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THE GENDER PAY GAP:
MICRO SOURCES AND MACRO CONSEQUENCES

Iacopo Morchio
Christian Moser

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ABSTRACT

Using linked employer-employee data from Brazil, we document a large gender pay gap due to women working at lower-paying employers with better nonpay attributes. To interpret these facts, we develop an equilibrium search model with endogenous firm pay, amenities, and hiring. We provide a constructive proof of identification of all model parameters. The estimated model suggests that amenities are important for both men and women, that compensating differentials explain half of the gender pay gap, and that there are significant output and welfare gains from eliminating gender differences. However, equal-treatment policies fail to achieve those gains.

Iacopo Morchio
University of Bristol
Iacopo.morchio@bristol.ac.uk

Christian Moser
Columbia Business School
546 Kravis Hall
665 West 130th Street
New York, NY 10027
and CEPR
and also NBER
c.moser@columbia.edu

A data appendix is available at <http://www.nber.org/data-appendix/w32408>

1 Introduction

Many workhorse models of the labor market feature a tight link between firm pay, size, productivity, and worker utility (Burdett and Mortensen, 1998). Through the lens of these models, firm pay differences between identical individuals reflect output and welfare losses from misallocation of workers, sustained by labor market frictions (Lentz and Mortensen, 2010). Under this view, it seems alarming that we observe women, who make up nearly half of the labor force, sorted into firms with significantly lower pay compared to men. At the same time, an empirical literature has convincingly established, based on survey data and experiments, that nonpay job attributes are important (Hall and Mueller, 2018), and that women have a higher willingness to pay for amenities such as work flexibility and employment stability (Wiswall and Zafar, 2017). Thus, it seems natural to revisit the observed gender differences in sorting through the lens of a richer framework that takes into account firm heterogeneity in both pay and nonpay attributes.

This paper's goal is to identify the microeconomic sources of the gender pay gap in order to assess its macroeconomic consequences. Our analysis proceeds in four steps. First, we establish empirical facts on gender differences in sorting across firm pay and amenities. Second, we interpret these facts by developing an equilibrium search model with endogenous firm pay, amenities, and employment. Third, we provide a constructive proof of identification of all model parameters based on linked employer-employee data. Finally, we use the estimated model to shed light on the structure of compensation across firms, to decompose the gender pay gap, and to simulate counterfactual equal-pay and equal-hiring policies. In doing so, we provide the first estimates of output and welfare losses from misallocation of workers across firms by gender.

In the first step, we leverage rich linked employer-employee data from Brazil, which has a large gender pay gap of 13.3 log points, making this an interesting context to study gender inequality. An advantage of studying Brazil is that it offers remarkably detailed information on gender-relevant labor market variables such as workers' education, occupation, tenure, work hours, and employment histories with information on parental leaves. To estimate firm pay differences for identical workers by gender, we follow Card et al.'s (2016) extension of the seminal two-way fixed effects (FEs) framework by Abowd, Kramarz, and Margolis (1999, henceforth AKM). Controlling for worker heterogeneity, we find a gender firm pay gap of 11.3 log points (i.e., 85.0% of the overall gender pay gap), mostly due to women sorting to lower-paying firms relative to men. Strikingly, men enjoy a sizable pay premium at larger firms, while pay is essentially flat across firm sizes for women. This is in spite of women being

disproportionately likely to work at the largest firms. Taken together, this poses a puzzle for models in which firms can be larger only by paying more. As a potential resolution to this puzzle, we show that women's jobs have better nonpay attributes, and more so at large firms.

In the second step, we develop an equilibrium search model, based on the seminal framework by [Burdett and Mortensen \(1998\)](#), with endogenous gender differences in firm pay, amenities, and hiring. Workers differ in their gender and ability and search for jobs both in and out of employment. Firms differ in their productivity, gender preferences, and amenity costs and face a convex increasing vacancy cost schedule. Our model accommodates several competing explanations for the gender pay gap, including gender-specific *compensating differentials* ([Rosen, 1986](#)), *taste-based discrimination* ([Becker, 1971](#)), and *monopsony power* ([Robinson, 1933](#)). The model features pay and utility dispersion both within and between worker types. The existence of pay differences, however, is neither necessary nor sufficient for the existence of utility differences. Job-to-job transitions may entail pay declines. Firms can discriminate based on their pay offers, amenities, or hiring decisions. Men and women climb different firm ladders. Finally, even nondiscriminatory firms without regard for gender may treat women differently as a best response to the labor market environment. To sum up, the gender-specific distributions of firm pay, amenities, and hiring are all jointly determined in equilibrium, making it a formidable task to isolate each of the model's features.

In the third step, we separately identify all model parameters, including labor market objects, gender-specific firm types, and economy-wide elasticities of the vacancy and amenity cost functions. We demonstrate that our equilibrium model admits a log-additive wage equation with separable worker and firm components, akin to [Card et al.'s \(2016\)](#) extension of AKM, which is helpful for two reasons. First, it enables us to interpret the gender-specific employer FEs from our empirical analysis through the lens of the structural model. Second, it allows us to control for gender-specific selection based on ability ([Mulligan and Rubinstein, 2008](#)). To identify labor market objects, we follow a revealed-preferences argument based on worker flows. Next, we identify gender-specific firm types. From a bird's eye view, we leverage the intuition that firms' unobserved surplus maps into hiring decisions. We show how to invert this model mapping to recover firm-level utility offers. By comparing those to firm pay, we back out the gender-specific amenity values at each firm. We then estimate employer preferences over gender by comparing equilibrium outcomes between men and women at the same firm. Finally, we show how to pin down the economy-wide elasticity parameters guiding vacancy and amenity costs based on aggregate moments. A novel aspect of our approach is that we do not rely on any distributional assumptions in identifying a large number of model parameters.

In the fourth step, we use the estimated model to revisit the observed patterns of gender-specific sorting across firms. By identifying rich gender-firm heterogeneity, our model provides several novel insights regarding the structure of firm pay and amenities. We find that amenities play an important role for both genders, with a mean amenity share of 48.8% for men and 52.2% for women. However, higher-ranked employers for men mostly offer higher pay, while for women they offer higher amenities. Compensating differentials explain the lion's share of overall firm pay dispersion, with utility dispersion only accounting for 4.4% of pay dispersion for men and 3.6% of that for women. This is all the more striking given that we find significant labor market frictions in Brazil. Taking into account gender differences in amenities, the gender gap in total compensation becomes 4.6 log points (i.e., 40.7% of the gender pay gap). Altogether, these results suggest that compensating differentials are central to understanding gender-specific sorting across firms.

Given the importance of firm-level amenities, we return to our motivation regarding the micro sources and macro consequences of the gender pay gap. We leverage the equilibrium nature of our model to decompose gender gaps in pay, amenities, and utility by shutting down one model ingredient at a time. In a world without firm heterogeneity in amenities, the gender pay gap closes by 45%, largely due to a relocation of women toward formerly male-dominated firms. Shutting down differences in employer preferences over gender eliminates the gender pay gap and leads to output gains of 12.9% but comes at the cost of pulling women into low-amenity firms. Gender differences in labor market efficiency have little effect on either pay, amenity, or utility gaps. Finally, removing all gender differences in the economy leads to output gains of 6.1% and welfare gains of 2.1%. While sizable, these numbers are significantly smaller than pay differences alone might suggest. Nevertheless, these potential gains motivate our assessment of equal-pay and equal-hiring policies using equilibrium counterfactuals. The bottom line is that both policies close part of the gender pay gap but lower worker welfare due to their adverse incentive effects on firms' pay, amenity, and hiring decisions. Thus, our results underline the importance of studying such policies in general equilibrium.

Related Literature. A burgeoning literature highlights the role of employer heterogeneity in explaining empirical pay dispersion (Card et al., 2013, 2018; Alvarez et al., 2018; Song et al., 2018). Our work builds on Card et al.'s (2016) extension of the seminal framework by AKM with gender-specific employer pay components.¹ Relative to their work, we make three contributions. First, we offer a

¹Complementary work on gender gaps in firm pay includes Sorkin (2017), Coudin et al. (2018), Bruns (2019), Barth et al. (2021), Casarico and Lattanzio (2022), Cruz and Rau (2022), Palladino et al. (2022), Lentz et al. (2023), and Vattuone (2023).

microfoundation for the wage equation in [Card et al. \(2016\)](#) and empirical patterns of worker sorting across firms by gender based on a tractable *equilibrium* model. Second, whereas [Card et al. \(2016\)](#) rationalize gender gaps in employer pay through differences in exogenous bargaining parameters across the sexes, we identify more than one reason behind them: compensating differentials ([Rosen, 1986](#)), taste-based discrimination ([Becker, 1971](#)), and monopsony power ([Robinson, 1933](#)). Third, we simulate a series of counterfactual experiments, including equal-treatment policies, for which the equilibrium nature of our model is crucial, as firms adjust their pay, amenity, and hiring.

Our equilibrium search model builds on the influential framework by [Burdett and Mortensen \(1998\)](#), which has been developed in different directions by [Bontemps et al. \(1999, 2000\)](#), [Moscarini and Postel-Vinay \(2013, 2018\)](#), [Meghir et al. \(2015\)](#), [Lise and Robin \(2017\)](#), [Bagger and Lenz \(2019\)](#), [Bilal et al. \(2022\)](#), and [Engbom and Moser \(2022\)](#). In these models, firms are heterogeneous only in productivity. Consequently, workers agree on a firm ranking, and wage gains go hand in hand with efficiency gains. Departing from this tradition, we develop a model with richer firm heterogeneity, which we identify based on linked employer-employee data. Specifically, we allow firms to differ not just in productivity but also in preferences over gender and amenity costs. As a result, firm pay, amenities, and hiring are jointly determined in equilibrium. In spite of this added complexity, we provide a constructive proof of identification of all model parameters, including labor market objects, gender-specific firm types, and economy-wide elasticities of the vacancy and amenity cost functions. By allowing for this richness, several novel insights emerge regarding gender-specific compensation structures across firms. Compared to aforementioned work, our model has radically different implications for the interpretation of empirical pay dispersion in relation to misallocation and welfare.²

There is ample empirical evidence that job amenities matter for labor market outcomes ([Hamer-mesh, 1999](#); [Pierce, 2001](#); [Hall and Mueller, 2018](#); [Sockin, 2022](#); [Maestas et al., 2023](#)), especially for women ([Goldin, 2014](#); [Mas and Pallais, 2017, 2019](#); [Wiswall and Zafar, 2017](#); [Chen et al., 2020](#)). However, quantifying the role of firm-level amenities is complicated by both data limitations and theoretical challenges. Regarding data, many firm-level amenities are unobserved to the analyst, so their valuations must be inferred under additional assumptions.³ Regarding theory, valuations of firm-

²For example, [Bagger et al. \(2014\)](#) find “*large marginal output and wage gains associated with labor reallocation*” (p. 5) and conclude that “*the finding that misallocation persists under these circumstances suggests that labor market frictions are important barriers to growth*” (p. 1). Furthermore, [Lentz and Mortensen \(2010\)](#) conclude that “*the reallocation of employment from less to more productive firms will yield efficiency gains*” (p. 577) and that “*workers will find it in their interest to seek out higher-paying employers*” (p. 577). Neither of these conclusions necessarily follows in our model with heterogeneity in employer amenities.

³Several works have estimated the values of specific job amenities like employer health insurance ([Dey and Flinn, 2005](#)), job security ([Jarosch, 2023](#)), fatality risk ([Lavetti and Schmutte, 2018](#)), commuting costs ([Flemming, 2020](#)), location ([Heise and Porzio, 2023](#)), family friendliness ([Hotz et al., 2018](#); [Xiao, 2023](#)), and working conditions ([Bonhomme and Jolivet, 2009](#)).

level amenities are not easily obtained in existing models, especially in the presence of frictions.⁴

Three related papers that also use linked employer-employee data stand out in this context. First, [Taber and Vejlin \(2020\)](#) develop a model with comparative advantage, search frictions, and compensating differentials. Despite its rich features, some of which we abstract from, they nonparametrically identify nearly all model parameters. A notable exception is workers' bargaining power, which is not identified since their revealed-preferences approach pins down *ordinal* but not *cardinal* utility.

Second, [Sorkin \(2018\)](#) embeds discrete choice within a search model, which can identify what he terms the "*Rosen motive*" of compensating differentials, capturing amenities dispersion conditional on a firm's value. In contrast, his model cannot identify what he terms the "*Mortensen motive*," capturing amenities dispersion correlated with firm values. This is because, in his model, the variance of utility is not pinned down due to an arbitrary but necessary normalization of the scale parameter of the type-I extreme value distribution guiding idiosyncratic utility draws.⁵ By allowing firms to choose hiring subject to a commonly used vacancy cost function, the parameters of which we identify, our general-equilibrium model recovers the entire distribution of firm values and amenities, which would not have been possible in the partial-equilibrium models of [Taber and Vejlin \(2020\)](#) or [Sorkin \(2018\)](#).

Third, [Lamadon et al. \(2022\)](#) develop an equilibrium labor market model featuring compensating differentials and rent sharing. Their model is frictionless, which implies that observed wages reflect productive attributes and idiosyncratic preferences following a nested logit structure. We complement their work by developing a distribution-free model that features search frictions, yet remains point-identified.⁶ Interestingly, we find a similarly important role for amenities and compensating differentials as they do, even under large search frictions. In addition, our model has several unique implications for gender inequality and equal-treatment policies not previously considered.

Outline. The paper is structured as follows. Section 2 describes the data. Section 3 presents motivating empirical facts. Section 4 develops our equilibrium model. Section 5 provides a constructive identification proof. Section 6 shows estimation results. Section 7 analyzes gender-specific compensation structures across employers. Section 8 simulates counterfactuals. Finally, Section 9 concludes.

Theoretical work by [Hwang et al. \(1998\)](#), [Lang and Majumdar \(2004\)](#), and [Albrecht et al. \(2018\)](#) develop models with *nonspecific* job amenities. Relatedly, [Sullivan and To \(2014\)](#), [Hall and Mueller \(2018\)](#), [Jung and Kuhn \(2019\)](#), [Luo and Mongey \(2019\)](#), and [Hsieh et al. \(2019\)](#) estimate nonspecific amenity values using individual-level (i.e., not linked employer-employee) data.

⁴In this sense, our model parallels [Boerma and Karabarbounis \(2021\)](#) who identify unobserved home production values.

⁵See Appendix C.8 for a detailed comparison between our model and that in [Sorkin \(2018\)](#).

⁶[Lamadon et al. \(2022\)](#) note that "*while incorporating [search frictions] would be interesting, it would also present severe challenges to identification, especially if one allows for two-sided heterogeneity*" (p. 210). We formally identify our model, though it is worth noting that our notion of worker heterogeneity and our production structure are substantially simpler than theirs.

2 Data Description

Dataset. Our main data source is the Brazilian linked employer-employee register *Relação Anual de Informações Sociais* (RAIS), which covers all workers at tax-registered employers. Starting in 2007, there is information on worker absences, including parental leaves. In 2015, the country entered a severe recession. Therefore, we restrict attention to the eight-year period from 2007 to 2014.

Variables. The data contain unique identifiers for workers and establishments (henceforth “employers” or “firms”). For each job spell, we observe the start and end dates, mean monthly earnings (henceforth “wage” or “pay”), as well as the worker’s gender, educational attainment in nine categories, worker age in years, tenure in years, contractual work hours per week, five-digit sector codes with 672 categories, municipality codes with 5,565 categories, and six-digit occupation codes with 2,383 categories. We exploit the full panel of the data going back to 1985 together with the tenure variable to impute actual—not just potential—formal-sector work experience in years.⁷

Sample Selection. We select workers between the ages of 18 and 54 earning at least the federal minimum wage. For each worker-year combination, we keep the highest paid among all longest employment spells. We then iteratively drop singleton observations defined by gender-employer combinations and worker identifiers. We also impose a minimum employer size threshold of 10 non-singleton workers—i.e., workers who are observed at least one more time at a future date.⁸ Finally, we require that employers appear in our sample in at least four out of the eight years. Together, these selection criteria leave us with a set of reasonably large and stable employers for which pay policies can be credibly estimated with minimal limited-mobility bias.⁹ In order to separately identify worker and employer pay components as well as employer ranks based on worker flows, we focus on observations in the largest strongly connected set, which requires flows into and out of all employers in the set. Our selection criteria do not substantially alter the raw gender pay gap.

Summary Statistics. Table 1 presents summary statistics on our final sample.¹⁰ The pooled sample comprises 267.3 million worker-years, including 56.3 million unique workers and 607.0 thousand

⁷The distinction between actual and potential experience is important given Brazil’s sizable informal sector, as shown in Figure A.1 in Appendix A.1, though gender differences are small and thus explain little of the empirical gender pay gap.

⁸While the RAIS data cover only Brazil’s formal sector, the employer size restriction implies that the vast majority of informal employers would in any case be excluded from our analysis (Ulyssea, 2018; Dix-Carneiro et al., 2021).

⁹See also Andrews et al. (2008, 2012), Kline et al. (2020), Borovičková and Shimer (2020), and Bonhomme et al. (2023).

¹⁰Appendix A.2 compares summary statistics based on the raw data (Appendix Table A.1), the selected sample (Appendix Table A.2), the connected set (Appendix Table A.3), and comparisons between them (Appendix Tables A.4–A.5).

unique employers. Around 38.2% of these observations are for women who are more likely to be White, more educated, older, work at significantly larger employers, work shorter hours, and have longer tenure. Importantly, the raw gender pay gap in our sample is 13.3 log points.

Table 1. Summary statistics, 2007–2014

	Overall	Men	Women
Mean log real monthly earnings (std. dev.)	7.211 (0.693)	7.262 (0.697)	7.129 (0.679)
Mean years of education (std. dev.)	11.1 (3.3)	10.4 (3.3)	12.1 (2.9)
Mean years of age (std. dev.)	33.6 (9.4)	33.5 (9.4)	33.8 (9.4)
Mean employer size (std. dev.)	2,815 (16,418)	1,774 (11,509)	4,497 (22,059)
Mean contractual work hours (std. dev.)	41.7 (5.1)	42.6 (3.9)	40.3 (6.4)
Mean years of tenure (std. dev.)	3.9 (5.6)	3.6 (5.2)	4.5 (6.1)
Share Nonwhite	0.378	0.409	0.327
Share female	0.382		
Mean log gender earnings gap	0.133		
Number of worker-years	267,318,328	165,149,632	102,168,696
Number of unique workers	56,297,308	33,761,656	22,535,652
Number of unique employers	607,029	403,585	203,444

Note: This table reports summary statistics for workers in the final sample, separately for the overall population, for men only, and for women only. Since information on race is missing for a significant number of observations, conditional means are reported for the share of Nonwhite workers. *Source:* RAIS, 2007–2014.

3 Empirical Gender Pay Gaps and Employer Heterogeneity

The goal of this section is to highlight the roles of employer pay heterogeneity, worker sorting across employers, and workplace amenities in relation to the gender pay gap.

3.1 Measuring Gender-Specific Employer Pay

We start by estimating a variant of [Card et al.’s \(2016\)](#) extension of the seminal two-way FE framework due to AKM, which allows for gender-specific employer pay components. Formally, we model log earnings of individual i in year t working at employer $j = J(i, t)$, denoted by $\ln w_{ijt}$, as

$$\ln w_{ijt} = \alpha_i + \psi_{G(i)j} + X_{it}\beta_{G(i)} + \varepsilon_{ijt}, \quad (1)$$

where α_i is a person FE; $\psi_{G(i)j}$ is a gender-specific employer FE for workers of gender $G(i) \in \{M, F\}$; X_{it} is a vector of time-varying worker characteristics including a set of restricted education-age dummies as well as dummies for hours, occupation, tenure, actual experience, and education-year combi-

nations, all subject to gender-specific returns $\beta_{G(i)}$; and ε_{ijt} is a residual.¹¹ By including person FEs, we control for selection of men and women across employers based on time-invariant worker pay characteristics. Our focus lies in the distribution of gender-specific employer FEs ψ_{Mj} and ψ_{Fj} .

Any two-way FEs model requires a normalization of the level of employer FEs relative to person FEs. In our case, the inclusion of gender-specific employer FEs in equation (1) requires two normalizations—one for each gender.¹² In previous work, [Card et al. \(2016\)](#) and [Gerard et al. \(2021\)](#) normalized the FEs of employers in each connected set to have zero mean in the restaurant and fast-food sector, which they argued has a low surplus. However, those papers were concerned only with employer heterogeneity in pay. Our setting with gender-specific amenities and compensating differentials calls for a different normalization of employer FEs, which we derive in [Appendix D.3](#) based on the theoretical framework in [Section 4](#). Guided by our theory, we would like to normalize employer pay for a subset of employers that (i) rank near the bottom in the utility ladder for both genders; (ii) treat men and women as near perfect substitutes in production; and (iii) provide a similar (e.g., close to zero) amenity value to men and women who they employ. We impose condition (i) based on our empirical estimates of revealed-preference ranks derived in [Section 5.3](#). We further assume that workers in the restaurant and fast-food sector satisfy conditions (ii) and (iii), which we think of as a reasonable assumption given the nature of jobs in this sector.

We now turn to our object of interest in equation (1)—namely, the gender-specific employer FEs.¹³ Panel **A** of [Figure 1](#) plots the distribution of employer FEs by gender. The distribution for women has visibly lower mean and lower variance than that for men. Panel **B** of the figure shows the distribution of within-employer differences in FEs for dual-gender employers. The distribution is relatively dispersed compared to its mean of 2.4 log points. Altogether, this evidence suggests that sorting of women into lower-paying employers is a significant source of gender pay differences.

To dissect the structure of pay and the relative contribution of employer heterogeneity, [Table 2](#) presents a variance decomposition of log earnings.¹⁴ Men have a slightly higher variance of earnings,

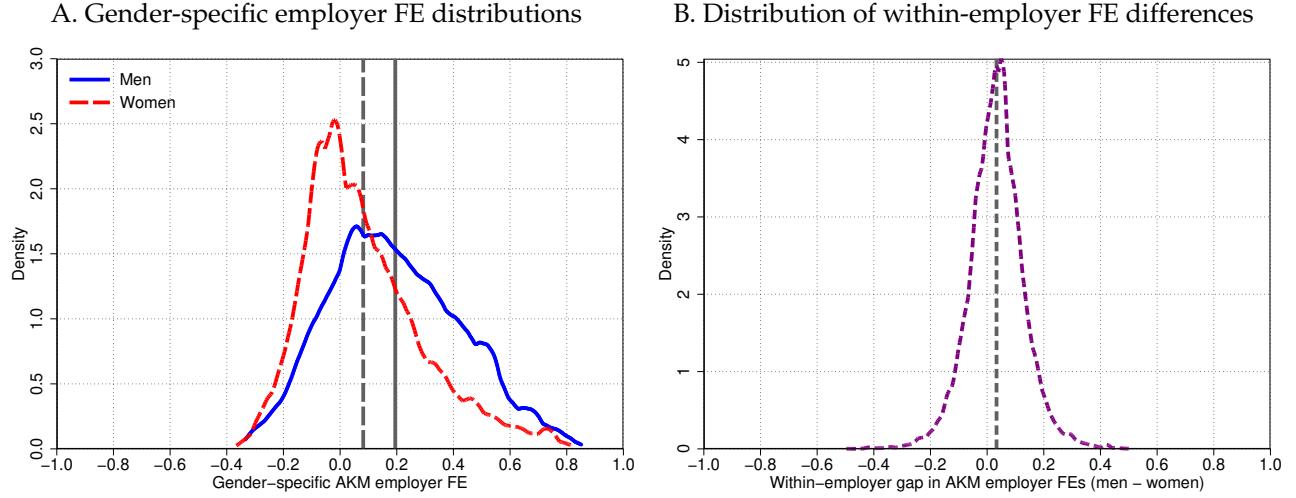
¹¹To simultaneously identify age, time, and worker FEs, we restrict the age-pay profile to be flat around ages 45–49. We view this as an attractive alternative to the approach advocated by [Card et al. \(2018\)](#), since it allows us to verify that our restriction leads to smooth education-age FEs around this age window. See [Appendix Figure B.6](#) for details.

¹²To see this, note that we could transform $\alpha_i \mapsto \alpha_i + k$ and $\psi_{G(i)j} \mapsto \psi_{G(i)j} - k$ for all workers i of a given gender $g = G(i)$, for any constant $k \in \mathbb{R}$, without changing the sum of the components in equation (1).

¹³[Appendix B.1](#) shows auxiliary results relating to the AKM equation, including estimated gender-specific hours FEs ([Figure B.1](#)), occupation FEs ([Figure B.2](#)), actual-experience FEs ([Figure B.3](#)), tenure FEs ([Figure B.4](#)), education-year FEs ([Figure B.5](#)), and education-age FEs ([Figure B.6](#)). Further tests of the log-additivity and exogenous mobility assumptions of similar specifications and data are presented in [Alvarez et al. \(2018\)](#), [Engbom and Moser \(2022\)](#), and [Gerard et al. \(2021\)](#).

¹⁴[Table 2](#) shows results based on the plug-in estimator of the variance components. The alternative leave-one-out estimator by [Kline et al. \(2020\)](#) uses a jackknife correction for limited-mobility bias. Related work by [Engbom and Moser \(2022\)](#) shows that this leave-one-out estimator delivers substantially similar results for a sample of men in the same RAIS data

Figure 1. Predicted AKM employer FEs for women and men



Note: This figure shows kernel density plots of estimated gender-specific employer FEs based on estimating earnings equation (1). Panel A shows the distributions of gender-specific employer FEs ψ_{gj} separately by gender. Panel B shows the distribution of within-employer FE differences $\psi_{Mj} - \psi_{Fj}$ weighted by total employment. Vertical patterned lines show the means of the respective distributions. Source: RAIS, 2007–2014.

with 51.0 log points, compared to 49.6 log points for women. For both genders, the largest variance component is due to estimated worker FEs, which account for 23.5% for men and 24.9% for women. In terms of the variance components, employer FEs account for 12.5% of the variance of log earnings for men and 11.1% of that for women. In terms of the covariance components, the relative importance of employer FEs is slightly larger, with the covariance between employer FEs and log earnings explaining around 21.8% of total earnings variation for men, and around 20.1% for women. Overall, these estimates suggest that employer heterogeneity explains a substantial share of earnings dispersion for both genders. The correlation between person and employer FEs is around 22.1% for men and 26.2% for women. Finally, the model explains upward of 92.3% of the variation in log earnings.

3.2 Gender Differences in Sorting Across Employer Pay and Amenities

A Kitagawa-Oaxaca-Blinder decomposition allows us to write the gender gap in employer FEs as

$$\underbrace{\left(\mathbb{E}_{i,t} \left[\psi_{Mj(i,t)} \middle| G(i) = M \right] - \mathbb{E}_{i,t} \left[\psi_{Mj(i,t)} \middle| G(i) = F \right] \right)}_{\text{between-employer gap}} + \underbrace{\mathbb{E}_{i,t} \left[\psi_{Mj(i,t)} - \psi_{Fj(i,t)} \middle| G(i) = F \right]}_{\text{within-employer gap}}. \quad (2)$$

from Brazil. A previous version of this paper (Morchio and Moser, 2021) demonstrated that the estimation results are stable across a range of sample restrictions designed to ease the threat of limited-mobility bias. For a discussion of limited-mobility bias and alternative approaches, see Bonhomme et al. (2019), Borovičková and Shimer (2020), and Bonhomme et al. (2023).

Table 2. Variance decomposition based on gender-specific employer FEs model

Variances	Men		Women	
	Level	Share (%)	Level	Share (%)
Variance of log earnings	0.510		0.496	
Variance components of log earnings:				
Person FEs	0.120	23.5	0.124	24.9
Employer FEs	0.064	12.5	0.055	11.1
Covariance components of log earnings:				
Person FEs	0.142	27.9	0.158	31.8
Employer FEs	0.111	21.8	0.100	20.1
Correlation between person and employer FEs	0.221		0.262	
R^2	0.923		0.931	
Mean employer FE	0.195		0.082	

Note: This table shows the variance and covariance components of log earnings based on equation (1). The variance components correspond to the variance decomposition $Var(\ln w_{ijt}) = Var(\alpha_i) + Var(\psi_{G(i)j}) + Var(X_{it}\beta_{G(i)}) + 2\sum Cov(\cdot) + Var(\varepsilon_{ijt})$. The covariance components correspond to the covariance decomposition $Var(\ln w_{ijt}) = Cov(\alpha_i, \ln w_{ijt}) + Cov(\psi_{G(i)j}, \ln w_{ijt}) + \sum Cov(\cdot) + Cov(\varepsilon_{ijt}, \ln w_{ijt})$. *Source:* RAIS, 2007–2014.

Equation (2) decomposes the gender gap in employer FEs into two terms. The *between-employer pay gap* is the gender-weighted difference in mean male-employer FEs. It reflects differences in pay between men and women that are due to their different allocations across employers. The *within-employer pay gap* is the mean difference in gender-specific employer FEs weighted by the distribution of women. It reflects differences in pay between women and men at the same employer.¹⁵

Results from the decomposition in equation (2) are shown in Table 3. Out of the total gender pay gap in employer FEs of 11.3 log points, a majority share of 78.7% is attributed to the between-employer pay gap. This suggests that women, compared to men, systematically work at lower-paying employers and that gender-specific sorting accounts for most of the gender pay gap.¹⁶

Table 3. Kitagawa-Oaxaca-Blinder decompositions of the gender gap in employer FEs

Gender gap in employer FEs	Between-employer gap		Within-employer gap	
	Level	Share (%)	Level	Share (%)
0.113	0.089	78.7	0.024	21.3

Note: This table shows results from the Kitagawa-Oaxaca-Blinder decomposition of the gender gap in employer FEs into a between-employer gap and a within-employer gap. The decomposition corresponds to equation (2) and uses women's employer FEs for computing the between-employer component. An alternative decomposition using men's employer FEs for computing the between-employer component is presented in Table B.1 in Appendix B.2. *Source:* RAIS, 2007–2014.

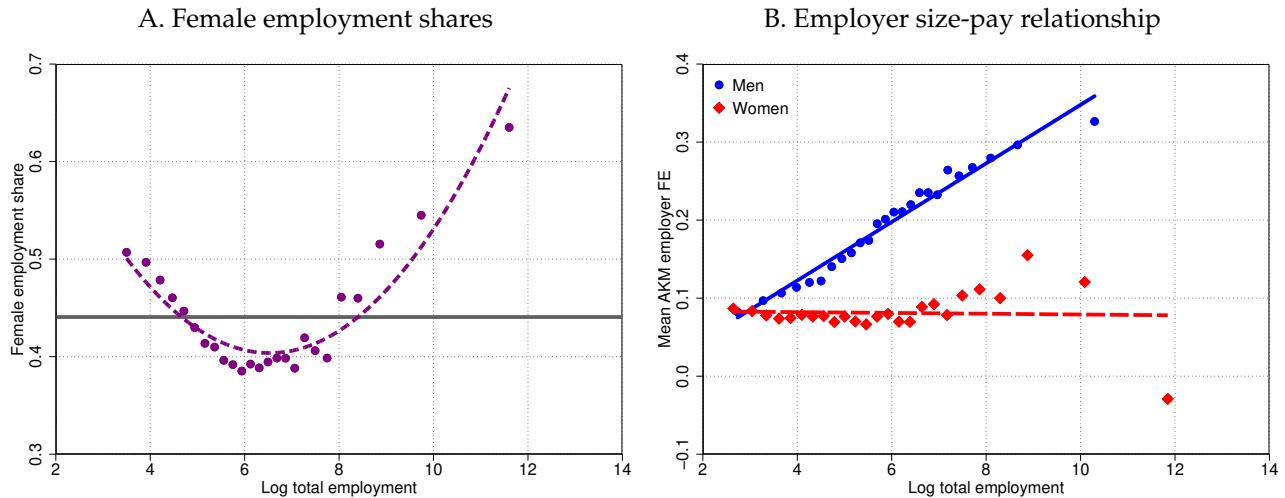
¹⁵To see that the between-employer gap is invariant to the normalization of gender-employer FEs, note that for any $k \in \mathbb{R}$, $\mathbb{E}_{i,t}[\psi_{gJ(i,t)} + k | G(i) = M] - \mathbb{E}_{i,t}[\psi_{gJ(i,t)} + k | G(i) = F] = \mathbb{E}_{i,t}[\psi_{gJ(i,t)} | G(i) = M] - \mathbb{E}_{i,t}[\psi_{gJ(i,t)} | G(i) = F]$ for $g \in \{M, F\}$. The within-employer gap, on the other hand, depends on the normalization of gender-employer FEs, as discussed in the text.

¹⁶An alternative decomposition using men's employer FEs for computing the between-employer component is presented in Appendix Table B.1. Appendix Figure B.7 illustrates the estimates underlying the two decompositions.

Where do women work? Panel A of Figure 2 shows substantial heterogeneity in female shares across employers, with women disproportionately represented at the largest employers. Heterogeneity in female employment shares may partly reflect women valuing certain employers differently than men. While there are many causes behind gendered sorting across employers, our focus lies on labor-demand-side factors. Specifically, we are interested in the extent to which both pay and nonpay employer attributes contribute toward observed sorting and the associated gender pay gap.¹⁷

To shed light on the gendered sorting across employers, we examine the employer size-pay relationship by gender in Panel B of Figure 2. As expected, employer pay is increasing in size for men. Strikingly, however, this pattern looks very different for women. For them, pay is flat across employer sizes. Furthermore, the coefficient of determination (R^2) from a regression of estimated employer FEs on flexible employer size categories is 3.3% for men and only 0.1% for women. This suggests that considerations other than pay may be driving women's, and possibly also men's, employer choices.

Figure 2. Female employment shares and gender-specific pay across employer sizes



Note: Panel A of this figure shows a binned scatter plot of female employment shares across employer sizes, with the curved purple dashed line indicating the quadratic best fit and the horizontal grey solid line indicating the mean female employment share. Panel B of this figure shows binned scatter plots of mean AKM employer FEs across log total (i.e., male plus female) employment separately by gender. The linear best fit lines in solid blue for men and in dashed red for women are weighted by gender-specific employment. Source: RAIS, 2007–2014.

If not pay, what drives the allocation of women across employers? To answer this question, we

¹⁷Clearly, labor-supply-side factors could be important. To address the role of child penalties, in Appendix B.3, we study life-cycle patterns of employer pay by gender and parental status. In Appendix B.4, we conduct an event study analysis around childbirth, following the methodology in Kleven et al. (2019). While we find significant gender gaps in participation and earnings associated with childbirth, our analysis suggests that childbirth is *not* a very important factor behind gender gaps in *employer pay* in Brazil. Nevertheless, we allow for gender differences in labor market attachment and job mobility in our structural analysis. Our framework is flexible enough to allow for the separate analysis of more granular population subgroups, for example different education groups or worker groups split by parental status.

project measures of workplace amenities on indicators for workers' gender, log employer size, and their interaction. Table 4 shows our estimation results for each of six amenity proxies. We find that women at large employers are more likely to work part time but less likely to be exposed to workplace hazards, fired for unjust reasons, and at risk of dying in work accidents. Women are also significantly more likely to congregate at employers with relatively generous parental leave policies, although those employers are not especially large in size. Finally, the R^2 coefficients are substantial and women tend to enjoy greater amenities on average compared to men. In summary, these results suggest that women at larger employers enjoy more amenities, which are presumably valued over and above pay.

Table 4. Workplace amenities by gender and employer size

	(1) Part-time	(2) Flexibility	(3) Parental	(4) Hazards	(5) Firings	(6) Deaths
Female	−0.045*	0.002	1.054***	0.129***	−0.002	0.005***
(std. err.)	(0.023)	(0.006)	(0.075)	(0.028)	(0.010)	(0.001)
Log size	0.006	−0.001*	0.028***	0.011	−0.012**	0.001***
(std. err.)	(0.005)	(0.001)	(0.004)	(0.010)	(0.005)	(0.000)
Female \times log size	0.015***	0.001	−0.040***	−0.013***	−0.005***	−0.002***
(std. err.)	(0.004)	(0.001)	(0.013)	(0.005)	(0.002)	(0.000)
R^2	0.557	0.377	0.712	0.176	0.516	0.267
Mean for men	0.094	0.030	0.085	0.170	0.559	0.008
Mean for women	0.230	0.053	0.893	0.211	0.429	0.005

Note: This table reports estimates from regressing various amenity proxies on indicators for workers' gender, log employer size, and their interaction. All estimates are conditional on municipality and sector FEs. Details of the dependent variables referenced in the headers of columns (1)–(6) are presented in Appendix E.3. Standard errors are clustered at the employer level. ***, **, and * denote significance at the 1%, 5%, and 10% levels, respectively. *Source:* RAIS, 2007–2014.

4 Equilibrium Model of Employer Pay, Amenities, and Size

In this section, we develop an equilibrium search model based on the seminal framework by [Burdett and Mortensen \(1998\)](#) to reconcile our empirical findings that women work at lower-paying firms, have a lower firm size-pay premium, and enjoy more amenities than men.

4.1 Workers

Workers are infinitely lived, risk neutral, and discount the future at rate ρ . They differ in their gender $g \in \{M, F\}$ and ability $z > 0$, with measure μ_{gz} such that $\sum_g \int_z \mu_{gz} dz = 1$. Given a consumption stream x , a worker of type (g, z) receives flow *felicity* $\mathcal{U}_{gz}(x) = \omega_{gz}^0 + \omega_{gz}^1 x$, where $\mathcal{U}_{gz}(\cdot)$ is an affine

function with worker type-specific intercept parameter $\omega_{gz}^0 \in \mathbb{R}$ and slope parameter $\omega_{gz}^1 > 0$.¹⁸

Job Search. Workers find themselves either nonemployed or employed.¹⁹ While nonemployed, workers receive flow consumption $x = b_{gz}$ and engage in random job search within labor markets segmented by worker type. Search is random in the sense that workers cannot direct their search to specific firms. Labor markets are segmented in the sense that workers search for jobs in a market specific to their type. While employed, workers receive flow consumption $x = w + a$ consisting of their wage, $w > 0$, and job amenity value, $a > 0$. Employed workers also engage in on-the-job search.

Workers receive job offers at rate λ_{gz}^U from nonemployment and at rate λ_{gz}^E from employment. While those job offers admit free disposal, at rate λ_{gz}^G workers also receive involuntary job offers. We think of the latter as capturing, among other things, spousal relocation problems and other idiosyncratic reasons for switching jobs. We write $\lambda_{gz}^E = s_g^E \lambda_{gz}^U$ and $\lambda_{gz}^G = s_g^G \lambda_{gz}^U$, where s_g^E and s_g^G are the relative hazards of voluntary and involuntary on-the-job offers, which are fixed separately by gender.

A job offer is an opportunity to work at a firm with wage w and amenity a . Since workers rank firms according to flow utility $x = w + a$, their decisions depend only on the flow-utility offer distribution $F(x)$. Jobs are endogenously terminated when a worker with flow utility x accepts a higher-utility job at rate $\lambda_{gz}^E(1 - F(x))$ and exogenously terminated either when the worker relocates to a randomly drawn job at rate λ_{gz}^G or when the worker moves into nonemployment at rate δ_g .

Value Functions. The value of an employed worker of type (g, z) in a job with flow utility x is

$$\begin{aligned} \rho S_{gz}(x) = x + \lambda_{gz}^E \int_{x' \geq x} [S_{gz}(x') - S_{gz}(x)] dF_{gz}(x') + \lambda_{gz}^G \int_{x'} [S_{gz}(x') - S_{gz}(x)] dF_{gz}(x') \\ + \delta_g [W_{gz} - S_{gz}(x)]. \end{aligned} \quad (3)$$

Analogously, the value of a nonemployed worker of type (g, z) is given by

$$\rho W_{gz} = b_{gz} + (\lambda_{gz}^U + \lambda_{gz}^G) \int_{x'} \max \{S_{gz}(x') - W_{gz}, 0\} dF_{gz}(x'). \quad (4)$$

¹⁸Without loss of generality, we set $\omega_{gz}^0 = 0$ and $\omega_{gz}^1 = 1$, so we interchangeably refer to x as flow consumption or utility. We return to the general parameterization in Section 5.7, where we discuss what components of $\mathcal{U}_{gz}(x)$ we can (not) identify.

¹⁹Throughout the paper, we think of “nonemployed” workers in the model as capturing real-world workers who are not formally employed—that is, those who are unemployed, on temporary parental or other leave, marginally attached to the labor force, or in informal employment. When mapping the model to the data, our estimation of labor market parameters will take into account that some workers might spend longer periods outside of formal employment because of these factors.

Policy Functions. Strict monotonicity of $S_{gz}(x)$ implies that optimal job acceptance of the nonemployed follows a threshold rule with reservation flow utility ϕ_{gz} . A nonemployed worker accepts an offer if $x \geq \phi_{gz}$ and rejects it otherwise. The reservation flow utility simply equals the sum of the flow utility in nonemployment plus the forgone option value of receiving job offers while nonemployed:

$$\phi_{gz} = b_g z + (\lambda_{gz}^U - \lambda_{gz}^E) \int_{x' \geq \phi_{gz}} \frac{1 - F_{gz}(x')}{\rho + \delta_g + \lambda_{gz}^G + \lambda_{gz}^E [1 - F_{gz}(x')]} dx'. \quad (5)$$

Employed workers in a job with flow utility x simply accept any job that delivers flow utility $x' > x$.

Nonemployment. The steady-state nonemployment rate for each worker type is

$$u_{gz} = \frac{\delta_g}{\delta_g + \lambda_{gz}^U + \lambda_{gz}^G}. \quad (6)$$

Utility Dispersion. The cross-sectional distribution of flow utilities for each worker type is

$$G_{gz}(x) = \frac{F_{gz}(x)}{1 + \kappa_{gz}^E [1 - F_{gz}(x)]}, \quad (7)$$

where $\kappa_{gz}^E = \lambda_{gz}^E / (\delta_g + \lambda_{gz}^G)$ governs the effective speed of climbing the firm ladder in utility space.

4.2 Firms

Firms differ in three dimensions: *productivity* $p > 0$ as in [Burdett and Mortensen \(1998\)](#), a set of *gender wedges* $\tau_g \in \mathbb{R}$ representing the firm's disutility from employing workers of each gender g , as in [Becker \(1971\)](#), and a set of *amenity cost shifters* $c_g^{a,0} > 0$ for each gender g , as in [Hwang et al. \(1998\)](#). Thus, a firm's type is $(p, \{\tau_g\}_g, \{c_g^{a,0}\}_g)$, which we assume is continuously distributed according to $\Gamma(\cdot)$.

Wages, Amenities, and Vacancies. Firms deliver value through wages w_{gz} and amenities a_{gz} .²⁰ The cost of providing amenities is paid per worker, as in [Hwang et al. \(1998\)](#), and of the following form:

$$c_{gz}^a(a) = c_g^{a,0} \frac{(a/z)^{\eta^a}}{\eta^a} z, \quad (8)$$

where the amenity cost shifter, $c_g^{a,0}$, varies at the gender-firm level and η^a is the economy-wide amenity cost elasticity. This formulation is consistent with amenities being provided as piece rates relative to

²⁰Appendix C.5 presents an alternative model, in which firms produce an amenity vector with gender-specific utility weights, and establishes conditions for *observational equivalence* and *counterfactual equivalence* between the two models.

worker ability z , as is the case for parental leave policies and paid time off. To recruit workers and produce output, firms post v_{gz} job vacancies in each market subject to flow cost

$$c_{gz}^v(v) = c_g^{v,0} \frac{v^{\eta^v}}{\eta^v} z, \quad (9)$$

where η^v is the economy-wide vacancy cost elasticity and the vacancy cost shifter $c_g^{v,0}$ varies by gender. This formulation is consistent with recruiting costs being denominated either in terms of new recruits' time used for onboarding or in terms of equally skilled incumbent workers' time spent on recruiting.

Production. A firm with productivity p employing $\{l_{gz}\}_{gz}$ workers of each type produces output

$$y(p, \{l_{gz}\}_{gz}) = p \sum_{g=M,F} \int_a z l_{gz} dz. \quad (10)$$

Gender Wedges. We entertain the possibility that employers have preferences over workers' gender captured by employer-specific gender wedges $\{\tau_g\}_g$. Two popular theories that map into this gender wedge include taste-based discrimination, as in [Becker \(1971\)](#), and firm-level comparative advantages in production, as in [Goldin \(1992\)](#). Without loss of generality, we normalize $\tau_g = \tau \mathbf{1}[g = F]$, where $\tau \in \mathbb{R}$ is the implicit tax rate on employing women relative to that on men.

Value Function. In summary, firms post wages, amenities, and vacancies in each market to maximize steady-state flow payoff. The value $\Pi(\cdot)$ of a firm of type $(p, \tau_g, \{c_g^{a,0}\}_g)$ is given by

$$\rho \Pi(\cdot) = \max_{\{w_{gz}, a_{gz}, v_{gz}\}_{gz}} \left\{ \sum_{g=M,F} \int_z \left[(1 - \tau_g) p z - w_{gz} - c_{gz}^a(a_{gz}) \right] l_{gz}(w_{gz}, a_{gz}, v_{gz}) - c_{gz}^v(v_{gz}) dz \right\}. \quad (11)$$

4.3 Matching

The effective mass of job searchers and total mass of vacancies in market (g, z) are given by

$$U_{gz} = \mu_{gz} \left[u_{gz} + s_g^E (1 - u_{gz}) + s_g^G \right], \quad V_{gz} = \int_j v_{gz}(j) d\Gamma(j), \quad \forall (g, z). \quad (12)$$

A Cobb-Douglas matching function with constant returns to scale combines the mass of job searchers with the mass of vacancies to produce $m_{gz} = \chi_g V_{gz}^\alpha U_{gz}^{1-\alpha}$ matches between workers and firms, where

$\chi_g > 0$ is the matching efficiency and $\alpha \in (0, 1)$ is the matching elasticity. Labor market tightness is

$$\theta_{gz} = \frac{V_{gz}}{U_{gz}}, \quad \forall (g, z). \quad (13)$$

The job-finding rates among nonemployed workers, λ_{gz}^U , the voluntary job offer rates among the employed, λ_{gz}^E , the involuntary job offer rates, λ_{gz}^G , and firms' job-filling rates, q_{gz} , are given by

$$\lambda_{gz}^U = \chi_g \theta_{gz}^\alpha, \quad \lambda_{gz}^E = s_g^E \lambda_{gz}^U, \quad \lambda_{gz}^G = s_g^G \lambda_{gz}^U, \quad \text{and} \quad q_{gz} = \chi_g \theta_{gz}^{\alpha-1}, \quad \forall (g, z). \quad (14)$$

4.4 Firm Size Distribution

The following Kolmogorov forward equation describes employment's law of motion given a firm's flow-utility and vacancy policies (x, v) , the offer distribution $F_{gz}(x)$, and tightness θ_{gz} in market (g, z) :

$$l_{gz}(x, v) = \left[-\delta_g - \lambda_{gz}^G - \lambda_{gz}^E [1 - F_{gz}(x)] \right] l_{gz}(x, v) + \left[\frac{u_{gz} + (1 - u_{gz})s_g^E G_{gz}(x) + s_g^G}{u_{gz} + (1 - u_{gz})s_g^E + s_g^G} \right] v q_{gz}. \quad (15)$$

Solving for the stationary employment distribution in each market (g, z) , firm sizes are given by

$$l_{gz}(x, v) = \left(\frac{1}{\delta_g + \lambda_{gz}^G + \lambda_{gz}^E [1 - F_{gz}(x)]} \right)^2 \frac{v}{V_{gz}} \mu_{gz} (u_{gz} + s_g^G) \lambda_{gz}^U (\delta_g + \lambda_{gz}^G + \lambda_{gz}^E). \quad (16)$$

4.5 Equilibrium Characterization

Appendix C.1 defines a *stationary equilibrium* of the economy. The combination of market segmentation and output being additive across worker types keeps this problem tractable by allowing us to divide the firm's problem into separate subproblems across markets. In market (g, z) , a firm offering wage w_{gz} and amenities a_{gz} finds itself ranked on a firm ladder according to flow utility $x_{gz} = w_{gz} + a_{gz}$. Next, we provide comparative statics results for firms' optimal policy functions.

Lemma 1 (Optimal Amenities). *A firm's optimal amenity policy function $a_{gz}^*(\cdot)$ is linear in worker ability z , strictly decreasing in its amenity cost shifter $c_g^{a,0}$, and invariant to all other firm parameters (i.e., p and τ_g). In equilibrium, $a_{gz}^*(c_g^{a,0}, z) = (c_g^{a,0})^{1/(1-\eta^a)} z$.*

Proof. See Appendix C.2. □

Due to their convex-increasing per-worker cost, amenities are offered by firms up to the point where the marginal cost of amenities equals that of wages, which is one. While amenities are endoge-

uously produced, Lemma 1 allows us to treat *composite productivity*,

$$\tilde{p}_{gz} \equiv (1 - \tau_g) p z + a_{gz}^*(c_g^{a,0}) - c_{gz}^a(a_{gz}^*(c_g^{a,0})), \quad (17)$$

which incorporates productivity p , the gender wedge τ_g , and the optimized amenity value $a_{gz}^*(c_g^{a,0})$ net of amenity costs $c_{gz}^a(a_{gz}^*(c_g^{a,0}))$, as a firm characteristic. Thus, we can rewrite the firm's problem as

$$\rho \Pi_{gz}(\tilde{p}_{gz}) = \max_{x,v} \left\{ [\tilde{p}_{gz} - x] l_{gz}(x, v) - c_{gz}^v(v) \right\}, \quad \forall (g, z). \quad (18)$$

Therefore, our model is isomorphic to one without amenities or gender wedges but with productivity p being replaced by composite productivity \tilde{p} and wages w being replaced by flow utility x .²¹

Lemma 2 (Optimal Vacancies). *Keeping fixed all other parameters, a firm's optimal vacancy policy $v_{gz}^*(\cdot)$ is strictly increasing in composite productivity \tilde{p}_{gz} and, thus, strictly increasing in productivity p , strictly decreasing in the gender wedge τ for women, and strictly decreasing in the amenity cost shifter $c_g^{a,0}$.*

Proof. See Appendix C.3. □

The intuition behind Lemma 2 is that more profitable firms benefit more from each worker contact.

Lemma 3 (Optimal Flow Utility and Wages). *Keeping fixed all other parameters, a firm's optimal flow utility offer $x_{gz}^*(\cdot)$ is strictly increasing in composite productivity \tilde{p}_{gz} and, thus, strictly increasing in productivity p for all worker types, strictly decreasing in the gender wedge τ for women, and strictly decreasing in the amenity cost shifter $c_g^{a,0}$. A firm's optimal wage offer $w_{gz}^*(\cdot)$ is strictly increasing in productivity p for all worker types and strictly decreasing in the gender wedge τ for women.*

Proof. See Appendix C.4. □

Lemma 3 extends well-known comparative statics results for wages (e.g., Bontemps et al., 1999, 2000) to a richer environment with both wages and amenities. Intuitively, firms with a greater payoff from employment optimally offer higher flow utility in order to attract and retain more workers.

4.6 Equilibrium Properties

Our model has several notable equilibrium properties. First, search frictions give rise to gender-specific monopsony power (Robinson, 1933) across firms, which results in utility dispersion both

²¹See Mortensen (2003) and Engbom and Moser (2022) for examples of such a model.

within and across genders.²² Search frictions imply that low- and high-utility firms coexist and relocation towards higher-utility firms is sluggish. As a result, both gendered sorting between firms and unequal treatment of men and women within firms depend on the severity of search frictions.

Second, observed wage differences are neither necessary nor sufficient for the existence of utility differences. Two firms can offer the same wage $w = w'$ but different utility $x \neq x'$ if $a \neq a'$. Conversely, two firms can offer different wages $w \neq w'$ but the same utility $x = x'$ if $a' = a + w - w'$. The competitive environment determines the extent to which amenities are priced into wages, giving rise to compensating differentials (Rosen, 1986). Consequently, gender pay gaps in the data may either underestimate or overstate inequality in utility, the measurement of which requires a structural model.

Third, the model rationalizes job-to-job transitions with wage declines through two channels. A worker may voluntarily transition from a job with wage-amenity combination (w, a) to one with (w', a') and $w' < w$ if $x' > x$. In addition, a worker may involuntarily transition from a job offering (w, a) to a randomly drawn job (w', a') with $w' < w$, regardless of $x' \leq x$.

Fourth, firms have multiple levers to discriminate between genders—wages w , amenities a , and vacancies v . Firms choose these levers to maximize the payoff given their productivity p , gender-specific amenity cost shifters $c_g^{a,0}$, and preferences over gender τ , as well as the general competitive environment. Thus, gender gaps in pay, amenities, and employment are all jointly determined.

Fifth, what is a high-paying, high-amenity, or large employer may differ across genders. While we naturally expect pay, amenities, and size to be correlated within an employer across genders, our model allows these characteristics to differ freely, so men and women climb separate firm ladders.

Sixth, even nondiscriminatory firms (i.e., those with $\tau = 0$ and $c_M^{a,0} = c_F^{a,0}$) may treat women differently than men due to the presence of other discriminatory firms (i.e., those with $\tau \neq 0$, as in Becker, 1971, or $c_M^{a,0} \neq c_F^{a,0}$). On-the-job search leads profit-maximizing firms to account for other employers' characteristics when making their own equilibrium decisions. In this sense, our model features “discrimination” spillovers arising from strategic links throughout the distribution of firms.²³

²²By search frictions, here we refer to the combination of the vacancy cost shifter $c_g^{v,0} > 0$, the relative hazard of voluntary on-the-job offers $s_g^E < \infty$, the relative hazard of involuntary on-the-job offers $s_g^G > 0$, and the separation hazard $\delta > 0$.

²³Black (1995) studies a related phenomenon with degenerate wage distributions, while Flabbi (2010) considers spillovers through gender-specific values of unemployment without on-the-job search. Relatedly, Caldwell and Harmon (2019) and Caldwell and Danieli (2023) show that workers' outside employment opportunities affect current employment outcomes.

4.7 Discussion of Model Assumptions

We now discuss some of our more restrictive modeling assumptions and their implications—see Appendix C.6 for details. First, that output is linear within worker types is arguably not particularly restrictive, since a firm’s profit function is already concave due to convex vacancy costs.

Second, labor market segmentation allows firms to tailor wages, amenities, and vacancies to each market, which we view as a modeling device to match the empirical gender segregation across employers together with observed differences in pay and amenity utilization even within employers.²⁴

Third, while our model allows for gender differences in labor market flow rates, we do not take into account workers’ family status. This simplifying assumption is grounded in the empirical evidence in Appendix B.4. Furthermore, women may be treated differently by employers even before childbirth in anticipation of future fertility events.²⁵

Fourth, we have paid special attention to gender differences while abstracting from labor demand or supply factors within genders. However, our framework is more general than its application to gender, as it can be applied to set of population groups indexed by g , which could be either observed (e.g., parental status, education, race) or inferred in a pre-estimation step (e.g., k -means clustering on observables, as in Bonhomme et al., 2019, 2022). This makes our model a flexible tool for studying employer heterogeneity in pay, amenities, and employment across population groups.

5 Identification

To operationalize our model, we provide a constructive proof of identification of all model parameters based on linked employer-employee data. From a bird’s eye view, we leverage the intuition that firms’ unobserved surplus, consisting of productivity and amenity values net of wage and amenity costs, can be inferred from the employer size distribution. To anticipate our findings, our model rationalizes the observation of a highly skewed employment distribution plus substantial pay dispersion conditional on firm surplus through sizable compensating differentials due to employer amenities.

Our identification proof takes as given three exogenous parameters and proceeds in five steps.

²⁴For robustness, we relax the assumption of market segmentation by solving three alternative models, which yield salient counterfactual predictions. A model with firms offering a single wage for men and women fails to account for the empirical within-firm pay differences documented in section 3.1. A model in which amenity values are the same across genders within a firm counterfactually predicts no dispersion in firm ranks conditional on gender-specific pay, while one in which firms produce an amenity vector with gender-specific utility weights is discussed in Appendix C.5. Finally, a model in which vacancies are gender-neutral, as in Appendix C.7 fails to account for the empirical dispersion of female employment shares and hence the between-employer pay gap in the data.

²⁵It would be straightforward to estimate our model separately for ever-parent and never-parent workers.

5.1 Exogenous Parameters

There are three exogenously set parameters in our framework. First, the discount rate $\rho = 0.051$ corresponds to an annual compound real interest rate of 5.3%. The choice of this parameter value is innocuous as it affects only our computation of the flow value of nonemployment. Second, we impose a common normalization of the matching efficiency $\chi_g = 1$ for both genders g . This is without loss of generality since Proposition 5 really identifies the vacancy cost shifter $c_g^{v,0}$ relative to the matching efficiency χ_g , which is all that matters for our purposes.²⁶ Third, the elasticity of the matching function $\alpha = 0.5$ is an agreed-upon value in the literature—see, for example, [Petrongolo and Pissarides \(2001\)](#), [Hall and Milgrom \(2008\)](#), and [Engbom and Moser \(2022\)](#).

5.2 Step 1: Gender-Specific Firm Pay

In the first step, we demonstrate that our equilibrium model provides a microfoundation for the decomposition of log wages into worker FEs and gender-specific employer FEs in [Card et al.'s \(2016\)](#) variant of the original framework due to AKM, on which our analysis in Section 3.1 builds.

Proposition 1 (Equilibrium Wage Equation). *The equilibrium wage of a worker of gender g and ability z at a firm with composite productivity \tilde{p}_g and amenity cost shifter $c_g^{a,0}$ is*

$$\ln w_{gz}(\tilde{p}_g, c_g^{a,0}) = \underbrace{\alpha_z}_{\text{"worker wage FE"}} + \underbrace{\psi_g^w(\tilde{p}_g, c_g^{a,0})}_{\text{"gender-firm wage FE"}}, \quad (19)$$

where

$$\alpha_z = \ln z, \quad (20)$$

$$\psi_g^w(\tilde{p}_g, c_g^{a,0}) = \ln \left(\tilde{p}_g - a_g^*(c_g^{a,0}) - \int_{\tilde{p}' \geq \phi_g}^{\tilde{p}_g} \left[\frac{1 + \kappa_g^E [1 - F_g(x_g^*(\tilde{p}_g))]}{1 + \kappa_g^E [1 - F_g(x_g^*(\tilde{p}'))]} \right]^2 d\tilde{p}' \right). \quad (21)$$

Proof. See Appendix D.1. □

Proposition 1 shows that equilibrium wages in the model are log-additive between a worker component and a gender-specific firm component, as in [Card et al.'s \(2016\)](#) variant of the framework originally due to AKM. The worker wage FE α_z is a strictly monotonic transformation of worker ability

²⁶To separately identify the match efficiency χ_g would require observing the total number of vacancies in the economy.

z. The gender-firm wage FE $\psi_g^w(\tilde{p}_g, c_g^{a,0})$ depends only on gender-firm-specific parameters—namely, a firm’s composite productivity \tilde{p}_g and its amenity cost shifter $c_g^{a,0}$.

In [Card et al. \(2016\)](#), the interpretation of gender-firm FEs was one of gender-specific rent sharing. In contrast, our interpretation allows for both gender-specific rent sharing and compensating differentials. Gender-specific rent sharing is captured by the function $\psi_g^w(\cdot)$, which depends on gender-specific monopsony power. Compensating differentials shape equilibrium wage offers through two channels. First, directly, by substituting for a given firm’s wage payments—see the term $\tilde{p}_g - a_g^*$ in equation (21). Second, indirectly, by shaping the degree of competition between firms—see the integral term involving $x_g^*(\tilde{p}_g)$ in equation (21). Therefore, our equilibrium model lends itself to reinterpreting the wage equation with gender-specific employer pay components, as in [Card et al. \(2016\)](#).

Proposition 6 in Appendix D.3 shows how to impose a model-consistent normalization of firm pay across genders, used in our empirical analysis in Section 3.1, by extending the arguments in [Card et al. \(2016\)](#) to our environment with gender-specific amenities and compensating differentials.

In Appendix D.2, we demonstrate that equilibrium amenities also have a log-additive structure, $\ln a_{gz}(c_g^{a,0}) = \alpha_z + \psi^a(c_g^{a,0})$, where $\alpha_z = \ln z$ is a worker amenity FE and $\psi^a(c_g^{a,0}) = \ln(c_g^{a,0})/(1 - \eta^a)$ is a gender-firm amenity FE. While [Card et al. \(2016\)](#) studied a model of wages akin to equation (19), a formal treatment of amenities and compensating differentials was missing from their analysis. Our framework fills this gap by explicitly modeling firms’ equilibrium wage and amenity choices.

In summary, our model allows us to separate worker from firm components of pay and amenities. As a result, we can abstract from heterogeneity in worker ability when discussing the sources of firm heterogeneity. This rationalizes analogous reduced-form assumptions implicitly made in environments that pool workers for the estimation of firm pay and amenities—see, for instance, [Sorkin \(2017, 2018\)](#). For the remainder of the analysis, we focus on gender-firm components of pay and amenities. This allows us to pool workers in the data, drop ability z from all subscripts in the model, and henceforth treat the gender-firm pay component $w_g \equiv \psi_g^w(\cdot)$ in equation (19) as known.²⁷

5.3 Step 2: Employer Ranks

In the second step, we estimate employer rankings by gender based on a model-consistent revealed-preference argument. For the remainder of this section, we drop the gender subscript g when it is dispensable and refer to firms by their (gender-specific) rank r . For example, we write $w(r)$ for the firm component of wages received by workers of gender g at a firm of rank r .

²⁷Specifically, this allows us to control for gender-specific selection based on ability ([Mulligan and Rubinstein, 2008](#)).

Proposition 2 (Employer Ranks). *All workers of the same gender share a common employer ranking $r \in [0, 1]$, which can be identified from employer sizes $l(r)$.*

Proof. See Appendix D.4. □

Proposition 2 allows us to estimate gender-specific revealed-preference employer ranks. Our rank notion coincides with that of our model in Section 4, in which workers are less likely to endogenously separate from and more likely to accept offers at higher-utility employers, so that higher-ranked employers are larger.²⁸ Of course, there are many other ways to estimate employer ranks in a model-consistent way. One alternative is to exploit the pattern of worker flows between firms, for instance using poaching ranks (Bagger and Lenz, 2019) or a variant of PageRanks (Page et al., 1998; Sorkin, 2018). Appendix D.5 proves that our model is consistent with these alternative firm rank measures.

5.4 Step 3: Labor Market Objects

In the third step, we estimate labor market objects by combining employer ranks from above with information on worker flows between employers as well as between employment and nonemployment. To this end, we exploit the existence of a job ladder across firm utility ranks in our model.

Proposition 3 (Labor Market Objects). *Gender-firm-specific recruiting intensities $f(r)$ and vacancies $v(r)$ as well as gender-specific separation hazards δ , job offer hazards from nonemployment λ^U , involuntary job offer hazards λ^G , voluntary on-the-job offer hazards λ^E , and aggregate vacancies V are identified given employer ranks and data on worker flows between employment states.*

Proof. See Appendix D.6. □

Proposition 3 states that ordinal employer ranks—rather than cardinal utility levels—are sufficient to identify key labor market objects in our model. Given that we have already estimated model-consistent revealed-preference ranks for each gender across firms, the flow pattern of workers between firms as well as between employment and nonemployment pins down the stated objects.

To gain some intuition, consider the identification of the involuntary job offer hazard, λ^G . With data on firm pay alone, this hazard is impossible to identify in our framework. The reason is that wage cuts between employers may be due to any one or a combination of two reasons. First, a worker may voluntarily switch to a higher-utility firm that offers higher utility but a disproportionately higher

²⁸That firms reveal their value (here, match surplus) through labor demand (here, vacancies) is a feature our model shares with a new generation of neoclassical frameworks (Lamadon et al., 2022; Berger et al., 2022; Felix, 2022; Sharma, 2023).

share of it is delivered in the form of amenities, leading to lower wages due to compensating differentials. Second, a worker may switch to a firm that offers lower utility, pay, and amenities due to an involuntary job offer. In contrast, given gender-specific firm ranks already estimated by virtue of Proposition 2 in the previous step, we can infer the involuntary job offer hazard by simply counting the incidence of transitions up versus down the firm ranks at different rungs of the job ladder.

As a result of Proposition 3, going forward we can treat gender-firm-specific recruiting intensities, $f(r)$, and vacancies, $v(r)$, as well as gender-specific separation hazards, δ , job offer hazards from nonemployment, λ^U , involuntary job offer hazards, λ^G , voluntary on-the-job offer hazards, λ^E , and aggregate vacancies, V as known.

5.5 Step 4: Firm-Level Parameters

In the fourth step, we identify gender-specific parameters for each firm. In doing so, we treat as known some economy-wide parameters, the identification of which we discuss next, in Section 5.6.²⁹

We now state an important identification result.

Proposition 4 (Firm-Level Parameters). *The following gender-firm-specific parameters as functions of r are point identified: productivity $p(r)$, the gender wedge $\tau(r)$, and the amenity cost shifter $c^{a,0}(r)$.*

Proof. See Appendix D.7. □

Our identification argument leverages the insight that unobserved firm flow profits per worker can be inferred from equilibrium recruiting intensities or, equivalently, from firm sizes. Intuitively, if a firm makes higher profits per matched worker, it will optimally post more vacancies and attain a larger size. In turn, by leveraging the equilibrium structure of our model, the distribution of profits per matched worker across firm ranks allows us to infer utility levels offered to workers. In combination with the observed wage components, these yield firm-specific amenity values, which—given our assumed amenity cost function—is equivalent to identifying amenity cost parameters. Finally, we identify firm productivities and gender wedge by combining observed wages and identified amenity costs with firms' profits per matched worker.

It is worth noting that our result is more general than the exact statement in Proposition 4, in the sense that our assumptions on the functional form of the amenity cost in equation (8) and of the vacancy cost in equation (9) can be significantly relaxed. All that is required is that the amenity and

²⁹These are the vacancy cost intercept $c^{v,0}$, the elasticity of vacancy costs η^v , and the elasticity of amenity costs η^a .

vacancy cost functions are increasing and convex, as is commonly assumed in many applications.³⁰ Furthermore, our choice of the amenity cost function has no bearing on the estimated distribution of firm-level amenities—in particular, our choice of the elasticity of the amenity cost function η^a is irrelevant for the estimated distribution of amenities $a(r)$.³¹ In comparison to related work by Sorkin (2017, 2018), we leverage the equilibrium nature of our model—specifically, firms' endogenous vacancy posting subject to a convex increasing cost function—to achieve identification of *levels* of utility across firms, which in the context of Sorkin (2017, 2018) are arbitrarily normalized due to the scale parameter of random utility shocks being not identified in his partial-equilibrium framework.³²

5.6 Step 5: Economy-Wide Parameters

In the final step, we pin down three remaining economy-wide parameters given aggregate statistics.

Proposition 5 (Economy-Wide Parameters). *(i) The vacancy cost shifter $c^{v,0}$ is identified based on the aggregate labor share; (ii) the elasticity of the vacancy cost function η^v is identified based on the firm pay-profit gradient; (iii) the elasticity of the amenity cost function η^a is identified based on the aggregate amenity cost share in the data.*

Proof. See Appendix D.9. □

The intuition for part (i) relies on the fact that vacancy costs introduce concavity with respect to the vacancy choice into the firm's objective, which uniquely pins down a firm's size and profits. The firm's FOC with respect to its vacancy choice implies that the same vacancy posting behaviour can be rationalized by any combination of profits and the vacancy cost shifter that keeps the ratio between the two constant. However, as we scale up profits, we mechanically lower the labor share because the level of wages is pinned down by the data. Therefore, we can estimate $c^{v,0}$ by finding the scale of profits that matches the empirical labor share.

³⁰ Examples of such amenity cost functions are Hwang et al. (1998), Lang and Majumdar (2004), and Lavetti and Schmutte (2018). The model in Sorkin (2018) is isomorphic to one with convex increasing amenity costs. Examples of such vacancy cost functions are Mortensen (2003), Kaas and Kircher (2015), Lise and Robin (2017), Bilal et al. (2022), Engbom and Moser (2022), Bilal and Lhuillier (2023), Bloesch and Larsen (2023), Heise and Porzio (2023), and Lindenlaub et al. (2023).

³¹ For instance, we would recover the identical distribution of amenities $a(r)$ under the assumption of exogenous amenities. However, the estimated value of the elasticity of the amenity cost function η^a will matter for the inferred distribution of firm productivity $p(r)$ and thus composite productivity $\tilde{p}(r)$.

³² In Sorkin (2017, 2018), the *levels* of utility across discrete choices of firms could be pinned down if the elasticity of labor supply with respect to the wage were known. Absent a credibly identified change in firm pay, holding fixed firm amenity values and all other features of the environment, our model provides an alternative approach to pinning down the scale of firm utilities using an equilibrium model and functional forms commonly used in the macro-labor literature, the cost parameters of which we identify and estimate based on linked employer-employee data and aggregate statistics.

The intuition for part (ii) is that as the elasticity of the vacancy posting cost becomes higher, the number of vacancies becomes more similar across two firms with given levels of profits per worker. In the limit as $\eta^v \rightarrow \infty$, all firms post a constant number of vacancies. Therefore, to rationalize the observed dispersion in vacancy posting, the model needs to generate more dispersion in profits per matched worker, yielding greater profit dispersion. For fixed levels of pay observed in the data, this implies that the pay-profit gradient varies directly with the elasticity of the vacancy cost function η^v .

Part (iii) follows from our assumptions on the amenity cost function in equation (8). The cost of creating the optimal amount of amenities is $c^a(a^*) = a^*/\eta^a$, which is inversely proportional to η^a . Therefore, we can identify η^a by using it to match the aggregate amenity cost share.

5.7 Interpretation of Results

To summarize, we have identified gender-firm-specific parameters $(p(r), \tau(r), c^{a,0})$, gender-specific labor market objects $(\delta, \lambda^U, \lambda^E, \lambda^G)$, and economy-wide parameters $(c^{v,0}, \eta^v, \eta^a)$. Combining the model structure with the data, this yielded firm-level estimates of $w(r), a(r), v(r)$ across firm ranks r .

At this point, it may be helpful to take a step back and ask: What can we (not) learn from these identification results? Recall the utility of a worker of gender g and ability z was specified to be $\mathcal{U}_{gz}(x) = \omega_{gz}^0 + \omega_{gz}^1 x$, where consumption $x = w + a$ consists of wages w and amenities a . For each gender, our estimates of amenities a and thus consumption x are *in units of wages*, w . In other words, we have identified the relative importance of wages versus amenities relative to the sum of the two.

Of course, we have not identified the utility scale ω_{gz}^1 , which guides the *slope* of felicity and may differ across worker types (g, z) . However, our model is invariant to the utility scale in the sense that all equilibrium objects—i.e., $w_{gz}(r)$, $a_{gz}(r)$, and $v_{gz}(r)$ —are constant for any choice of the parameter ω_{gz}^1 . Naturally, the same caveat applies to the utility intercept ω_{gz}^0 , as we have nothing to say about the *level* of felicity across worker types. This rules out comparisons of the relative felicity of individuals across worker types (e.g., comparing within-gender inequality in felicity between men and women). It also rules out comparisons of absolute levels of felicity between worker types (e.g., comparing the felicity of women with that of men).

Nevertheless, since wages and amenities are in the same units, our identification results allow us

to quantify the relative importance of utility x and amenities a in wages w across firms r as

$$\underbrace{\frac{w_{gz}(r)}{x_{gz}(r)}}_{\text{wage share in total compensation}} + \underbrace{\frac{a_{gz}(r)}{x_{gz}(r)}}_{\text{amenity share in total compensation}} = 1. \quad (22)$$

They also allow us to quantify the shares of variation in felicity $\mathcal{U}_{gz}(x_{gz}(r))$ across firms r due to variation in wages, amenities, and their covariance, which are invariant to felicity's scale and location:

$$\underbrace{\frac{Var(x_{gz}(r))}{Var(w_{gz}(r))}}_{\text{variance share of wages due to } x_{gz}(r)} + \underbrace{\frac{Var(a_{gz}(r))}{Var(w_{gz}(r))}}_{\text{variance share of wages due to } a_{gz}(r)} - \underbrace{\frac{2Cov(x_{gz}(r), a_{gz}(r))}{Var(w_{gz}(r))}}_{\text{variance share of wages due to covariance}} = 1. \quad (23)$$

That all the statistics in equations (22) and (23) are identified in our equilibrium framework is an important contribution over existing work on compensating differentials. For example, the partial-equilibrium model by [Sorkin \(2018\)](#) “can identify the variation in amenities that comes from the ‘pure’ Rosen motive” (p. 1373) but, without further assumptions, “cannot identify the variation in amenities that contribute to utility dispersion, that is, those that come from the Mortensen motive” (p. 1374). By making additional assumptions on the cost structure of firms’ hiring decisions and other features of the environment, our equilibrium model sheds new light on compensating differentials across firms by recovering the joint distribution of amenities and wages, which allows us to quantify both the “Rosen motive” and the “Mortensen motive,” in the language of [Sorkin \(2018\)](#).

In addition to decomposing total compensation into wage and amenity values, our model also allows us to identify the underlying sources of (gender differences in) wages and amenities by associating with each wage-amenity bundle (w, a) a firm type $(p, \tau, (c_g^{a,0})_g)$. In classical job ladder models à la [Burdett and Mortensen \(1998\)](#), productivity p is the only source of firm heterogeneity and wages are the only form of compensation, so more productive firms offer higher wages and employ more workers in equilibrium. The identification results within our richer framework allow us to empirically test these relationships in a world with endogenous amenity provision and hiring.

5.8 Implementation

To implement our identification results, we proceed sequentially by gender. We first trim the top and bottom one percent of the gender-specific pay FE distributions to eliminate outliers. Then, we start

by studying men, for whom gender wedges are normalized to zero. We estimate men's firm ranks r_M using Proposition 2 and men's firm pay $w_M(r_M)$ using Proposition 1. Given the distribution of firm ranks r_M , Proposition 3 allows us to estimate all of the men's labor market objects. We regularize the estimated hiring intensities with a kernel smoother to limit the extent of measurement error and then use Proposition 4 to identify the distribution of productivity $p(r_M)$ and amenity cost shifters $c_M^{a,0}(r_M)$ for men.³³ We then iterate over this process until we find the economy-wide parameters that allow us to match a set of aggregate moments detailed in Proposition 5.

Second, we study women, for whom gender wedges represent the implicit tax relative to the productivity level estimated for men. The identification proceeds analogously to that for men except that we take as given the values of firm productivity $p(r)$ and economy-wide parameters already estimated based on men. As part of this procedure, we recover firms' gender wedges for women such that women's productivity net of the gender wedge at a firm with rank r_F is $(1 - \tau(r_F))p(r_F)$.

A final remark is in order. While our model features a large number of parameters, our identification results demonstrate that these parameters are point-identified and thus pinned down empirically. In this sense, in spite of its richness, our model does not have any remaining degrees of freedom.³⁴

6 Estimation Results

In Section 3, we estimated gender-specific firm pay components. Now, we present estimates of gender-specific firm ranks, labor market parameters, firm types, and economy-wide parameters based on the identification proof in Section 5. A novel aspect of our approach is that we impose no parametric restrictions on the distribution of gender-specific firm types, which the following analysis exploits.

6.1 Estimates of Employer Ranks

While the average firm in our sample is small, the average worker is employed at a large firm. Appendix Figure E.1 shows that employment is highly skewed toward large, high-ranked employers for both genders: the employment-weighted mean rank for men is 0.846 and that for women is 0.845.

³³To translate our results from continuous firm types in theory to discrete firm types in the data, see Appendix D.8.

³⁴Appendix D.10 demonstrates in a sequence of Monte Carlo simulations that our identification procedure perfectly recovers the model parameters under different parameterizations.

6.2 Estimates of Labor Market Parameters

Our estimates of labor market parameters are shown in Table 5. Women receive fewer job offers from nonemployment ($\lambda_F^U = 9.1\%$ compared to $\lambda_M^U = 10.4\%$) and have a lower job destruction rate ($\delta_F^U = 2.8\%$ compared to $\delta_M^U = 3.6\%$). For both men and women, involuntary job offers ($\lambda_M^G = 1.1\%$ and $\lambda_F^G = 0.8\%$) are about as frequent as voluntary ones ($\lambda_M^E = 0.9\%$ and $\lambda_F^E = 0.7\%$). Overall, men receive a greater total of job offers than women. The prevalence of involuntary job offers indicates substantial undirectedness of job search across utility ranks, not just pay ranks (Jolivet et al., 2006).³⁵ The implied nonemployment rates ($u_M = 23.6\%$ and $u_F = 21.9\%$) reflect the presence of a large informal sector for both men and women in Brazil.³⁶ The flow value of nonemployment for men ($b_M = 2.281$) is slightly higher than that for women ($b_F = 2.234$), as is the implied reservation utility ($\phi_M = 2.353$ compared to $\phi_F = 2.274$).³⁷ It is important to keep in mind that these estimates reflect widespread unregistered employment in Brazil (Meghir et al., 2015). Compared to a typical high-income country's labor market (Taber and Vejlin, 2020), these estimates suggest substantial labor market imperfections in Brazil.

Table 5. Job offer arrival rates, job destruction rates, and flow values of nonemployment

Parameter	Description	Men	Women
λ_g^U	Offer arrival rate from nonemployment	0.104	0.091
δ_g	Job destruction rate	0.036	0.028
s_g^E	Relative arrival rate of voluntary on-the-job offers	0.090	0.074
s_g^G	Relative arrival rate of involuntary on-the-job offers	0.101	0.083
b_g	Flow value of nonemployment	2.281	2.312

Note: This table shows the estimated values of all labor market parameters—specifically, the offer arrival rate from nonemployment λ_g^U , the job destruction rate δ_g , the relative arrival rate of voluntary on-the-job offers s_g^E , the relative arrival rate of involuntary job offers s_g^G , and the flow value of nonemployment b_g —separately by gender $g \in \{M, F\}$. All rates are monthly. *Source:* Model estimates based on RAIS, 2007–2014.

6.3 Estimates of Firm Types

Productivity. Our estimates of firm productivity p in Figure E.3 in Appendix E.5 display substantial dispersion and a long right tail. The employment-weighted mean log productivity is 0.864 for men and 0.781 for women, implying a gender productivity gap of 8.3 log points. The standard deviation of log productivity is 0.573 for men and 0.601 for women, more than double that of firm pay.

³⁵Figure E.2 in Appendix E.4 shows large dispersion in estimated firm-level recruiting intensities, and more so for women.

³⁶While women are more likely to be informally employed (Engbom et al., 2022) and out of the labor force (World Bank, 2021b), these estimates suggest that both sexes are similarly attached to Brazil's formal sector conditional on participating. For the U.S., Albanesi and Şahin (2018) also find that men's unemployment rate has exceeded women's in the recent past.

³⁷Le Barbanchon et al. (2020) also find that unemployed men have a higher reservation wage than women in France.

Gender Wedges. The distribution of estimated gender wedges τ is shown in Appendix Figure E.4. Women are less likely to work at firms with high gender wedges, with an employment-weighted mean of 0.059 for women compared to 0.235 for men. Gender wedges in our model may stand in for taste-based discrimination (Becker, 1971) or employer-level comparative advantages across genders (Goldin, 1992). To understand what they capture in the real world, we estimate

$$\hat{\tau}_j = Z_j \eta + \iota_j, \quad (24)$$

where $\hat{\tau}_j$ is the estimated gender wedge for employer j , Z_j is a vector of employer covariates, and ι_j is an error term. We include as covariates in Z_j a total of six variables constructed in the RAIS data.

Table 6 shows that our estimated gender wedges significantly load onto factors related to the female-friendliness of a workplace. For example, having a female manager is associated with lower gender wedges. Employers with higher nonroutine manual task intensity, longer working hours, no major financial stakeholders, and larger workforces have higher gender wedges.³⁸ Altogether, we explain 54.6% of the variation in estimated gender wedges across firms, suggesting that gender wedges in our model capture real-world employer differences.

Table 6. Regressing estimates of gender wedges on employer characteristics

	Coefficient	(std. err.)
Female manager	-0.095***	(0.011)
Nonroutine manual task intensity	0.028***	(0.011)
Nonroutine interpersonal task intensity	0.002	(0.009)
Mean working hours	0.104***	(0.035)
No major financial stakeholders	0.011**	(0.005)
Log size	0.047***	(0.003)
R^2	0.546	

Note: This table reports estimated coefficients from regressing structurally estimated gender wedges on observable employer characteristics—see equation (24). Estimates are conditional on municipality and sector FEs. Details of all covariates are presented in Appendix E.2. Standard errors are clustered at the employer level. ***, **, and * denote significance at the 1%, 5%, and 10% levels, respectively. *Source:* Model estimates based on RAIS, 2007–2014.

Amenity Cost Shifters. The estimated amenity cost shifters $c_g^{a,0}$ are dispersed with long right tails, see Appendix Figure E.5. We relate the implied amenity values to real-world amenity proxies as

$$\hat{a}_{gj} = Z_{gj} \eta_g + \iota_{gj}, \quad (25)$$

³⁸We conservatively cluster standard errors at the employer level to address *experimental design issues* (Abadie et al., 2022).

where \hat{a}_{gj} is the estimated amenity value for gender g at employer j , Z_{gj} is a vector of gender-specific employer covariates, and ι_{gj} is an error. We include in Z_{gj} eight variables based on the RAIS data.

Table 7 shows that, for both men and women, employers with more generous parental leave policies, more stable income and employment, and larger workforces are associated with higher amenity values. For women, but not significantly for men, greater working hours flexibility is valued as a positive amenity.³⁹ Altogether, we explain 44.9% of the variation in estimated amenities for men and 42.3% of that for women, again suggesting that the model amenities capture empirically relevant differences in employer characteristics.

Table 7. Regressing estimates of amenity values on employer characteristics, by gender

	Men		Women	
	Coefficient	Std. err.	Coefficient	Std. err.
Part-time work incidence	-0.030	(0.024)	0.038	(0.025)
Working hours flexibility	-0.010	(0.037)	0.128**	(0.058)
Parental leave generosity	0.041***	(0.009)	0.013*	(0.007)
Income fluctuations	-0.283***	(0.084)	-0.152**	(0.075)
Workplace hazards	-0.496*	(0.276)	-0.235	(0.224)
Incidence of unjust firings	-0.035**	(0.016)	-0.066***	(0.025)
Incidence of workplace deaths	-0.626***	(0.163)	-1.387***	(0.245)
Employer size	0.046***	(0.005)	0.048***	(0.006)
R^2	0.449		0.423	

Note: This table reports estimated coefficients from regressing estimates of gender-specific employer amenity values on observable gender-specific employer characteristics—see equation (25). Estimates are conditional on municipality and sector FEs. Details of all covariates are presented in Appendix E.3. Standard errors are clustered at the employer level. ***, **, and * denote significance at the 1%, 5%, and 10% levels, respectively. *Source:* Model estimates based on RAIS, 2007–2014.

Correlation Structure. Appendix Table E.1 correlates gender-specific pay w_g , amenities a_g , productivity net of gender wedges $(1 - \tau_g)p$, employment l_g , and employer ranks r_g . At this stage, the most interesting takeaway is that pay (0.909), ranks (0.576), and amenities (0.884) are positively but imperfectly correlated within employers across genders. For both genders, amenities are negatively related to pay, which suggests the presence of compensating differentials.

6.4 Estimates of Economy-Wide Parameters

Table 8 shows our estimated elasticity of the vacancy cost function, $\eta^v = 2.064$, which is in the range of existing estimates for Brazil (Engbom and Moser, 2022). Our estimated elasticity of the amenity cost function, $\eta^a = 5.738$, suggests that employer amenities are provided relatively inelastically.

³⁹Again, we conservatively cluster standard errors at the employer level.

Table 8. Estimates of economy-wide parameters

Parameter	Value	Moment	Data	Model
η^v	2.064	Elasticity of pay w.r.t. value added per worker	0.179	0.179
η^a	5.738	Cost share of amenities in value added	0.080	0.080

Note: This table reports the estimated values of the elasticity of the vacancy cost function η^v and the elasticity of the amenity cost function η^a . Targeted moments are the elasticity of pay w.r.t. value added per worker from Alvarez et al. (2018) and the cost share of amenities in value added based on Bieri et al. (2023). See Appendix E.1 for details on the construction of the aggregate statistics. Source: Model estimates based on RAIS, 2007–2014.

6.5 Model Fit

Table 9 shows the model fit based on a range of moments relating to employer pay and worker transitions. Overall, the model fits the data well. The model understates the gender pay gap by 0.5 log points but matches the empirical variances of gender-specific pay and the gender pay gap, job-to-job transition rates, the share of transitions with a pay cut, and the correlation between men’s and women’s pay within firms. Notice that we fit gender-specific firm pay and ranks by construction but discrepancies arise from the model not perfectly replicating the smoothed employment distribution.

Table 9. Model fit

Moment	Description	Data	Model
$\mathbb{E}[\psi_M - \psi_F]$	Gender log pay gap	0.113	0.108
$\mathbb{E}[\psi_F g = M] - \mathbb{E}[\psi_F g = F]$	Gender log pay gap between employers	0.089	0.082
$\mathbb{E}[\psi_F - \psi_M g = F]$	Gender log pay gap within employers	0.024	0.026
$Var[\psi_M]$	Variance of men’s pay	0.054	0.053
$Var[\psi_F]$	Variance of women’s pay	0.044	0.044
$Var[\psi_M - \psi_F]$	Variance of gender pay gap	0.009	0.010
$\mathbb{E}[\lambda_M^E(1 - F_M(x)) + \lambda_M^G]$	Job to job transition rate for men	0.015	0.015
$\mathbb{E}[\lambda_F^E(1 - F_F(x)) + \lambda_F^G]$	Job to job transition rate for women	0.011	0.011
$\mathbb{P}[\psi'_M < \psi_M]$	Probability of wage decline on job to job, men	0.479	0.479
$\mathbb{P}[\psi'_F < \psi_F]$	Probability of wage decline on job to job, women	0.499	0.497
$Corr(\psi_M, \psi_F)$	Correlation between men’s and women’s pay	0.921	0.951

Note: This table reports the fit of the model in terms of data-based and model-based moments across genders $g \in \{M, F\}$. All statistics are employment-weighted. Source: Model estimates based on RAIS, 2007–2014.

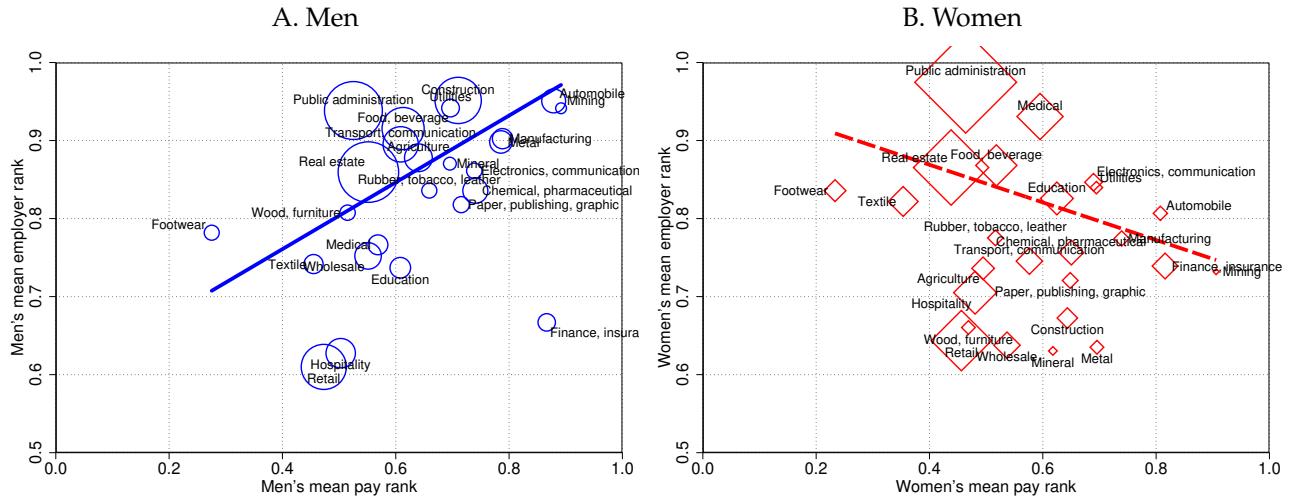
7 Gender-Specific Compensation Structures Across Employers

We now use the estimated model to shed light on the structure of employer compensation by gender.

7.1 Intersectoral Differences in Employer Pay, Amenities, and Ranks

Grouping our estimates into 25 sectors, Figure 3 plots mean employer ranks against mean pay ranks for men in Panel A and for women in Panel B. The rank-pay relationship is upward-sloping for men but downward-sloping for women. For men, the highest-utility employers—e.g., the automobile sector—are also among the highest-paying ones. For women, however, there is a trade-off between higher pay and higher overall utility—e.g., the public sector offers average pay rank but has the highest utility rank. There are also notable gender differences across sectors. For example, the textile sector has a higher pay rank for men but a higher utility rank for women.⁴⁰ Overall, this suggests that preferred employers for men are those with higher pay while the same is not true for women.

Figure 3. Sectoral employer ranks against employer pay ranks, by gender



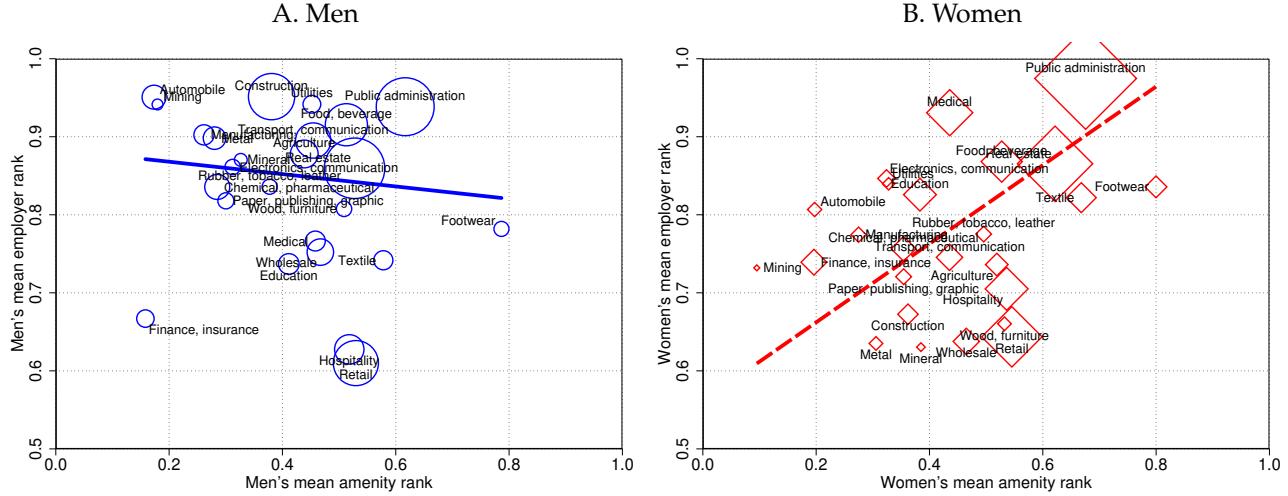
Note: This figure shows ranks of employer utility (x_g) against ranks of employer pay (w_g) for men in Panel A and for women in Panel B across 25 sectors. Circle sizes represent employment weights, on which the linear fit lines are based.

Source: Model estimates based on RAIS, 2007–2014.

Figure 4 plots the estimated employer rank-amenity relationship across the same 25 sectors for men in Panel A and for women in Panel B. For men, mean employer ranks are approximately flat across amenity ranks, suggesting that amenities are not a key determinant of utility for men. For women, however, the rank-amenity relationship is steeply increasing. Therefore, for women more so than for men, employer amenities are a key determinant of overall utility.

⁴⁰See also [Sharma \(2023\)](#) for a comprehensive study of gender-specific monopsony power in the Brazilian textile sector.

Figure 4. Sectoral employer ranks against employer amenity ranks, by gender



Note: This figure shows ranks of employer utility (x_g) against ranks of employer amenities (a_g) for men in Panel A and for women in Panel B across 25 sectors. Circle sizes represent employment weights, on which the linear fit lines are based.

Source: Model estimates based on RAIS, 2007–2014.

7.2 The Importance of Amenities in Total Compensation

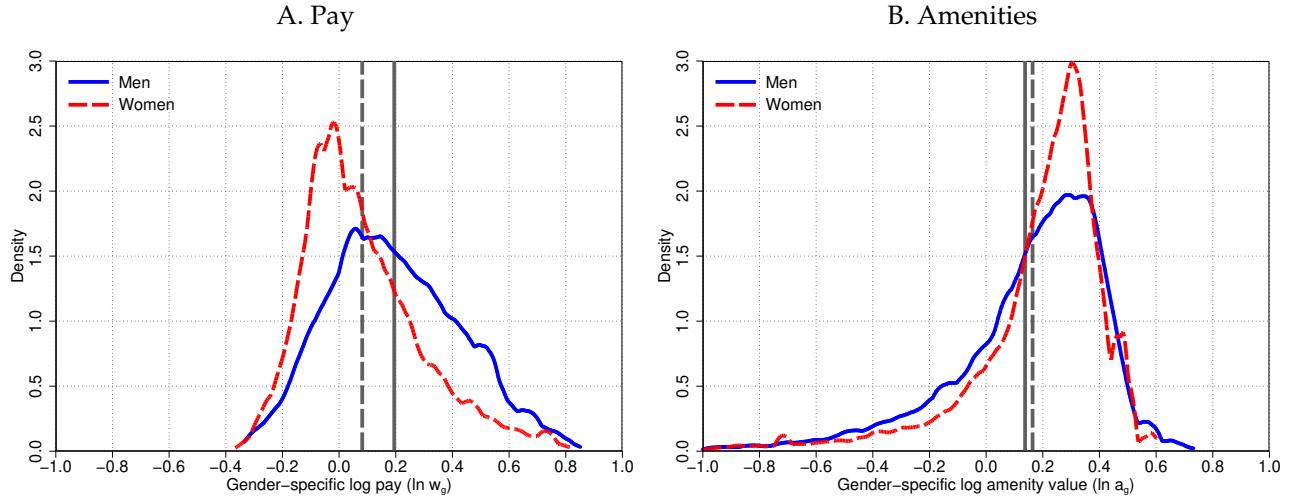
What is the relative importance of pay versus amenities in total compensation, and how does the compensation structure vary across employers for men and women? Figure 5 shows the gender-specific distributions of pay and amenities. The distribution of pay in Panel A is repeated, for comparison, from the empirical analysis in Section 3.1. The distribution of amenity values in Panel B shows that women are more concentrated than men at employers offering high amenity values. Women's mean log amenity value is 0.164, while men's is 0.138, implying a gender amenity gap of -2.6 log points.⁴¹

The structure of pay and amenities has important implications for gender-specific firm rankings. Figure 6 shows the relative values of pay, amenities, and total compensation throughout the firm ladder. Relative to bottom-ranked firms, total compensation increases by 18 log points for men and 12 log points for women toward top-ranked firms. For men, more than this amount is due to higher pay at higher firm ranks, while amenities actually decline across the bottom four rank quintiles. For women, pay is relatively flat throughout most of the distribution, so most of the increase in total compensation across firm ranks is due to higher amenities.

Next, we inspect amenity shares in total compensation, $a_g / (w_g + a_g)$. Panel A of Figure 7 shows the density of amenity shares. For both men and women, amenity shares ranges from zero at the low end all the way up to approximately three quarters at the high end. The mean amenity share is 48.8%

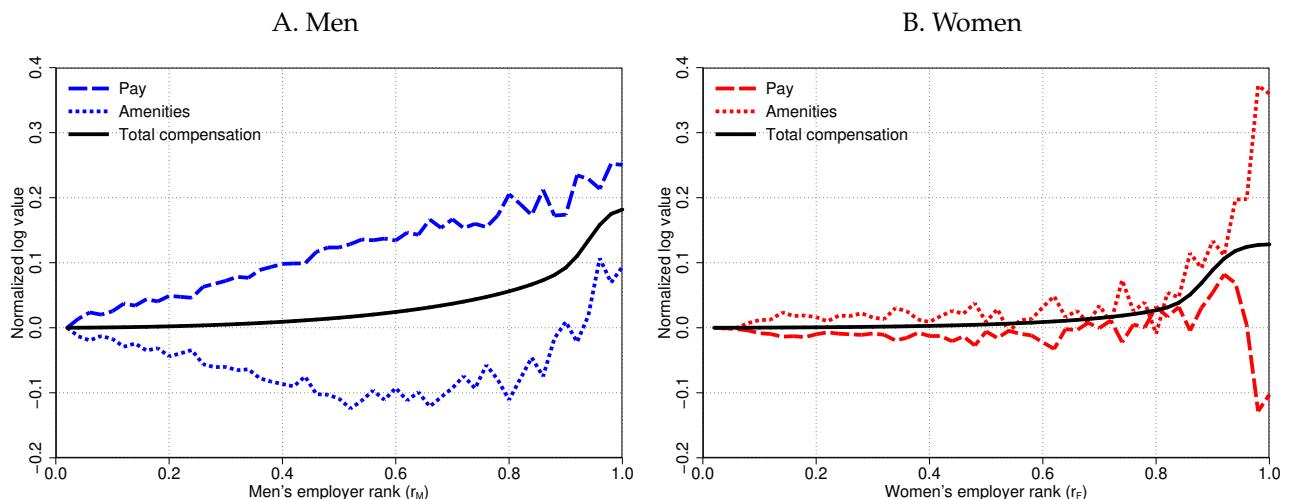
⁴¹Throughout, we compare pay, amenities, and total compensation in logarithms, consistent with the empirical analysis of log pay. The conversion between levels and logs is purely for presentation purposes and inconsequential for our analysis.

Figure 5. Estimated distributions of pay and amenities, by gender



Note: This figure shows the gender-specific employment-weighted distributions of log pay ($\ln w_g$) in Panel A and of log amenities ($\ln a_g$) in Panel B. The grey patterned vertical lines show the population means for the corresponding gender $g \in \{M, F\}$. Source: Model estimates based on RAIS, 2007–2014.

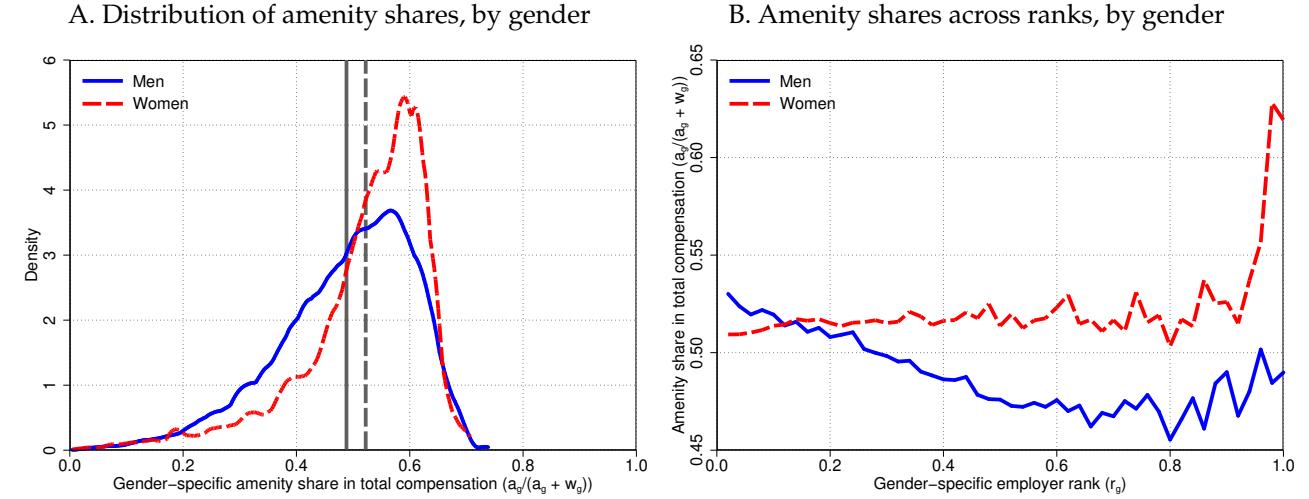
Figure 6. Pay, amenities, and total compensation across employer ranks, by gender



Note: This figure shows the relative values of log pay ($\ln w_g$), log amenities ($\ln a_g$), and log total compensation ($\ln x_g$) across firm ranks (r_g) separately for men in Panel A and for women in Panel B. All log values are normalized to zero at the gender-specific group of bottom-ranked employers. Source: Model estimates based on RAIS, 2007–2014.

for men and 52.2% for women. Overall dispersion in amenity shares is lower for women than for men. Panel B shows the estimated amenity shares across employer ranks r_g . For men, the amenity share is decreasing across most employer ranks. For women, the amenity share is mostly flat and then spikes up in the top decile.

Figure 7. Distribution of amenity shares in total compensation, by gender



Note: Panel A of this figure shows the gender-specific employment-weighted distribution of amenity shares in total compensation ($a_g/(w_g + a_g)$). The grey patterned vertical lines show the population means for the corresponding gender $g \in \{M, F\}$. Panel B of this figure shows the amenity share in total compensation ($a_g/(w_g + a_g)$) across employer ranks (r_g) separately by gender $g \in \{M, F\}$. Source: Model estimates based on RAIS, 2007–2014.

7.3 Employer Pay Dispersion Due to Utility Dispersion

Our framework's ability to account for differences in amenities across employers allows us to revisit hitherto documented facts about labor market inequality. As shown in Table 10, the variance of log employer pay is 0.054 for men and 0.044 for women. Taken at face value, such dispersion in pay for identical workers across employers suggests significant labor market imperfections for both genders. However, we find that the variance of log total compensation across employers is 0.002 (i.e., 4.4% of pay dispersion) for men and 0.002 (i.e., 3.6% of pay dispersion) for women. Thus, the lion's share of firm pay differences are explained by compensating differentials due to firm amenities, with only a small fraction reflecting utility differences. As a result, looking only at differences in pay across employers vastly overstates labor market inequality for both men and women.⁴²

⁴²This result mirrors a similar finding by Lamadon et al. (2022) who estimate a model without search frictions for the U.S. labor market. What is striking is that we find a similarly small role for utility dispersion across firms using a model with search frictions for a labor market characterized by significant imperfections in a developing-country context.

Table 10. Decomposition of employer pay dispersion into utility and amenity terms

Variances	Men		Women	
	Level	Share (%)	Level	Share (%)
Variance of log pay	0.054		0.044	
Variance components of log pay:				
Log utility	0.002	4.4	0.002	3.6
Log amenities	0.051	94.3	0.045	102.8
Covariance between log utility and log amenities	0.001	1.3	-0.003	-6.4
Covariance components of log pay:				
Covariance between log utility and log pay	0.003	5.1	0.000	0.4
Covariance between log amenities and log pay	0.052	94.9	0.044	99.6

Note: This table shows the variance and covariance components of log pay ($\ln w$). To this end, we define “amenities” as the utility-to-wage ratio $\tilde{a} = x/w$ so that $\ln w = \ln x - \ln \tilde{a}$. The variance components correspond to the variance decomposition $Var(\ln w) = Var(\ln x) + Var(\ln \tilde{a}) - 2Cov(\ln x, \ln \tilde{a})$. The covariance components correspond to the covariance decomposition $Var(\ln w) = Cov(\ln w, \ln x) - Cov(\ln w, \ln \tilde{a})$. *Source:* Model estimates based on RAIS, 2007–2014.

7.4 Gender Gaps in Pay, Amenities, and Total Compensation

While there is a gender pay gap of 11.3 log points, we find a gender amenities gap of -2.6 log points in favor of women. As a result, the gender gap in total compensation is 4.6 log points (i.e., 40.9% of the pay gap). That the total compensation gap is lower than the pay gap is a direct consequence of the fact that women work at employers with higher amenity shares in total compensation.

To shed light on the gender gaps in pay, amenities, and total compensation, Table 11 shows Kitagawa-Oaxaca-Blinder decompositions into gaps between versus within employers. The first row, repeated from the empirical analysis in Section 3, shows that the majority share of the gender pay gap is between employers. The second row shows that the gender amenities gap of -2.6 log points is due to a larger between-employer component of -9.2 log points, reflecting the sorting of women into high-amenity firms, and an offsetting within-employer component of 6.5 log points, reflecting the amenity premium that men enjoy over women at the same firm. Altogether, the gender gap in total compensation of 4.6 log points is almost entirely accounted for by the within-employer gap. This suggests that in order to close the gender utility gap, we need to inspect factors leading to unequal treatment of men and women within the same employer—such as the gender wedges τ in our model.

7.5 Different Margins of Gender Discrimination

In classical theories of taste-based discrimination (e.g., Becker, 1971), employers receive disutility from employing certain population groups, which affects the employer’s recruiting decisions vis-à-vis these groups. In our framework, the gender wedge τ plays precisely this role. In addition, our frame-

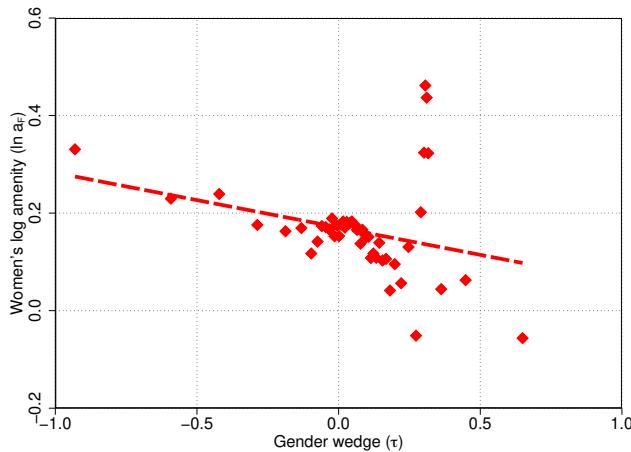
Table 11. Kitagawa-Oaxaca-Blinder decompositions of gaps in pay, amenities, total compensation

Gender gap	Between-employer gap		Within-employer gap		
	Level	Share (%)	Level	Share (%)	
Pay	0.113	0.089	78.7	0.024	21.3
Amenities	-0.026	-0.092	348.6	0.065	-248.6
Total compensation	0.046	0.002	4.6	0.044	95.4

Note: This table shows results from the Kitagawa-Oaxaca-Blinder decomposition of the gender gaps in pay, amenities, and total compensation into a between-employer and a within-employer gap. In logarithms, the gap in pay w plus the gap in amenities a need not add up to the gap in total compensation $x = w + a$. All decompositions are based on equation (2). Table B.1 in Appendix B.2 as well as Tables F.1–F.2 in Appendix F.1 show alternative decompositions using men’s compensation for computing the between-employer component of pay, amenities, and total compensation, respectively. *Source:* Model estimates based on RAIS, 2007–2014.

work features frictional pay dispersion across employers and allows employers to choose amenities separately for each gender.⁴³ This highlights amenities as a novel margin of employer “discrimination” (i.e., unequal treatment) across genders. Under the hypothesis that employers use amenities to differentiate between workers, one would expect gender wedges and women’s amenity values a_F to be negatively related. Indeed, we confirm such a negative relationship, shown in Figure 8.

Figure 8. Negative relation between women’s amenities and gender wedges



Note: This figure shows a binned scatter plot of women’s log amenities ($\ln a_F$) against gender wedges (τ), with the linear best fit line in dashed red being weighted by female employment. *Source:* Model estimates based on RAIS, 2007–2014.

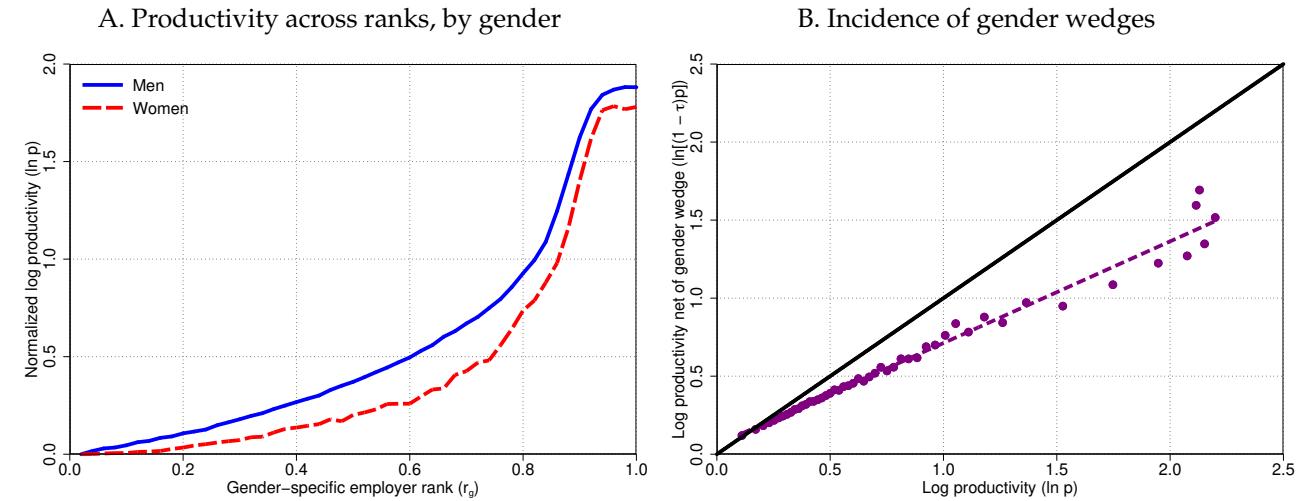
7.6 Implications for Productivity

Panel A of Figure 9 shows the mean productivity p at different rungs of men’s and women’s firm ladders. Productivity is more steeply increasing in employer ranks for men than for women. The differences are meaningful. For example, men’s median-ranked employer is 35 log points more produc-

⁴³We have in mind the costly provision of amenities such as health insurance (Dey and Flinn, 2005), job security (Jarosch, 2023), workplace safety (Lavetti and Schmutte, 2018), and protection against sexual harassment (Folke and Rickne, 2022).

tive than bottom-ranked employers, while the same statistic is only 21 log points for women. Thus, for men more so than for women, improvements in labor market efficiency yield productivity gains. Panel B plots women's productivity net of the gender wedge ($(1 - \tau)p$) against men's productivity (p). Among the least productive firms, gender wedges are close to zero but they steadily increase toward higher productivity levels. Again, the magnitudes are noteworthy. Near the top of the productivity distribution, the average gender wedge accounts for up to 50 log points of productivity.

Figure 9. Productivity, ranks, and gender wedges



Note: Panel A of this figure shows gender-specific employment-weighted log productivity ($\ln p$) across employer ranks (r_g) separately by gender $g \in \{M, F\}$. Panel B shows a binned scatter plot of women's productivity net of gender wedges ($\ln[(1 - \tau)p]$) against men's log productivity ($\ln p$), with the linear best fit line in dashed purple being weighted by total (i.e., male plus female) employment. Source: Model estimates based on RAIS, 2007–2014.

While not targeted, our model generates a lower elasticity of pay with respect to productivity for women (0.094) than for men (0.174). In our model, rent sharing is determined endogenously due to the combination of three gender-specific factors that we separately identify: compensating differentials (Rosen, 1986), taste-based discrimination (Becker, 1971), and monopsony power (Robinson, 1933).

7.7 Switching Employment and Compensation Policies Across Genders

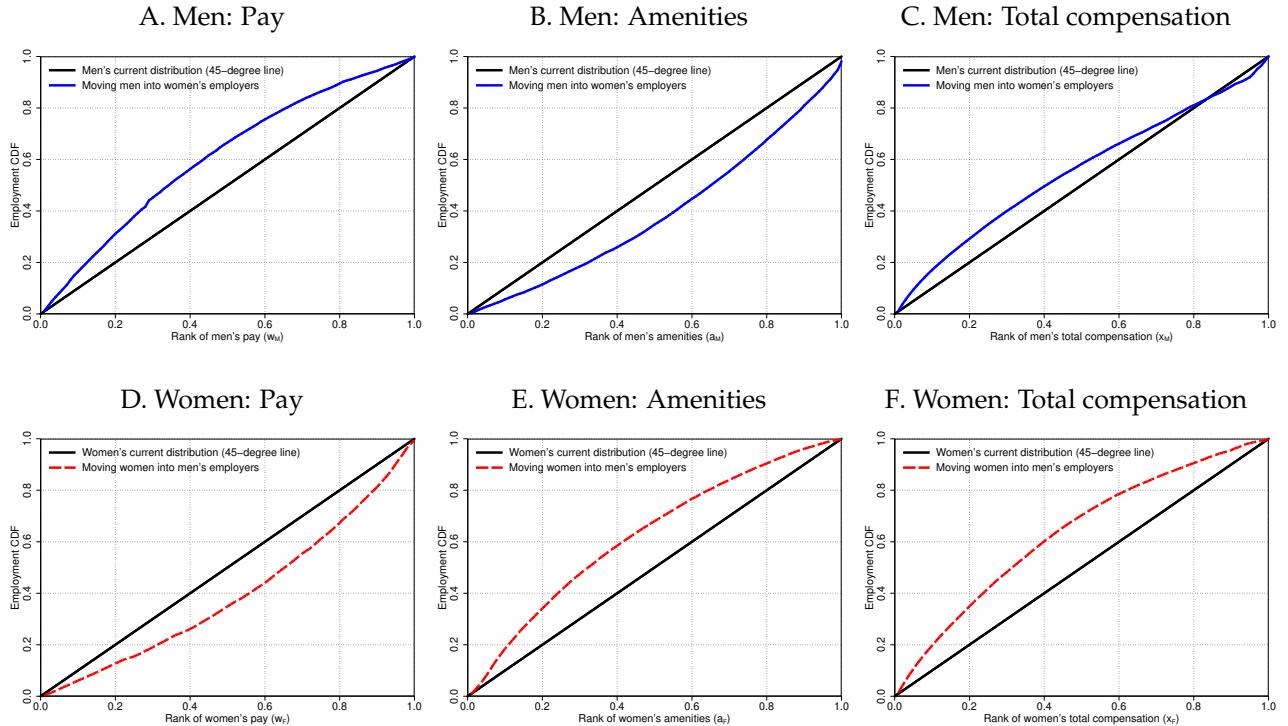
Next, we relocate all workers of one gender into the other gender's employers, while keeping compensation policies constant, and vice versa. In an accounting sense, we then ask whether either men or women would prefer the other gender's employment distribution or compensation policies.

We first shift men's employment distribution to that of women: $l_M \mapsto l_F$, the results of which are presented in Panels A–C of Figure 10. In the baseline, men's CDF of employment is represented by the 45-degree line in each panel. After moving men into women's firms, the solid blue line indicates

the simulated CDF of employment. Such a move reduces men's welfare by 0.2 log points overall, consisting of a 8.9 log points loss in pay and a 9.2 log points gain in amenities. Interestingly, workers in the top 15% of the utility distribution actually prefer women's employment distribution. If, instead, we keep men's employment constant but change firm pay and amenities to those for women, men's total compensation decreases by 5.9 log points, consisting of a decrease in amenities by 9.1 log points and a decrease in pay by 4.0 log points. This experiment demonstrates that there are large differences in the treatment of men and women within employers.

Next, we shift women's employment distribution to that of men: $l_F \mapsto l_M$, the results of which are presented in Panels D–F of Figure 10. As a result of this shift, women's welfare decreases by 1.3 log points, consisting of a 7.3 log points increase in pay but a 11.8 log points decrease in amenities. If, instead, we keep women's employment constant but change firm pay and amenities to those of men, women's amenities increase by 6.5 log points and their pay increases by 2.4 log points. As a result, women's total compensation increases by 4.4 log points, accounting for almost all of the gender utility gap, which again highlights the importance of unequal treatment within employers.

Figure 10. Outcomes associated with moving men into women's employers and vice versa



Note: This figure shows men's CDF over pay (w_M) in Panel A, amenities (a_M) in Panel B, and total compensation (x_M) in Panel C in the baseline as the diagonal solid black line and after moving men into women's employers as the solid blue line. Analogously, it shows women's CDF over pay (w_F) in Panel D, amenities (a_F) in Panel E, and total compensation (x_F) in Panel F in the baseline as the diagonal solid black line and after moving women into men's employers as the dashed red line. *Source:* Model estimates based on RAIS, 2007–2014.

8 Equilibrium Counterfactuals

In this section, we use the estimated equilibrium model to conduct a series of counterfactual experiments. The equilibrium nature of our model is key because we study counterfactual economies in which the removal of certain model ingredients or the imposition of certain policies changes the optimizing behavior of workers and firms. We rely on the rich, nonparametrically identified distribution of gender-specific employer characteristics to quantify both microeconomic (e.g., the gender pay gap) and macroeconomic (e.g., aggregate output) effects due to these counterfactuals.

8.1 Structural Decomposition of Gender Gaps in Pay, Amenities, and Utility

Our structural decomposition in Table 12 consists of four counterfactuals that illustrate the relative contributions of gender-specific compensating differentials (Rosen, 1986), taste-based discrimination (Becker, 1971), monopsony power (Robinson, 1933), and their interplay. First, we remove employer heterogeneity in amenities. Second, we remove employer heterogeneity in gender wedges. Third, we remove gender differences in labor market efficiency. Fourth, we remove all gender differences.

Table 12. Structural decomposition of the gender pay gap

	Baseline	Counterfactuals			
	(0)	(1)	(2)	(3)	(4)
Differences in amenities	✓		✓	✓	
gender wedge	✓	✓		✓	
labor market parameters	✓	✓	✓		
Gender log pay gap	0.108	0.059	-0.002	0.105	0.000
between employers	0.082	0.022	-0.027	0.082	0.000
within employers	0.026	0.037	0.025	0.023	0.000
Gender log amenities gap	-0.017	0.036	0.072	-0.017	0.000
Gender log utility gap	0.048	0.048	0.030	0.047	0.000
Output	1.000	1.016	1.129	0.992	1.061
Worker welfare	1.000	1.015	1.010	1.000	1.021
Employment for men	0.764	0.772	0.764	0.764	0.764
Employment for women	0.781	0.805	0.821	0.764	0.764

Note: This table reports results from equilibrium counterfactuals. The baseline economy (column 0) is compared to counterfactuals without differences in amenities across employers (column 1), without differences in gender wedges across employers (column 2), without gender differences in labor market efficiency (column 3), and without any gender differences in the economy (column 4). *Source:* Model estimates based on RAIS, 2007–2014.

The Role of Gender-Specific Compensating Differentials. What would gender inequality be in a world without amenity differences across employers? To answer this question, we set all amenities to

the mean amenity value for each gender, $a_g \mapsto \bar{a}_g$, by equalizing firms' amenity cost shifters. As a result, the gender pay gap declines by 4.9 log points, or 45% of the baseline, due to two channels. First, women relocate away from low-productivity, high-amenity employers, which lowers the between-employer pay gap by 6.0 log points. Second, higher-productivity employers tend to have larger gender wedges and pay women less, which increases the within-employer gap by 1.1 log points. Interestingly, while the gender pay gap closes substantially, the gender utility gap remains unchanged because workers lose in amenities by about as much as they gain in pay. However, employment rises by 2.4 percentage points and output rises by 1.6% due to the increased competitiveness of high-productivity firms. In net, worker welfare increases by 1.5%. Overall, this counterfactual highlights that amenities play an important role in that they shape equilibrium labor market competition by disproportionately helping lower-productivity firms attract and retain workers—especially women.

The Role of Employer Preferences over Gender. What would the gender inequality be if there were no heterogeneity in gender wedges? We set gender wedges at all firms to the average gender wedge, $\tau \mapsto \bar{\tau}$. As a result, the gender pay gap disappears completely, largely because women relocate toward higher-productivity employers who initially have higher gender wedges and, once removed, compete more for women by increasing their recruiting intensity and pay. As a result, the between-employer pay gap closes and output increases by 12.9%. However, more productive employers also offer lower amenities to women leading to an increase in the gender amenities gap by 8.9 log points. Overall, the gender utility gap is reduced by only 1.8 out of the original 4.8 log points and worker welfare increases by 1.0%. Taken together, this counterfactual makes clear that amenities interact with gender wedges: low-paying low-productivity firms require both higher amenities and lower gender wedges in order to attract a substantial female workforce.

The Role of Gender-Specific Monopsony Power. What is the role of gender-specific monopsony power in shaping gender inequality? We set the parameters guiding women's labor market efficiency so that $\lambda_F^U \mapsto \lambda_M^U$, $s_F^E \mapsto s_M^E$, $s_F^G \mapsto s_M^G$, and $\delta_F \mapsto \delta_M$. As a result, the gender pay gap declines by only 0.3 log points and the gender utility gap by 0.1 log points. The reason behind the small effect is that women receive more on-the-job offers but also separate more frequently from their employers. Thus, their overall speed of climbing the firm ladder barely changes. All in all, while there is large monopsony power in Brazil, differences in labor market fluidity are not a key driver of gender gaps.⁴⁴

⁴⁴This contrasts with [Bowlus \(1997\)](#) and [Flinn et al. \(2023\)](#) who attribute a significant fraction of the U.S. gender wage gap to different labor market behaviors across the sexes using an equilibrium search model *without* compensating differentials.

The Effects of Moving To a Gender-Neutral Labor Market. What would a labor market with no gender differences in amenities (i.e., $a_F \mapsto a_M$), no gender wedges (i.e., $\tau = 0$), and no gender differences in labor market efficiency (i.e., $\lambda_F^U \mapsto \lambda_M^U$, $s_F^E \mapsto s_M^E$, $s_F^G \mapsto s_M^G$, and $\delta_F \mapsto \delta_M$) look like? Obviously, this closes the gender gaps in pay and amenities. Strikingly, this also increases aggregate output by 6.1% and overall worker welfare by 2.1%, as women experience greater flow utility by 4.8 log points associated with them moving to more productive firms with higher total compensation. In summary, moving to a gender-neutral labor market yields significant output and welfare gains.

8.2 The (Unintended) Effects of Equal-Treatment Policies

Many countries have recently considered or already imposed legislation requiring the equal treatment of men and women among their workforce and their applicant pool.⁴⁵ Given that such policies have clear effects on firm's incentives to hire, pay, and provide amenities, our equilibrium framework is ideally suited to evaluating such policies.⁴⁶ To this end, we simulate the effect of imposing an *equal-pay policy* and, separately, an *equal-hiring policy*. Our results are summarized in Table 13, where column 0 shows the baseline economy, column 1 the equal-pay policy, and column 2 the equal-hiring policy.⁴⁷

The Equal-Pay Policy. Our first policy experiment simulates an equal-pay policy that requires all dual-gender firms to offer the same pay to workers of identical ability, regardless of their gender. By construction, the within-employer gender pay gap disappears. In addition, the between-employer gender pay gap also reduces substantially since firms, which initially paid men more than women, are now forced to offer suboptimally higher wages for women and suboptimally lower wages for men. This reduces their hiring of workers of both genders, as they make lower profits on women and become less attractive employers to men. Consequently, high-gender wedge firms shrink, employment declines, and average pay increases. The reason for the latter is that surviving firms with negative gender wedges absorb some of the jobs. Aggregate output declines by 3.9% and worker welfare declines slightly, though conditional on staying employed both men and women benefit in net. The bottom line is that an equal-pay policy closes 46.3% of the overall pay gap but is detrimental

⁴⁵In the Brazilian context, on July 3, 2023, Brazilian president Luiz Inácio Lula da Silva passed *Law Number 14.611*, amending Article 461 of the Labor Code, which requires equal pay for men and women performing substantially equal work. In the U.S. context, the *Equal Pay Act of 1963* is an amendment to the *Fair Labor Standards Act* that prohibits employers from paying different wages across the sexes for substantially equal work.

⁴⁶In related work, [Lamadon et al. \(2022\)](#) assume that firms are endowed with a fixed set of amenities but note that “*it would be interesting to extend this analysis to allow for firms to adjust amenities in response to [policy] counterfactuals*” (p. 208).

⁴⁷As equal-treatment policies link the markets for men and women, computing equilibria becomes significantly more complicated. Appendices G.1 and G.2 describe the baseline and alternative numerical solution algorithms, respectively.

to worker welfare and output due to its negative employment effects.

The Equal-Hiring Policy. Our second policy experiment simulates an equal-hiring policy that requires all dual-gender firms to post an equal number of vacancies across the sexes. Such a policy has large reallocation effects, leading to a reduction in the gender pay gap by 6.8 log points due to a near-disappearance of the between-employer pay gap. However, worker welfare actually declines slightly. The reason is that firms, which are constrained by the policy to make suboptimal hiring decisions, now pay less to both men and women. Specifically, high-productivity firms with positive gender wedges reluctantly hire more women, while low-productivity firms with large amenities hire more men. As a result, both genders' firm ladder becomes less directed in utility space. In particular, women receive relatively more pay but relatively fewer valued amenities. Consequently, welfare of employed men and women declines, in spite of greater aggregate output. The equal-hiring policy simulation makes clear that such a heavy-handed policy has large distortionary effects on the allocation of men and women in the labor market related to the fact that men and women have different valuations of pay versus nonpay attributes across employers.

Table 13. Effects of simulated equal-pay and equal-hiring policies

	Baseline	Equal-pay policy	Equal-hiring policy
	(0)	(1)	(2)
Gender log pay gap	0.108	0.058	0.040
between employers	0.082	0.058	0.007
within employers	0.026	0.000	0.033
Gender log amenities gap	-0.017	0.037	0.073
Gender log utility gap	0.048	0.045	0.052
Output	1.000	0.969	1.028
Worker welfare	1.000	0.995	0.999
Employment for men	0.764	0.757	0.748
Employment for women	0.781	0.764	0.807

Note: Table reports results from two counterfactual policy experiments. Baseline results (column 0) are compared against the economy with an equal-pay policy (column 1) and the economy with an equal-hiring policy (column 2). *Source:* Model estimates based on RAIS, 2007–2014.

9 Conclusion

In this paper, we studied the micro sources and macro consequences of the gender pay gap. Our inquiry was motivated by the empirical observation that men are sorted into employers with higher pay, while women are sorted into employers with better workplace amenities. To interpret these facts,

we developed an equilibrium model of firm pay, amenities, and employment. A notable feature of our model was that it allowed for the allocation of and transfers to workers of both genders to reflect compensating differentials (Rosen, 1986), taste-based discrimination (Becker, 1971), and monopsony power (Robinson, 1933) in a frictional labor market à la Burdett and Mortensen (1998). We provided a constructive proof of identification of all model parameters based on linked employer-employee data, which allowed us to flexibly estimate the multiple dimensions of gender-specific employer heterogeneity. We used the estimated framework to shed light on the structure of employer compensation by gender and to simulate counterfactual experiments, including an evaluation of equal-treatment policies.

It should be evident that our methodology and quantitative results have many interesting implications beyond the application to gender. Here, we focus on three. First, both our empirical and structural estimates suggest that men and women do not share a common employer ranking. Consequently, we should not expect all workers to climb the same job ladder. In allowing for separate job ladders by gender, we have taken but a first step in this direction. Our methodology can be applied to study employer heterogeneity across other population groups (e.g., parental status, education, race).

Second, our finding of a large role for compensating differentials demonstrates that measured inequality in labor market outcomes may overstate (or possibly understate, in other contexts) true inequality. That we documented stark differences in the structure of total compensation across men and women prompts us to revisit other distributional phenomena, such as cross-country differences in welfare and the uneven evolution of welfare within countries over time.

Third, employers in our framework have more than one margin of adjustment to changes in the environment. When considering the impact of equal-treatment policies, minimum wages, or income taxation, for example, amenities may move in the opposite direction from pay. Thus, the equity and efficiency consequences of those policies may be different from what data on pay alone would suggest.

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