.111)	0.641 (0.088)	0.776 (0.083)