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DURABLES AND SIZE-DEPENDENCE IN
THE MARGINAL PROPENSITY TO SPEND

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ABSTRACT

Stimulus checks have become an increasingly important policy tool in recent U.S. recessions. How does the households' marginal propensity to spend (MPX) vary as checks become larger? To quantify this size-dependence in the MPX, we augment a canonical model of durable spending by introducing a smooth adjustment hazard. We discipline this hazard by matching a rich set of micro moments. We find that the MPX declines slowly with the size of checks. In contrast, the MPX is flatter in a purely state-dependent model of durables, and declines sharply in a two-asset model of non-durables. Finally, we embed our spending model into an open-economy heterogeneous-agent New-Keynesian model. In a typical recession, a large check of \$2,000 increases output by 25 cents per dollar, compared to 37 cents for a \$300 check. Large checks thus remain effective but extrapolating from the response out of small checks overestimates their impact.

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1 Introduction

Stimulus checks have become an increasingly important policy tool in recent U.S. recessions. Eligible individuals received a tax rebate of up to \$300 in 2001 and \$600 in 2008, and a payment of \$1,200 early in 2020 plus roughly \$2,000 in subsequent rounds. The government relied on these stimulus checks to boost spending and close the output gap during these episodes. Despite the importance of stimulus checks, we know surprisingly little about their effectiveness as they become larger. A large check of \$2,000 could be barely more effective than a smaller check of \$300 if households spend less and less of each additional dollar they receive.

How does the households' marginal propensity to spend (MPX) vary as stimulus checks become larger?¹ Measuring the *size-dependence* in the MPX is challenging.² Empirical studies obtain a wide range of estimates: the marginal propensity to spend can be decreasing, essentially flat, or even increasing (Souleles, 1999; Kueng, 2018; Fuster et al., 2021; Ganong et al., 2022). State-of-the-art models of the MPX focus on non-durables and predict that the marginal propensity to spend falls rapidly with the size of stimulus checks (Kaplan and Violante, 2014). The relevant quantity for policy, however, is total household spending including durables. Indeed, durable spending accounts for a large share of the MPX out of stimulus checks (Souleles, 1999; Parker et al., 2013; Orchard et al., 2022).³ The literature has conjectured that durable purchases could become more responsive as checks become larger (Parker et al., 2013; Fuster et al., 2021), both because durables are lumpy (Bertola and Caballero, 1990; Eberly, 1994) and they can be financed after making a down payment (Attanasio et al., 2008).

To quantify the size-dependence in the MPX, we augment a canonical incomplete markets model of lumpy durable spending (e.g., Berger and Vavra, 2015) by

¹ Following the literature, we use the term “marginal propensity to spend” (MPX) to refer to the average spending response across individuals divided by the size of the income change (e.g., the check). The empirical counterpart is a “rebate coefficient” (Kaplan and Violante, 2014). The MPX includes spending on non-durables and durables (Auclert, 2019; Laibson et al., 2022), in contrast to the marginal propensity to consume (MPC) which only includes non-durables.

² The MPX is notoriously difficult to estimate even in *levels*. Part of the reason is that the MPX varies with the state of the business cycle (Gross et al., 2020), the depth of the recession, etc. Estimating the size-dependence in the MPX is even more challenging, as we do not directly observe multiple checks for the *same* household at the *same* point in the business cycle. Lottery gains are typically much larger than stimulus checks (Fagereng et al., 2021; Golosov et al., 2021).

³ More generally, an extensive literature documents that durable spending responds strongly to income changes (Wilcox, 1989; Aaronson et al., 2012) and wealth shocks (Mian et al., 2013).

allowing for time-dependent adjustments in a flexible way. Households are subject to linearly additive taste shocks for adjustment (McFadden, 1973; Artuç et al., 2010) whose variance controls the degree of time-dependence in adjustment. This specification delivers a smoother adjustment hazard than the typical (s, S) bands produced by the canonical model where adjustment is purely state-dependent. In turn, the model can generate a decreasing, flat, or increasing MPX, depending on the shape of the adjustment hazard. We also assume that households make a down payment in cash to purchase a durable, and borrow the rest with credit.

We discipline the shape of the hazard by matching four pieces of micro evidence that a purely state-dependent or time-dependent model cannot replicate jointly. In particular, our model (i) matches the evidence on the quarterly MPX on durables and non-durables out of small checks; (ii) generates a realistic short-run price elasticity of durable purchases; (iii) replicates the distribution of durable adjustment sizes in the data; and (iv) matches the empirical probability of adjustment as a function of the time elapsed since the last adjustment, which is central to the response to shocks in fixed cost models (Alvarez et al., 2021). The calibrated model also matches several untargeted moments well; for example, the annual MPX out of small and large lottery gains in Fagereng et al. (2021), the fraction of hand-to-mouth agents in Kaplan and Violante (2022) and Aguiar et al. (2023), and the skewed distribution of marginal propensities to spend (with many above 1) in Fuster et al. (2021) and Lewis et al. (2022).

We find that the MPX declines slowly with the size of stimulus checks. The quarterly MPX is around 45% out of a \$100 check, 40% out of a \$1,000 check, and 35% out of a \$2,000 check. The MPXs in our model lie between those of canonical models of non-durables and durables, both in terms of levels and size-dependence. A canonical two-asset model of non-durables (Kaplan and Violante, 2022) produces smaller MPXs which decline much more rapidly, whereas a version of our model with only state-dependent adjustments of durables (as in Berger and Vavra, 2014, for example) produces much larger MPXs which are essentially flat at first and then decline. Overall, the MPX in our model neither surges as sometimes conjectured in the literature (Parker et al., 2013), nor does it fall sharply as in the canonical two-asset model of non-durables.

The extensive margin of durable adjustment plays an important role in this result. As stimulus checks become bigger, a larger and larger share of households adjusts its stock of durables, consistently with the survey evidence of [Fuster et al. \(2021\)](#). This effect offsets the usual precautionary savings motive at the intensive margin which contributes to a rapidly decreasing MPX in non-durables models. Yet, the extensive margin is more muted in our model compared to a purely state-dependent model of durables, as our calibration implies some degree of time-dependence. In turn, the MPX on durables is both lower compared to a purely state-dependent model and does not surge as checks become larger.

We conclude the paper with an application. We embed our spending model into an open-economy heterogeneous-agent New-Keynesian model. This allows us to account for forces that can dampen the effect of checks in general equilibrium, such as inflation and relative price movements, the response of monetary policy, or international leakages through imports. We use this model to evaluate the effect of checks on output and inflation in various recessions driven by a mix of demand and supply shocks.

We first consider a purely demand-driven recession where output falls by 4% (or \$670 per capita) over three quarters and later recovers over two years. Starting from this recession, the government sends a stimulus check in the first quarter to eligible households. A large check of \$2,000 increases output by 25 cents per dollar in the quarter when it is sent, compared to 37 cents for a small check of \$300. Large checks thus remain effective, but extrapolating from the response out of small checks overestimates how much stimulus larger checks provide. A larger check of \$2,500 (or \$3,000 depending on the specification) is required to fully close the output gap. For comparison, we then consider a recession that is coupled with an adverse supply shock and a non-linear Phillips curve. The effect of larger checks wears off more rapidly in this case. A government that misdiagnoses the recession as being entirely demand-driven and attempts to close the perceived output gap by sending a \$3,000 stimulus check would overheat the economy and raise inflation meaningfully.

Methodologically, our paper advances the literature on durable spending in incomplete markets economies. [Berger and Vavra \(2015\)](#) developed the canonical

model that spearheaded this literature. Most notably, [McKay and Wieland \(2021\)](#) extend this canonical model to study monetary policy. They introduce several features to dampen the interest rate elasticity of durable purchases, including operating costs, exogenous adjustment shocks, and limited attention. [Gavazza and Lanteri \(2021\)](#) also build on the canonical model to study the effect of credit shocks, and [Berger et al. \(2023\)](#) analyze policies that subsidize durable purchases. Relative to these papers, we augment the canonical model by introducing a smooth adjustment hazard in the tradition of [Caballero and Engel \(1999\)](#) and more recently [Beraja et al. \(2019\)](#) and [Alvarez et al. \(2023\)](#). We show how to discipline this hazard by matching a rich set of micro level moments. We also study different questions compared to this literature: the size-dependence in the MPX and the effect of stimulus checks in general equilibrium.

We generate a smooth adjustment hazard by introducing a discrete choice problem with additive taste shocks à la [McFadden \(1973\)](#). This specification allows for purely time-dependent adjustment (constant hazard), purely state-dependent adjustment (binary hazard), and everything in between.⁴ An important body of work in industrial organization uses this form of discrete choice to estimate the demand for durables both in static settings ([Berry et al., 1995](#)) and dynamic ones ([Chen et al., 2013](#); [Gowrisankaran and Rysman, 2012](#)). Some papers in the heterogeneous-agent literature adopt taste shocks when studying discrete choices for labor supply or prices ([Iskhakov et al., 2017](#); [Auclert et al., 2021](#)). They do so for numerical reasons only; the shocks have an arbitrary small variance and a zero mean. In contrast, we discipline both the mean and the variance of these shocks using micro data, and these moments are key for the shape of the adjustment hazard and the size-dependence in the MPX.

Our paper also adds to a literature that studies the effect of stimulus checks in general equilibrium. The existing work on tax rebates (e.g., [Wolf, 2021](#); [Wolf and McKay, 2022](#)) or transfers in fiscal unions (e.g., [Farhi and Werning, 2017](#); [Beraja, 2023](#)) abstracts from durables altogether and uses first order approximations in the aggregates. In contrast, durable spending is central to our analysis, and

⁴ This specification is rooted in the psychology literature and has axiomatic foundations ([McFadden, 2001](#)). It is used extensively in the context of consumption choices ([Nevo, 2001](#)), school choices ([Agarwal and Somaini, 2020](#)) and occupational choices ([Artuç et al., 2010](#)). Random monetary fixed costs of adjustment, which are sometimes used in the firm investment and price setting literatures, do not have a clear empirical counterpart for consumer durables.

we show that it generates substantial non-linearities in the aggregate. Our general equilibrium application is also related to [Orchard et al. \(2022\)](#), who use a linearized two-agent model to show that changes in the relative price of durables can dampen the response to stimulus checks in general equilibrium. We focus on the non-linearities generated by our heterogeneous-agent model with lumpy durables. When allowing for relative price changes, we find that the effect of checks wears off more rapidly as they become larger.

Finally, our analysis is related to a literature that explores how behavioral frictions affect the MPX. [Laibson et al. \(2021\)](#) find that MPXs can remain elevated for large shocks when households are present-biased. In an extension that builds on [Laibson et al. \(2022\)](#), they allow for a durable good whose adjustment is frictionless. In contrast, non-convex adjustment costs are key to our mechanism. [Fuster et al. \(2021\)](#) find that non-convex costs of attention or re-optimization can generate an MPX that increases with income changes. Their model allows for a single non-durable good, whereas durables are central to our analysis. We microfound the logit adjustment hazard in our model by introducing random taste shocks. [Matějka and McKay \(2015\)](#) provide a behavioral foundation for such hazard that is based on agents making mistakes due to costly information processing.

2 A Model With A Smooth Adjustment Hazard

We now introduce our model of household spending. Households consume non-durables and invest in durables, and they face uninsured earnings risk. Time is discrete, and there is no aggregate uncertainty. Periods are indexed by $t \geq 0$.

2.1 Goods and Preferences

Households consume $c_t \geq 0$, and invest in durables $d_t \geq 0$. Their utility is

$$\mathcal{U}_t \equiv u(c_t, d_{t-1}) + \beta \mathbb{E}_t [\mathcal{U}_{t+1}],$$

for some discount factor $\beta \in (0, 1)$. Inter- and intra-temporal preferences are

$$u(c, d) = \frac{1}{1 - \sigma} U(c, d)^{1 - \sigma} \quad \text{and} \quad U(c, d) = \left[\vartheta_c^{\frac{1}{\nu}} c^{\frac{\nu-1}{\nu}} + \vartheta_d^{\frac{1}{\nu}} d^{\frac{\nu-1}{\nu}} \right]^{\frac{\nu}{\nu-1}},$$

where σ is the inverse elasticity of inter-temporal substitution, ν is the elasticity of intra-temporal substitution, and consumption weights satisfy $\vartheta_c + \vartheta_d = 1$.

2.2 Durable Adjustment Hazard

We specify a flexible adjustment hazard that captures the time- and state-dependence in durable adjustment. Households are subject to linearly additive taste shocks for adjustment. These taste shocks ϵ are independent over time and distributed according to a logistic distribution \mathcal{E} .⁵ The mean and variance of this distribution are controlled by $\kappa > 0$ and $\eta^2 > 0$, respectively.⁶ The resulting durable adjustment hazard is

$$S(\mathbf{x}) = \frac{\exp\left(\frac{V^{\text{adjust}}(\mathbf{x}) - \kappa}{\eta}\right)}{\exp\left(\frac{V^{\text{adjust}}(\mathbf{x}) - \kappa}{\eta}\right) + \exp\left(\frac{V^{\text{not}}(\mathbf{x})}{\eta}\right)}, \quad (2.1)$$

where V^{adjust} and V^{not} denote the continuation values when adjusting and not adjusting, respectively, and \mathbf{x} denotes the household's idiosyncratic state which we define formally later in this section.

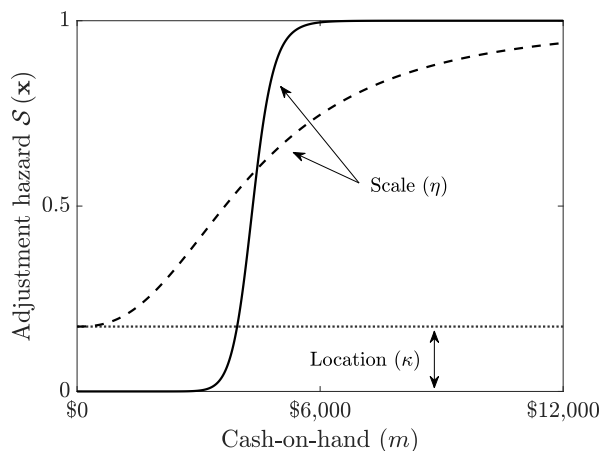
The scale parameter η controls the *shape* of the adjustment hazard while the location parameter κ controls its *position*. The model reduces to a fully state-dependent model when $\eta \rightarrow 0$, i.e., adjustment is deterministic conditional on \mathbf{x} . The parameter κ controls the position of (s, S) bands in this case. In this sense, κ effectively governs the fixed cost of adjustment. At the other extreme, the model boils down to a fully time-dependent model when $\eta \rightarrow +\infty$, i.e., adjustment is random and independent of \mathbf{x} . The parameter κ controls the probability of adjustment in this case.⁷ Figure 2.1 provides an illustration of two such hazards. The first (solid curve) is a very steep hazard. It resembles the discontinuous adjustment hazard associated with (s, S) bands in canonical models of lumpy durable spending, which are purely state-dependent. The second (dashed curve) is a much flatter hazard, which results from allowing for time-dependent adjustments (Alvarez et al., 2016b). As

⁵ This specification is common in the literature, as discussed in our introduction. Additional references in the context of automobile demand include Rust (1985) and Gillingham et al. (2022).

⁶ The literature typically normalizes the mean of these shocks to zero (Artuç et al., 2010). By letting the mean and variance be unrestricted, we introduce one extra degree of freedom which allows us to match the micro-level evidence (Section 3). Random monetary fixed costs of adjustment (Alvarez et al., 2023) also produce a smooth hazard, although they do not have a clear economic interpretation in the context of consumer durables.

⁷ In this limit, $\kappa = \log(1/\phi - 1)\eta$ induces a constant hazard $\phi \in (0, 1)$.

Figure 2.1: Adjustment hazard (fixing d)



we discuss after presenting the rest of the model, the shape of this adjustment hazard plays a key role in the size-dependence in the MPX (Section 2.6).

2.3 Investment, Saving, and Down Payment

Households invest in durables. Their stock depreciates at rate δ and requires a mandatory maintenance rate ι between adjustments so $d_t = (1 - (1 - \iota)\delta)d_{t-1}$ when the household does not adjust (Berger and Vavra, 2015). Households also save in a liquid asset $m \geq 0$ (i.e., cash, deposits) with return r^m . They use this liquid asset to make a down payment when they purchase a durable and borrow the rest through credit at interest rate $r^b \geq r^m$. This credit equals a share $1 - \theta$ of the value of the durable next period (before depreciation).⁸ Households repay their outstanding credit at the same rate at which the value of their durable depreciates, so that credit effectively tracks the stock of durables d . This assumption allows us not to introduce credit as an additional state variable, which would make the problem numerically intractable.⁹ It is also fairly realistic. Households make pre-determined credit repayments in our model while they hold their stock of durables

⁸ Down payments are an important feature of durable goods purchases in practice (Argyle et al., 2020), and are key to understand the response of durables to shocks (Luengo-Prado, 2006). In practice, the vast majority of down payments on cars — the largest component of consumer durables — do not exceed the minimum level required (Green et al., 2020). Refinancing and prepayment are relatively rare too for auto loans.

⁹ An *even* richer model could allow for refinancing (Berger et al., 2021; Laibson et al., 2021) or prepayments. Adding these features *in addition to* lumpy durables would be intractable.

(as in [Laibson et al., 2021](#)), which mimicks the rule of thumb they appear to follow in practice ([Argyle et al., 2020](#)). Moreover, when it comes to cars — the largest component of consumer durables — most loans are repaid within 5–6 years and cars depreciate at a rate of roughly 20% per year so that outstanding credit effectively tracks durables. Finally, households repay any outstanding credit in full when purchasing a new durable.

Our formulation differs from existing models of durables, which assume a loan-to-value constraint and do not make a distinction between cash and credit ([Luengo-Prado, 2006](#); [Berger and Vavra, 2015](#); [McKay and Wieland, 2021](#)). This presumes that households can refinance *continuously* and extract equity from their durables. As a result, the effective supply of liquidity in the economy (i.e., the average distance to the borrowing constraint) is much larger than in the data and the households' MPX is implausibly small ([McKay and Wieland, 2021](#)) particularly for non-durables.¹⁰ Moreover, while refinancing is common for housing, it is virtually nonexistent for consumer durables which we focus on; auto loan prepayments are relatively rare too ([Heitfield and Sabarwal, 2004](#)).

2.4 Earnings and Income

Households' earnings $y_t Y_t^{\text{inc}}$ are the product of idiosyncratic productivity y_t and aggregate income Y_t^{inc} . The log-productivity $\log(y_t)$ follows an AR(1) process as in [Berger and Vavra \(2015\)](#) and [McKay and Wieland \(2021\)](#). We denote the associated transition kernel by $\Gamma(dy'; y)$. Households' net income before interest rate payments is $\psi_0 (y_t Y_t^{\text{inc}})^{1-\psi_1}$, where ψ_0 and ψ_1 parametrize progressive taxation ([Heathcote et al., 2017](#)). Total income after interest rate payments is

$$\mathcal{Y}_t(\mathbf{x}; T_t) \equiv \psi_{0,t} (y_t Y_t^{\text{inc}})^{1-\psi_1} + (1 + r_{t-1}^m) m - r_{t-1}^b (1 - \theta) d + T_t,$$

where $\mathbf{x} \equiv (d, m, y)$ is the household's idiosyncratic state (i.e., its stock of durables, holdings of liquid assets, and income shock), and T_t are stimulus checks.¹¹

¹⁰ For instance, [Kaplan et al. \(2018\)](#) report that the average stock of *net* durables equals 22% of annual GDP. Assuming that $\theta = 20\%$ as in our calibration (Section 3), the conventional formulation would imply that the average household can draw liquidity at any point to $22\%/\theta \times (1 - \theta) = 88\%$ of average income. This figure is much larger than usual values (e.g., [Kaplan et al., 2018](#)).

¹¹ We assume for now that the stimulus check in the first period $T_0 \geq 0$ is the same for all households. It acts as a one-time, unanticipated income shock. The spending response that we measure

2.5 Recursive Formulation

We now state the household's problem recursively. The household first chooses whether to adjust its stock of durables or not. The value associated to the discrete choice problem is

$$\mathcal{V}_t(\mathbf{x}; \epsilon) = \max \left\{ V_t^{\text{adjust}}(\mathbf{x}) - \epsilon, V_t^{\text{not}}(\mathbf{x}) \right\}.$$

This discrete choice problem yields the adjustment hazard (2.1). When the household adjusts its stock of durables, it solves

$$\begin{aligned} V_t^{\text{adjust}}(\mathbf{x}) &= \max_{c, d', m'} u(c, d') + \beta \int \mathcal{V}_{t+1}(d', m', y'; \epsilon') d\mathcal{E}(\epsilon') \Gamma(dy'; y) \\ \text{s.t. } \theta d' + m' + c &\leq \mathcal{Y}_t(\mathbf{x}; T_t) + \{(1 - \delta) - (1 - \theta)\} d \\ m' &\geq 0. \end{aligned}$$

The households' cash-on-hand consists of its total income $\mathcal{Y}_t(\mathbf{x}; T_t)$ plus the value of the durable it sells $(1 - \delta)d$ net of the outstanding credit it repays $(1 - \theta)d$. The household chooses its new stock of durables d' and makes a down payment $\theta d'$, and it decides how much to spend on non-durables c . When holding on to its existing stock of durables, the household solves

$$\begin{aligned} V_t^{\text{not}}(\mathbf{x}) &= \max_{c, m'} u(c, d') + \beta \int \mathcal{V}_{t+1}(d', m', y'; \epsilon') dG(\epsilon') \Gamma(dy'; y) \\ \text{s.t. } m' + c &\leq \mathcal{Y}_t(\mathbf{x}; T_t) - \iota \delta d - (1 - \theta)(d - d') \\ m' &\geq 0, \end{aligned}$$

where $d' = (1 - (1 - \iota)\delta)d$ is the depreciated stock after maintenance. The household pays $\iota \delta d$ for maintenance and repays $(1 - \theta)(d - d')$ off of its outstanding credit. In Appendix A, we provide further details about this recursive problem and we explain how we solve it numerically.

off of that is thus an average marginal propensity to spend, as in the literature (footnote 1). We allow for an asymmetric incidence of checks in our general equilibrium model (Section 5).

2.6 Adjustment Hazard and Size-Dependence in the MPX

Having presented the model, we are now ready to discuss the role that the adjustment hazard plays in the size-dependence in the MPX. Following the literature, we will compute the MPX as the average spending response across individuals divided by the size of the check. The empirical counterpart to this MPX is what [Kaplan and Violante \(2014\)](#) refer to as a “rebate coefficient.” We focus momentarily on the marginal propensity to spend on durables since our adjustment hazard is particularly important for durables. Let T be a one-time unanticipated transfer and $\text{MPX}^d(T)$ be the associated average marginal propensity to spend on durables

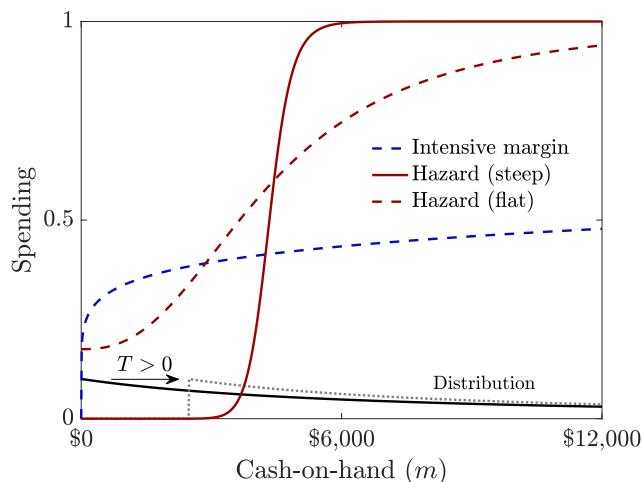
$$\text{MPX}^d(T) \equiv \frac{1}{T} \int \int \underbrace{\mathcal{S}(m, d)}_{\text{extensive}} \underbrace{x(m + d)}_{\text{intensive}} \{d\mu(m - T, d) - d\mu(m, d)\},$$

where $\mathcal{S}(m, d)$ is the adjustment hazard, $x(m + d)$ is spending conditional on adjustment for a household with cash-on-hand m and durable stock d , and μ is the associated distribution. The expression abstracts from the households’ idiosyncratic productivity y to save on notation. Stimulus checks shift the distribution of cash-on-hand in the economy (the last term in the expression). Households spend more on durables as a result. They adjust their stock of durables both at the extensive margin (as captured by the hazard \mathcal{S}) and the intensive margin (as captured by spending conditional on adjustment x).

Figure 2.2 illustrates these two objects as a function of cash-on-hand m , fixing the other states d and y . The figure shows the same two hazards (in red) as in Figure 2.1, with the steeper hazard associated with more state-dependent adjustments. Finally, the spending conditional on adjustment (in blue) is concave due to a standard precautionary savings motive. We also plot the distribution of cash-on-hand (in black). A stimulus check $T > 0$ shifts this distribution to the right (dotted black curve). Households are more likely to adjust their stock of durables (they move along the hazard) and they spend more conditional on adjustment.

The shape of the adjustment hazard is key for the size-dependence in the MPX on durables. To see this, suppose first that the model is purely state-dependent, i.e., \mathcal{S} is discontinuous around some threshold $m^*(d)$. In this case, the extensive margin of adjustment is particularly strong and it dominates the intensive margin

Figure 2.2: Hazard and intensive margin (fixing d and y)



(Section 4.3). The marginal propensity to spend on durables becomes

$$\text{MPX}^d(T) \propto \int \int_{m^*(d)}^{+\infty} \frac{d\mu(m - T, d) - d\mu(m, d)}{T}$$

when the intensive margin is roughly constant. Thus, the marginal propensity to spend on durables *increases* with the size of stimulus checks T when the distribution of cash-on-hand decreases with m (as in the data). The reason is that *proportionately* more and more households are pushed over their adjustment threshold as the check T becomes larger — the conjecture in [Parker et al. \(2013\)](#). Next, consider the opposite polar case where the model is purely time-dependent, i.e., \mathcal{S} is constant. In this case, there is no response at the extensive margin and the intensive margin dominates. After a simple change of variable, the marginal propensity to spend on durables becomes

$$\text{MPX}^d(T) \propto \int \int \{x(m + d + T) - x(m + d)\} d\mu(m, d),$$

and households move along a concave spending function. In this case, the marginal propensity to spend on durables *decreases* with the size of stimulus checks.

These two polar cases illustrate that the shape of the adjustment hazard is key for the size-dependence in the MPX on durables, and hence the total MPX more generally (which includes spending on non-durables too). We will discipline this hazard carefully in the next section by matching several pieces of micro evidence.

3 Bringing the Model to the Data

We interpret durables as consumer durables (cars, appliances, furniture). We assume that our single, composite durable good behaves as cars (in terms of frequency of adjustment, down payment, etc.) since they make up most of the spending on consumer durables. We abstract from housing purchases since these are unlikely to be affected by a stimulus check of a realistic size. Each period in the model corresponds to a quarter. We start by calibrating some parameters externally (Section 3.1), before calibrating internally the most important ones (Section 3.2). Tables 3.1 and 3.2 summarize the parametrization. We discuss alternative parametrizations in Section 4.1. We explain how to solve the model in Appendix A.

3.1 External Calibration

External parameters are set to standard values in the literature. The inverse elasticity of intertemporal substitution is $\sigma = 2$, which is usual in the literature on durables (Berger and Vavra, 2015; Guerrieri and Lorenzoni, 2017). We choose an elasticity of substitution between durables and non-durables of $\nu \rightarrow 1$ to obtain a unitary long-run price elasticity for cars (Berry et al., 2004; Orchard et al., 2022). The quarterly depreciation rate is $\delta = 5\%$. We set θ so the down payment share is 20%, which lies between the estimates of Adams et al. (2009) and Attanasio et al. (2008). The real return on the liquid asset is $r^m = 1\%$ per year and the borrowing spread is $r^b - r^m = 3.5\%$ for auto loans. We assume that idiosyncratic log-productivity follows an AR(1) process as in Berger and Vavra (2015) and McKay and Wieland (2021). We set the persistence of this process so as to obtain an annual persistence of 0.91 (Floden and Lindé, 2001). We set the standard deviation of the innovations to match an annual standard deviation of 0.92 in log-earnings (Auclert et al., 2018). We normalize the earnings process so that aggregate income is 1 at the stationary equilibrium. The elasticity of the tax schedule is $\psi_1 = 0.181$ as in Heathcote et al. (2017), and we choose the intercept $\psi_0 = 0.782$ so the marginal tax rate is 30% at the stationary equilibrium.

Table 3.1: External calibration

Parameter	Description	Value	Source / Target
<i>Preferences</i>			
σ	Inverse EIS	2	Berger and Vavra (2015)
ν	CES parameter	1	Long-run price elasticity
<i>Durables</i>			
δ	Depreciation rate	5%	NIPA
<i>Earnings</i>			
ρ	Persistence	0.977	Floden and Lindé (2001)
γ	Volatility	0.198	Auclert et al. (2018)
ψ_0	Tax intercept	0.782	Average marginal tax rate of 30%
ψ_1	Tax progressivity	0.181	Heathcote et al. (2017)
<i>Financial asset</i>			
θ	Down payment	20%	Adams et al. (2009); Attanasio et al. (2008)
r^m	Return on cash	1%	Real annual Fed funds rate
$r^b - r^m$	Borrowing spread	3.5%	Fed board (G.19 Consumer Credit)

Table 3.2: Internal Calibration

Param.	Description	State-dep.	Our model	Target	Value
β	Discount factor	0.946	0.944	Liquid. / A inc.	26%
ϑ	Non-dur. pref.	0.711	0.687	d / c spending	26%
ι	Maintenance	0.255	0.257	Mainten. ratio	32.6%
κ	Location param.	0.239	0.803	Adjust. frequ.	23.8%
η	Scale param.	0	0.20	See Section 3.2	

Notes: The purely state-dependent model is a version of our model with $\eta \rightarrow 0$. We calibrate $\eta = 0.2$ in our model as we discuss in Section 3.2. All other targets are matched exactly. The sources are described in Section 3.2.

3.2 Internal Calibration

We calibrate five parameters internally: (i) the discount factor β ; (ii) the relative weight on non-durables ϑ_c ; (iii) the maintenance rate ι ; (iv) the location parameter for preference shocks κ ; and (v) the scale parameter for preference shocks η . We choose the discount factor to match an average stock of liquid asset holdings m of 26% of average annual income (Kaplan et al., 2018). We calibrate the relative weight on non-durables to target a ratio of durables to non-durable expenditures $x/c = 0.26$ based on CEX data.¹² We set the maintenance rate to obtain a ratio of maintenance spending to gross investment of 32.6% as in the CEX for cars. We choose the location parameter κ to match an annual frequency of adjustment of 23.8% for vehicles in the PSID, which is in line with conventional estimates (Atanasio et al., 2022; McKay and Wieland, 2021).¹³ The rest of this section describes the calibration of the scale parameter η since it plays an important role in our analysis.

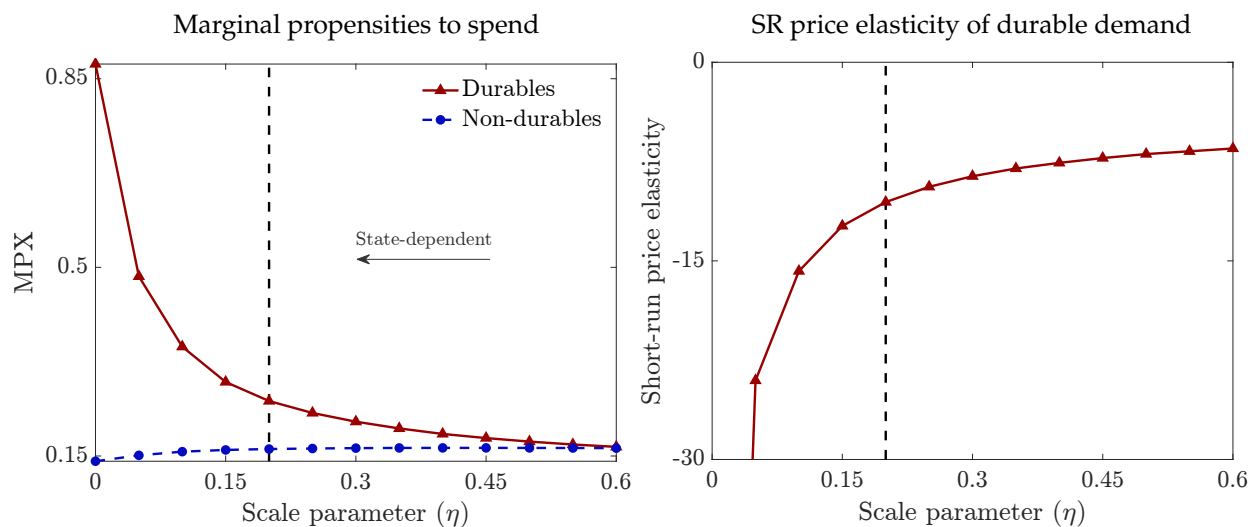
Bounding the scale parameter. The scale parameter η controls the shape of the hazard (2.1) and hence the response of households' durable spending to changes in income and the price of durables (i.e., their user cost). In particular, two moments are especially informative about η : the households' MPX on durables relative to the one on non-durables out of small stimulus checks, and the short-run price elasticity of durables. We show below that these moments provide upper and lower bounds for the scale parameter η . They are natural targets for our calibration too: the MPX controls the spending response to checks in partial equilibrium; and the price (or user cost) elasticity determines how price and interest rate changes dampen this response in general equilibrium.

The left panel of Figure 3.1 shows the marginal propensity to spend on durables and non-durables out of a \$500 check for different values of η . All other parameters are re-calibrated as we change η to match the moments described before. The

¹² As discussed, we exclude housing from both durables and non-durables. Durable spending in the CEX consists of: household furnishings and equipment; vehicle purchases; maintenance and repairs on vehicles; audio and visual equipment and services; and other entertainment supplies, equipment and services. Non-durable spending consists of total spending minus the categories above and housing.

¹³ In Section 3.3, we describe how we estimate the empirical distribution π_k of the duration k between vehicle purchases. The frequency of adjustment is the inverse of the average duration $1 / \sum_{k \geq 0} k \pi_k$.

Figure 3.1: Bounding the scale parameter η



Notes: The left panel plots the marginal propensities to spend (quarterly) out of a \$500 check on durables and non-durables for various values of the scale parameter η in (2.1). These are computed as a rebate coefficient, i.e., the average propensity to spend. The right panel plots the short-run price elasticity of durable demand after a one-quarter increase in the price of durables by 1%. The dashed vertical line is our preferred estimate ($\eta = 0.2$).

lower η , the more state-dependent the model; eventually it converges to the canonical model with (s, S) bands as $\eta \rightarrow 0$. The MPX on durables declines monotonically as η increases and the model becomes more time-dependent. The literature offers a wide range of estimates of the MPX on durables and non-durables; but it is generally agreed that the MPX on durables is larger (Havranek and Sokolova, 2020; Orchard et al., 2022).¹⁴ For this reason, 0.45 is a plausible upper bound for the scale parameter η . That is, the model cannot be *too* time-dependent to match the evidence on the marginal propensity to spend on durables relative to the one on non-durables.

The right panel shows the *short-run* elasticity of durable purchases after a one-quarter transitory increase in the price of durables by 1%. It is well-known that conventional models of durable spending produce an excessively high elasticity

¹⁴ In their meta analysis, Havranek and Sokolova (2020) compile hundreds of micro estimates of the MPX from the literature. Using their data, the average total MPX is 58% across 100 micro estimates at the quarterly frequency from studies that report total spending. In turn, the average MPX on non-durables is 22% across 285 micro estimates at the quarterly frequency from studies that report it. This suggests that the MPX on durables is roughly one and a half times as large as the MPX on non-durables.

of durable demand to changes in the user cost (House, 2014; McKay and Wieland, 2021). This effect is almost entirely driven by the extensive margin of adjustment (McKay and Wieland, 2022). Consistently, the fully state-dependent model with (s, S) adjustments bands ($\eta \rightarrow 0$) predicts an implausibly high elasticity of -90 . Introducing a smooth adjustment hazard is a parsimonious way to dampen this elasticity.¹⁵ There is much uncertainty in the empirical literature about the exact elasticity. Bachmann et al. (2021) find an elasticity of durable purchases of roughly -15 following a short-run decrease in the VAT in Germany.¹⁶ Gowrisankaran and Rysman (2012) estimate a short-run elasticity of -2.55 for camcoders. For this reason, 0.1 is a plausible lower bound for the scale parameter η . That is, the model cannot be *too* state-dependent to match the evidence on the elasticity of durable purchases.

Overall, our preferred value for the scale parameter is $\eta = 0.2$ which is between the lower and upper bounds. This value delivers a total MPX of 42% out of a \$500 windfall. This figure lies between the estimate of 34% in Orchard et al. (2022) and the mean estimate of 58% across micro studies compiled in the meta analysis of Havranek and Sokolova (2020) (footnote 14). The marginal propensity to spend on durables is 25% in our model. This is comparable to the preferred estimate of 30% in Orchard et al. (2022), and it is one and a half times as large as the MPX on non-durables consistently with the meta analysis.¹⁷ We obtain a short-run price elasticity of durables of -10.6 in our calibration, which lies between the existing estimates. We will show that our results are robust to other choices of η in the region $0.1 \leq \eta \leq 0.45$ (Figure 4.2). Moreover, the next section shows that the model with $\eta = 0.2$ matches well other important untargeted moments.

¹⁵ McKay and Wieland (2022) dampen the interest rate elasticity by introducing a combination of low elasticity of intertemporal substitution, low elasticity of substitution between durables and non-durables, various operating costs, exogenous mandatory adjustments, and limited attention.

¹⁶ See Table A.4, columns 3 and 9 in their paper. The literature evaluating the impact of the 2009 Cash for Clunkers program obtains relatively high elasticities too (Mian and Sufi, 2012; Green et al., 2020).

¹⁷ In Appendix D.2, we also consider a Calvo-Plus model. When matching the same short-run price elasticity as in our calibration, the Calvo-Plus model misses the MPX on durables, both in level and relative to the MPX on non-durables.

3.3 Untargeted Moments

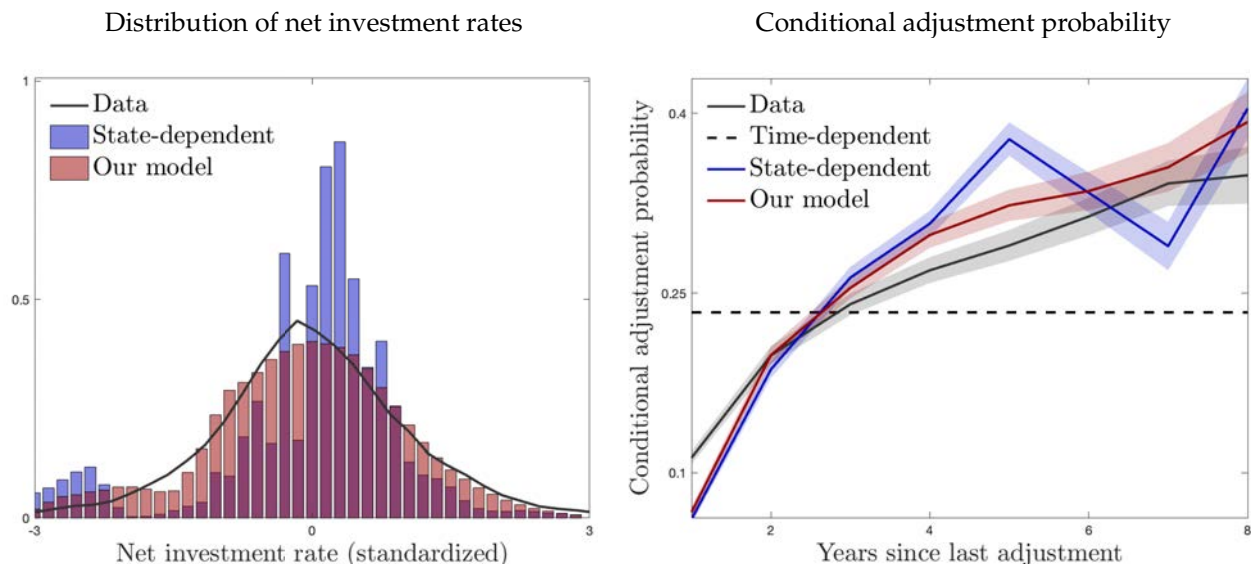
Our calibrated model performs well along several untargeted dimensions. We start by inspecting two moments — the distribution of net investment rates in durables upon adjustment, and the conditional probability of adjustment — which highlight the importance of allowing for a smooth adjustment hazard. We also examine the distribution of MPXs.

Net investment. The left panel of Figure 3.2 plots the empirical distribution of net investment rates in vehicles by households who adjust their stock across two consecutive PSID waves w (in black). To measure net investment, we restrict our sample to household heads (or reference persons) who are male, aged 21 or above, and own at least one vehicle in at least three PSID waves between 1999 and 2019. An adjustment ($\text{Adj}_w = 1$) occurs in two cases. Either the number of vehicles owned by the household changes. Or the household reports that the vehicle that was last purchased (vehicle “#1”) was acquired more recently than the one reported in the previous wave $\text{Purchase}_w^{\#1} > \text{Purchase}_{w-1}^{\#1}$, and at most two years before the interview date $\text{Purchase}_w^{\#1} \geq t_w - 2$ (since the PSID waves are bi-annual). We denote the year of the most recent purchase by Year_w . We measure the net investment rate upon a purchase as $\log(d_w^{\text{net}}) - \log(d_{w-1}^{\text{net}})$ when $\text{Adj}_w = 1$, where d_w^{net} is the value of the stock of vehicles *net* of liabilities reported by the household.¹⁸ Lastly, we standardize the distribution of net investment rates by de-meaning it and normalizing it by its standard deviation (Alvarez et al., 2016a). We trim the top and bottom 1% of the distribution when standardizing.

The left panel of Figure 3.2 also plots the distribution of net investment rates in our model with a smooth adjustment hazard ($\eta = 0.2$, in red) and in a version of our model with only state-dependent adjustments ($\eta \rightarrow 0$, in blue). To ensure that the data and models are comparable, we discretize our model-simulated series into PSID waves and treat those identically to the actual data. We divide time into years, as our model is set up quarterly. For each individual and wave, we compute Year_w as the year of the most recent purchase. The value of the stock of durables

¹⁸ We do not attempt to back out the gross value of the stock by using imperfect information on liabilities, which would add another layer of measurement error. Instead, we directly compute the changes in the net stock, and we treat the model-generated data identically. Note that $\log(d_w^{\text{net}}) - \log(d_{w-1}^{\text{net}})$ is exactly equal to net investment rate in the model when the price of durables is constant.

Figure 3.2: Untargeted moments



Notes: The left panel plots the distribution of net investment rates (standardized) across two consecutive PSID waves between which households adjusted their stock of durables. The black curve is the data, while the red and blue bars are our calibrated model ($\eta = 0.2$) and a version with purely state-dependent adjustments ($\eta \rightarrow 0$), respectively. The right panel plots the adjustment probability conditional on a household not having adjusted so far. The black, red and blue curves are the same models as on the left panel. The dashed black curve is a version of our model with purely time-dependent adjustments ($\eta \rightarrow +\infty$). The confidence intervals are bootstrapped (10%).

in the simulated PSID w is $d_{T(w)}$, where $T(w)$ is the last quarter in that wave. The value *net* of credit is $d_w^{\text{net}} \equiv \theta d_{T(w)}$ in the model.

Our calibrated model produces a bell-shaped distribution that resembles the one in the data. Crucially, our model matches well the tails of the distribution — an important moment in models with lumpy adjustment (Alvarez et al., 2016a). In contrast, the purely state-dependent model fails to reproduce the empirical distribution.¹⁹ There are too few negative adjustments and most adjustments are concentrated around the same value.²⁰

Probability of adjustment. The right panel of Figure 3.2 plots (in black) the empirical

¹⁹ In Appendix D.2, we also consider a Calvo-Plus model. We find that this model also fails to reproduce the empirical distribution of net investment rates.

²⁰ The empirical distribution might contain some measurement error, i.e., households over- or under-estimating the value of their cars for instance. To account for this possibility, we conducted an experiment where we introduced a measurement error of 10% in the model-generated investment sizes. The overall shapes of the resulting distributions are essentially unchanged compared to the left panel of Figure 3.3.

probability that a household adjusts its stock of vehicles after a certain number of years *conditional* on not having adjusted so far (Alvarez et al., 2021), which is also known as the Kaplan-Meier hazard. We construct this conditional probability using the purchase dates Year_w as follows. The duration between two consecutive purchases is given by $\text{Duration}_w = \text{Year}_w - \text{Year}_{w-2}$ whenever an adjustment occurs ($\text{Adj}_w = 1$). We restrict attention to the first purchase by a given household.²¹ This yields an empirical probability distribution π_k over durations $k = 1, 2, \dots$ expressed in years. Following Alvarez et al. (2021), we compute the conditional probability of adjustment as

$$\text{Prob}_k = \frac{\pi_k}{1 - \sum_{j < k} \pi_j}.$$

The right panel of the figure compares the empirical probability (in black) to the one implied by our model ($\eta = 0.2$, in red) and two alternative calibrations with, respectively, purely time-dependent adjustments ($\eta \rightarrow +\infty$, dashed) and state-dependent adjustments ($\eta \rightarrow 0$, in blue). The conditional probability is flat in the purely time-dependent model. On the contrary, the data suggests that vehicle adjustments are fairly state-dependent. This is intuitive: the longer a household owns a car and the more it depreciates, the more likely it is that the household will adjust next period. The model with $\eta = 0.2$ matches the empirical profile quite well.²² The overall pattern is roughly similar in the purely state-dependent model ($\eta \rightarrow 0$), although the fit becomes somewhat poorer as the horizon increases. Overall, this confirms that our calibrated model retains a substantial degree of state-dependence. This also means that the conditional probability of adjustment is only a *partially* informative moment. It allows us to rule out very large values of η (a strong time-dependence), as did the evidence on the relative marginal propensity to spend on durables (left panel of Figure 3.1). But it does not allow us to discriminate between lower values of η . Very low values of η are instead ruled out by the evidence on the price elasticity (right panel of Figure 3.1)

²¹ The reason is that subsequent purchases, if observed in the PSID's relatively short time dimension, are more likely to be of shorter duration which would bias our estimates. Focusing on the first adjustment allows us to circumvent this issue.

²² Note that the model matches the *average* probability, by construction. The reason is that we target the empirical frequency of adjustment in our calibration, which is computed using the empirical probability of adjustment. The model's success lies in the fact that it matches the *profile* well.

as well as the evidence on the distribution of net investment rates (left panel of Figure 3.2).

Annual MPX. The model delivers an annual marginal propensity to spend of 40% on durables, and 52% on non-durables out of a \$500 check. The total MPX is 92%, which is comparable to the estimates of Fagereng et al. (2021) out of small lottery gains in Norway (most gains are much larger). We obtain an annual MPX of 67% out of the mean lottery gain in their sample (\$9,240). This value lies between their benchmark (truncated) estimate of 51% and their untruncated estimate of 72%.²³ The latter is more comparable to our value since we do not trim the distribution of MPXs in the model. We report the dynamic responses (or intertemporal MPXs in the language of Auclert et al., 2021) in Figure C.1 in Appendix C.1. The time profile out of a check of the same size as the mean lottery gain in Fagereng et al. (2021) lines up closely with their estimates.

Share of hand-to-mouth. We find that 42% of households are hand-to-mouth, i.e., their holdings of liquid assets are less than half of their monthly (gross) income (Kaplan et al., 2014). While untargeted, this figure turns out to be almost exactly identical to the estimates of Kaplan and Violante (2022) and Aguiar et al. (2023).

Secondary market. Our model makes no distinction between old and new durables.²⁴ However, suppose that households who adjust their stock of durables (upward or downward) first *sell* their existing stock. Part of households' gross purchases is then fulfilled by old durables on the secondary market. Under this assumption, used durables account for 53% of gross purchases. For comparison, used cars represent roughly 55% of total spending on cars in the US (Department of Transportation, 2023).²⁵

²³ For comparison, Golosov et al. (2021) find an annual MPX of roughly 60% in their sample of US lottery winnings of at least \$30,000.

²⁴ In particular, they have the same depreciation rate and households value them equally. Gavazza and Lanteri (2021) model the secondary market explicitly by allowing older cars to have a lower perceived quality.

²⁵ About 70% of car sales in the US involve a used car. However, used cars are cheaper than new ones in the data and hence account for a smaller share of total spending on cars. Modelling the secondary market explicitly by allowing for a quality ladder is beyond the scope of this paper.

Distribution of MPX. Figure C.2 in Appendix C plots the distribution of total MPXs produced by our model. We also compare this distribution to the ones produced by a purely state-dependent version of our model and by a two-asset model of non-durable spending similar to one in Kaplan and Violante (2022).²⁶ The distribution of MPXs is skewed in our model and has a relatively long right tail. The overall shape of the distribution is consistent with the evidence in Fuster et al. (2021) and Lewis et al. (2022). In particular, a non-negligible share of households displays an MPX close to (or above) 1.²⁷ Lumpy adjustment and households’ ability to pay only a fraction of the price as a down payment make such high MPXs possible. Turning to the purely state-dependent version of our model, the distribution of MPXs is bi-modal (with a second mode around 0.5), which is expected in a model with (s, S) adjustment bands. Finally, the two-asset model of non-durables struggles to generate MPXs larger than 1 as observed in the data.

3.4 State- vs. Time-Dependent Adjustments

The previous section showed that our calibrated model has both state- and time-dependent features. Having calibrated the model, we can now quantify the degree of state-dependence more formally.

In the purely state-dependent model, durable adjustment is deterministic conditional on the household’s idiosyncratic state \mathbf{x} , and it results exclusively from movements in \mathbf{x} along the state space. In the purely time-dependent model, durable adjustment is purely random and unrelated to \mathbf{x} . In our model, adjustment occurs $\mathcal{A}(\mathbf{x}; \psi) = 1$ if $\psi \leq \mathcal{S}(\mathbf{x})$, where $\mathcal{S}(\mathbf{x})$ is the adjustment hazard (2.1) and ψ is distributed uniformly on the line $[0, 1]$. No adjustment occurs $\mathcal{A}(\mathbf{x}; \psi) = 0$ otherwise.

Accordingly, we introduce the following measure of state-dependence

$$\text{State-dependence (SD)} \equiv \frac{\text{share with } \mathcal{A}(\mathbf{x}'; \psi) = 1 \text{ and } \mathcal{A}(\mathbf{x}; \psi) = 0}{\text{share with } \mathcal{A}(\mathbf{x}'; \psi') = 1 \text{ and } \mathcal{A}(\mathbf{x}; \psi) = 0} \quad (3.1)$$

where households are tracked over consecutive periods as they move along the state space from \mathbf{x} to \mathbf{x}' and switch from a draw ψ to ψ' . Households decide to adjust for two reasons: either because they moved to \mathbf{x}' or because they got a par-

²⁶ We describe the two-asset model of non-durables in Appendix D.1.

²⁷ Figure C.3 in Appendix C breaks down the MPX by quartile of the distribution of liquid assets.

ticular draw ψ' . Our measure of state-dependence captures the share of adjustments that occur *exclusively* for the first reason. By definition, $SD = 1$ in the purely state-dependent model, and $SD = 0$ in the purely time-dependent model.

We plot our measure of state-dependence in Figure C.4 in Appendix C, as a function of the scale parameter η . All other parameters are re-calibrated as we change η . We repeat this experiment at the quarterly and annual frequencies. As anticipated in Section 2.2, the model becomes less state-dependent as η increases. In our preferred calibration ($\eta = 0.2$), roughly 23% (50%) of all adjustments during a quarter (year) occur due to changes in households' idiosyncratic state \mathbf{x} . In both cases, our state-dependence index is rather flat around our preferred calibration value ($\eta = 0.2$). This will help explain why the size-dependence in the MPX is not very sensitive to changes in η around this value (Figure 4.2).

4 Size-Dependence in the MPX

We now quantify how the MPX varies as stimulus checks become larger (Section 4.1). We compare this size-dependence to previous estimates in the literature, and highlight the role of our smooth adjustment hazard (Section 4.2). We then discuss the role of the extensive margin (Section 4.3), and how aggregate conditions affect the MPX (Section 4.4).

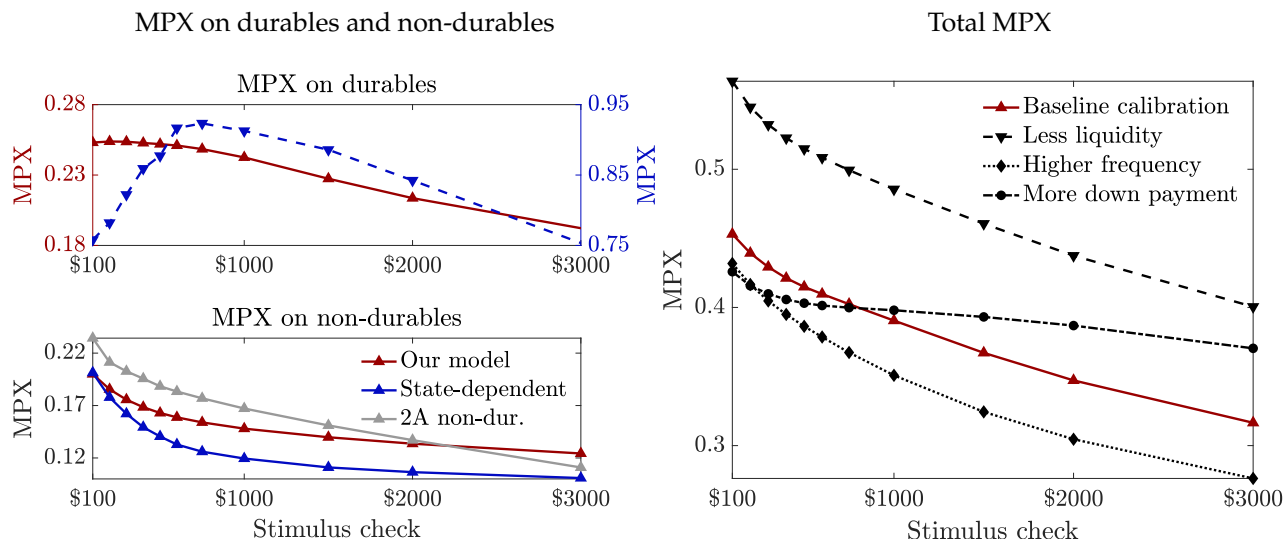
4.1 Durables, Non-Durables, and the Total MPX

The left panel of Figure 4.1 plots the marginal propensities to spend on durables and non-durables at the quarterly frequency following stimulus checks of varying sizes (red curves).²⁸ We also plot the MPXs in a purely state-dependent version of our model (in blue) and in a canonical two-asset model of non-durables similar to Kaplan and Violante (2022) (in grey).²⁹

²⁸ Stimulus checks are used to stimulate the economy in the short-run. The recessions during which they are sent can be relatively short. For instance, the 2001 recession lasted only 8 months, and the 2020 recession lasted 2. This explains our focus on quarterly responses. Figure C.1 in Appendix C plots the dynamic responses, i.e., beyond the first quarter. Annual responses also exhibit a meaningful degree of size-dependence (Figure C.5 in Appendix C), as discussed in Section 3.3. All responses are computed starting from the stationary equilibrium. We explore the role of aggregate conditions in Section 4.4.

²⁹ Again, we describe the two-asset model of non-durables in Appendix D.1.

Figure 4.1: Size-dependence in the MPX



Notes: The left panel plots the MPX on durables and non-durables at the quarterly frequency as a function of the size of stimulus checks. The red curves are our model. The blue curves are a purely state-dependent version of our model. The grey curve is a canonical two-asset model of non-durables. The right panel plots the MPX as a function of the size of the checks in our model and in three alternative calibrations with lower liquidity (13% of annual income instead of 26%), more down payment ($\theta = 30\%$ instead of $\theta = 20\%$), and higher frequency of adjustment (35% instead of 25%).

Starting with durables, we find that the MPX is essentially flat in our model over the range \$100 to \$600, and then it declines slowly. In particular, the MPX on durables does not surge with the size of stimulus checks, as sometimes conjectured in the literature (Parker et al., 2013). This contrasts with a purely state-dependent version of our model where the MPX starts much higher (as in Figure 3.1) and does increase substantially at first. We explain this difference in Section 4.3 when discussing the role of the extensive margin of adjustment.

Turning to non-durables, the MPX declines more rapidly in our model compared to durables. The MPX on non-durables out of \$2,000 is about 1/3 lower than the one out of \$100, whereas the MPX on durables is only 15% lower. In contrast, the canonical two-asset model of non-durables produces a MPX on non-durables that declines much faster relative to our model: the response is essentially halved when comparing a \$100 and \$2,000 check. This partly reflects the complementarity between durables and non-durables which is absent from the two-asset model of non-durables. As checks become larger, households spend more on durables

in our model, and this raises the marginal utility of consuming non-durables and the associated MPX. Note that in the purely state-dependent model, however, the initial surge in the MPX on durables is so strong that the MPX on non-durables actually declines faster initially relative to our model.

The right panel plots the total MPX (the sum of the MPXs on durables and non-durables) in our model as a function of the size of stimulus checks (red curve). We find that the MPX declines slowly with the size of stimulus checks, and it remains elevated even for large checks. For instance, the MPX decreases by a fourth when comparing \$100 and \$2,000 checks. As we discuss in the next section, the total MPX starts between the ones in the purely state-dependent version of our model and the two-asset model of non-durables, and it declines at a rate that also lies between these two models.³⁰ In particular, the total MPX is almost constant when comparing \$100 and \$2,000 checks in the purely state-dependent model, as the changes in the MPX on durables and on non-durables offset each other. In contrast, the MPX is almost halved in the canonical model of non-durables when comparing the same amounts.

Sensitivity. Finally, we perturbate various parameters to explore how they affect our results. The right panel of Figure 4.1 plots the total MPX as a function of the size of stimulus checks for three alternative calibrations. To make sure that all the models are comparable, we calibrate the scale parameter η to match the same short-run price elasticity (Figure 3.1). All other parameters are re-calibrated to match the targets discussed in Section 3.2.

The first alternative calibration reduces the amount of liquidity in the economy by a factor 2, from 26% of annual income in our benchmark calibration to 13%. This value lies between the mean and median holdings of liquid assets measured by Kaplan and Violante (2022). As expected, this raises the *level* of the MPX,

³⁰ The *rate* at which the MPX changes (not its absolute change) is the relevant metric to assess how quickly the effect of stimulus checks wears off as they become larger. For instance, suppose that the MPX declines from 45% to 35% when comparing checks of \$100 and \$2,000 (as in our model). Then, spending increases by \$655 as the check becomes larger since $\Delta \text{Spending} \equiv \text{MPX} \times T$. Instead, suppose that the MPX declines from 23% (as in the non-durables model) to 13% for the same checks. The absolute decline is the same across scenarios, but the rate of decline is different. In the second scenario, spending increases by a mere \$237 (less than half the increase in our model). Accordingly, we use the *elasticity* of the MPX with respect to T in the next section to compare the size-dependence across models.

but the overall profile is mostly unchanged. The second calibration increases the frequency of adjustment to 35% instead of 25%. The level of the MPX and its size-dependence are essentially unchanged. The third calibration increases the down payment to 30% instead of 20%. In this case, the MPX declines much more slowly, as larger stimulus checks provide households with the down payment to purchase durables. Figure C.6 in Appendix C breaks down these responses between durables and non-durables.

4.2 Concavity in the Spending Response

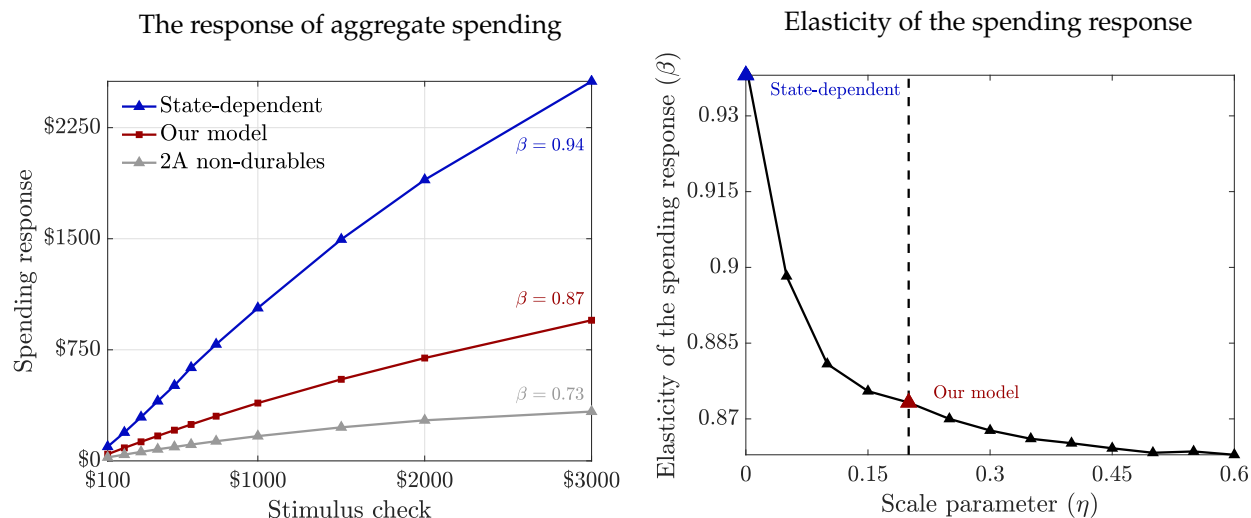
The left panel of Figure 4.2 plots the response of aggregate spending as a function of the size of stimulus checks in the three models that we have discussed so far. The concavity in this function reflects the size-dependence in the MPX. To compare this size-dependence across models in a parsimonious way, we compute the elasticity β of the spending response with respect to the size of checks. Specifically, we fit a parametric function $\Delta\text{Spending} = \alpha T^\beta$ over the range \$100 to \$3,000, where β is the elasticity of interest. The lower β , the more concave the spending response, and the faster the MPX declines with the size of checks ($1 - \beta$ is the rate at which it declines).³¹ The left panel of Figure 4.2 also indicates the elasticity β for each model.

Our model (in red) predicts that large checks remain effective at stimulating aggregate spending. The elasticity is $\beta = 0.87$ in our preferred parameterization with $\eta = 0.2$: the spending response is somewhat concave but it remains robust as stimulus checks become larger. In contrast, the two-asset model of non-durables (in grey) predicts that the effect of checks wears off rapidly as they become larger. Beyond \$2000, larger checks become essentially ineffective at boosting aggregate spending further. The spending response is very concave in the size of checks, with an elasticity $\beta = 0.73$. That is, the MPX declines at a rate $1 - \beta$ that is twice as fast in the non-durables model relative to ours. Finally, a purely state-dependent model of durables (in blue) predicts a much stronger and more linear response. The elasticity $\beta = 0.94$ is much closer to unity in this model with $\eta \rightarrow 0$.³² That is,

³¹ By definition, $\text{MPX} \equiv \Delta\text{Spending}/T$ so $\beta - 1$ is elasticity of the MPX with respect to T and $1 - \beta$ is the rate at which the MPX declines. This rate of decline is the relevant metric to compare the size-dependence across models (footnote 30).

³² Berger et al. (2023) build a purely state-dependent model of housing purchases. To compute total

Figure 4.2: Spending response



Notes: The left panel plots the response of aggregate spending as a function of the size of stimulus checks. The red curve is our model. The blue curve is a purely state-dependent version of our model. The grey curve is a canonical two-asset model of non-durables. The right panel reports the elasticity β (see text) as a function of the scale parameter η . All other parameters are re-calibrated to match the targets discussed in Section 3.2. The vertical dashed line is our preferred calibration with $\eta = 0.2$.

the MPX declines at half the rate compared to our model with $\eta = 0.2$.

What role does the smooth adjustment hazard play in the size-dependence in the MPX in our model? The right panel of Figure 4.2 reports the elasticity β as we vary the scale parameter η . The spending response becomes more concave as the scale parameter η (and hence time-dependence) increases. However, the elasticity β is relatively flat around our preferred calibration $\eta = 0.2$. In other words, the size-dependence in our model is robust to changes in η between the lower bound ($\eta = 0.1$) and the upper bound ($\eta = 0.45$) discussed in Section 3.2.³³

4.3 Decomposing the MPX on Durables

The smooth adjustment hazard in our model dampens the extensive margin of adjustment. To understand how it affects the size-dependence in the MPX, we

spending, they add non-durable spending and the imputed service flow from housing. While not the focus of their paper, they find in a numerical experiment that the marginal propensity to consume declines more slowly compared to a canonical model of non-durables.

³³ Changes in the scale parameter within these bounds still affect the level of the MPX and the other moments discussed in Section 3. We prefer $\eta = 0.2$ for the reasons discussed in that section.

decompose the marginal propensity to spend on durables into its extensive and intensive margins as follows

$$\begin{aligned} \text{MPX}^d(T) = & \underbrace{\frac{\int \overbrace{\{\mathcal{S}_0(d, m+T, y) - \mathcal{S}_0(d, m, y)\}}^{\# \text{ of marginal adjusters}} \times \overbrace{x(d, m, y)}^{\text{selection}} \times d\mu(\mathbf{x})}{T}}_{\text{Extensive margin}} \\ & + \underbrace{\frac{\int \mathcal{S}_0(d, m, y) \times \{x(d, m+T, y) - x(d, m, y)\} \times d\mu(\mathbf{x})}{T}}_{\text{Intensive margin}} + \text{res} \quad (4.1) \end{aligned}$$

The extensive margin captures changes in the durable adjustment hazard \mathcal{S} , holding fixed the policy function conditional on adjustment. The intensive margin captures the change in this policy function, holding the hazard fixed. The residual “res” captures the non-linear interaction between the two margins.

The left panel of Figure C.7 in Appendix C plots these three components as a function of the size of stimulus checks in our model. The intensive and extensive margins contribute to the MPX on durables in roughly the same proportions in our model. This contrasts with a purely state-dependent model where the extensive margin dominates (right panel of Figure C.7). The intensive margin declines in our model as the stimulus checks become larger due a standard precautionary savings motive. Perhaps surprisingly, the extensive margin declines as well. Figure C.8 in Appendix C shows that more and more households are pushed into adjustment as stimulus checks become larger, initially at a constant rate and eventually at a lower pace. Overall we find that increasing the size of stimulus checks from \$100 to \$3,000 increases the mass of adjusters by 2.5% or so, which is broadly consistent with the survey evidence from Fuster et al. (2021). The decline in the pace at which households adjusts accounts for most, but not all the decrease in the extensive margin. There is a selection effect too: households who do not adjust unless they receive a large check value durables less and thus buy a smaller one.³⁴ The residual is smaller than the other components. However, its contribution rises with the size of stimulus checks as late adjusters are poorer on average and have higher marginal propensities to spend.

³⁴ This selection effect is well known in the price setting literature (Golosov and Lucas, 2007).

4.4 Aggregate Conditions

Finally, we explore how aggregate conditions affect the MPX in our model. The left panel of Figure C.9 in Appendix C plots the MPX out of \$500 at various points of the business cycle. The stimulus checks are received unexpectedly after three quarters of constant expansion or contraction, followed by a linear mean-reversion over eight quarters. The MPX is mildly countercyclical: it tends to be larger in recessions, and even more so in deeper ones. This prediction is in line with the evidence of Gross et al. (2020) and Baker et al. (2018). In contrast, a purely state-dependent model predicts a sharp decline in the MPX in deeper recessions (right panel of Figure C.9) through the mechanism proposed by Berger and Vavra (2015).

5 Stimulus Checks in General Equilibrium

In the rest of this paper, we evaluate the effect of stimulus checks in general equilibrium. We start by embedding our model of households' spending into an open-economy heterogeneous-agent New-Keynesian model (Section 5.1). Our model accounts for various forces that can dampen the effect of stimulus checks. We describe the parameterization in Section 5.2. We quantify the general equilibrium response to stimulus checks in Section 5.3. We allow for supply shocks and richer inflation dynamics in Section 5.4. We provide more details in Appendix B.

5.1 Environment

The economy has two sectors. The first produces a non-durable good and the second an investment good. The non-durable good can be used for consumption or as an intermediate for producing the investment good. The investment good can be used to build up the stock of durables or capital. The non-durable good is produced with labor. The investment good is produced with non-durables (as in McKay and Wieland, 2021), or with capital.

Households. The household block of the economy is identical to the one introduced in Section 2. The only difference is that we allow for relative price movements between durables and non-durables and inflation over time, as well as imports and exports of goods.

Households import part of their non-durable and investment goods.³⁵ Non-durable consumption c_t and investment x_t are given by

$$c_t = \left[\sum_{j \in \{H,F\}} \left(\alpha_j^c \right)^{\frac{1}{\rho}} \left(c_t^j \right)^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1}} \quad \text{and} \quad x_t = \left[\sum_{j \in \{H,F\}} \left(\alpha_j^d \right)^{\frac{1}{\rho}} \left(x_t^j \right)^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1}}, \quad (5.1)$$

where c_t^H and c_t^F are the consumptions of the home and foreign non-durable goods, respectively, and the weights $\alpha_H^c + \alpha_F^c = 1$ capture the corresponding spending shares. The terms x_t^j and α_j^d are defined similarly for investment in durables. In the following, we let P_t^c and P_t^d denote the price of the consumption and investment baskets (5.1) expressed in terms of the home non-durable good. All other prices and real quantities are also expressed in terms of the home non-durable good (Appendix B.1).

The demands from the rest of the world are similar to (5.1). *Total* consumption of non-durables c_t^* and investment in durables x_t^* in the rest of the world are constant and equal to the steady state levels at home, so there are no net imports in steady state. However, countries can run a current account surplus or deficit after an aggregate shock. Domestic and foreign prices are normalized to 1 at the initial stationary equilibrium. Foreign nominal prices are fixed throughout. Finally, the nominal exchange rate is pinned down by purchasing power parity in the long-run, and uncovered interest rate parity during the transition (Appendix B.1).

Non-durable goods. A firm produces non-durables using labor. Inflation in the price of the non-durable good (π_t) follows a Phillips curve

$$\pi_t = \kappa \log \left(\frac{Y_t^{\text{dom}}}{Y_t^{\text{potent}}} \right) + \beta \pi_{t+1}, \quad (5.2)$$

where Y_t^{dom} is the aggregate demand for the non-durable good, Y_t^{potent} is potential output in that sector, and $\kappa > 0$ is the slope of the Phillips curve.³⁶

³⁵ For instance, foreign goods account for a fourth of US durable expenditure. Allowing for imports dampens the equilibrium response of output to stimulus checks since some spending leaks abroad.

³⁶ See McKay and Wieland (2021) for a microfoundation. This Phillips curve can result from sticky prices or wages. Distinguishing between the two would require taking a stance on workers' labor

Investment goods. A firm can produce $F(M) = A_0 M^{\frac{\zeta}{1+\zeta}}$ units of the investment good using M units of non-durables as in [McKay and Wieland \(2021, 2022\)](#), where $1/\zeta > 0$ governs the decreasing returns in production and $A_0 > 0$ is productivity.

We assume that the firm can also produce the investment good using capital. This allows us to introduce investment shocks that act as aggregate demand shifters in a tractable way.³⁷ Specifically, we assume that the firm can use K_{t-1} units of capital to produce $A_1 K_{t-1}$ units of the investment good, where $A_1 > 0$ is productivity. New capital is produced with investment goods too. The stock of capital evolves as

$$K_t = \left\{ 1 - \delta^K + \Phi(I_t/K_{t-1}) + z_t \right\} K_{t-1}, \quad (5.3)$$

with initial condition $K_{-1} = K$ at the steady state, where I_t is investment, δ^K is the depreciation rate of capital, and $\Phi(x)$ is the investment technology which is increasing and concave.³⁸ As in [Brunnermeier and Sannikov \(2014\)](#), the shocks $\{z_t\}$ are a source of aggregate fluctuations in our economy.

The firm maximizes its value and smoothes the dividends Div_t that it disburses to households ([Leary and Michaely, 2011](#)). This ensures that investment shocks affect households' incomes in (5.9) and hence their aggregate spending.³⁹ Profit maximization implies that, in equilibrium, the relative price of the investment good is

$$p_t^d \equiv \left(\frac{X_t^{\text{dom}}}{X_t^{\text{potent}}} \right)^{1/\zeta}, \quad (5.4)$$

where X_t^{dom} is the aggregate demand for durables produced domestically and X_t^{potent} is potential output in that sector. The potential outputs Y_t^{potent} and X_t^{potent}

supply, which is not the focus of this paper. We consider an alternative, non-linear Phillips curve in Section 5.4.

³⁷ Firms investment shocks are a key driver of US business cycle fluctuations ([Justiniano and Primiceri, 2008](#); [Auclert et al., 2020](#)). Beyond their importance in the data, investment shocks also allow us to compute efficiently the sequence of shocks that produce a given recession of interest despite the non-linearities inherent to the demand side of our economy (Appendix B.3).

³⁸ This specification with a linear production function and a concave investment technology is common in the asset pricing literature ([Jermann, 1998](#); [Brunnermeier and Sannikov, 2014](#)).

³⁹ Absent dividend smoothing, an increase in investment raises output but not incomes when output is demand-determined, as is evident from (5.9). We describe the dividend smoothing in more detail when we discuss the parametrization (Section 5.2).

in (5.2) and (5.4) capture sectoral productivities (Appendix B.2). In Section 5.4, we allow for shocks to these potential outputs which can be inflationary. In the following, we let $\hat{y}_t \equiv \log(Y_t^{\text{dom}}/Y_t^{\text{potent}})$ and $\hat{x}_t \equiv \log(X_t^{\text{dom}}/X_t^{\text{potent}})$ denote the sectoral output gaps.

Policy. The government sends nominal stimulus checks to eligible households in the first period. We assume that households who earned less than \$75,000 in the previous year are eligible to receive a check. The check decreases linearly with income after that and reaches zero at \$80,000.⁴⁰ The government's flow budget constraint is

$$B_t^g + P_t^c G_t + t_t = \frac{1 + r_t}{1 + \pi_t} B_{t-1}^g + \mathcal{T}_t + \Sigma_t, \quad (5.5)$$

where B_t^g are real asset holdings, G_t is government spending on non-durables, t_t are real stimulus checks, $\mathcal{T}_t \equiv \int (yY_t^{\text{inc}} - \psi_{0,t}(yY_t^{\text{inc}})^{1-\psi_1}) d\mu_{t-1}$ are the revenues from progressive income taxation (Heathcote et al., 2017) with Y_t^{inc} denoting households' aggregate real income, and Σ_t are credit payments from households.⁴¹ As in our baseline calibration, the government maintains a constant ratio of debt to output at the stationary equilibrium. Its real spending $G > 0$ on domestic goods balances the budget (5.5) in steady state. In period $t = 0$, the government sends a one-time nominal stimulus check to eligible households. These checks are deficit-financed. In later periods $t > 0$, the government maintains a constant spending $G_t = G > 0$ and repays its new debt over time by raising the tax intercept $\psi_{0,t}$ as we explain in Section 5.2.

Monetary policy follows a standard rule

$$r_t^m = \max \{ r^m + \phi_{\Pi} \pi_t, \underline{r} \}, \quad (5.6)$$

where r^m is the steady state interest rate on the liquid asset, ϕ_{Π} is the coefficient on inflation, and \underline{r} is the effective lower bound.⁴²

⁴⁰ This distribution of checks mimicks the one observed in 2020–2021. We assume that mean annual income is \$67,000 at the steady state, as in Kaplan and Violante (2022).

⁴¹ Instead of assuming that the government claims Σ_t , we could have introduced a separate financial sector. We assume that the government spends G_t on domestic and foreign varieties using the same aggregator (5.1) as the households.

⁴² We assume that the Taylor coefficient on the output gap is zero, as in Auclert et al. (2021). We also assume that monetary policy responds to inflation in non-durables π_t , as in McKay and Wieland (2022), since this is the only good produced with labor. We have experimented with a version

Outputs and incomes. Market clearing requires that the amounts spent on the non-durable and durable goods equal the value of the production in these sectors

$$P_t^c (C_t + G_t) + F^{-1} \left(X_t^{\text{dom}} \right) + \text{NX}_t^{c,\text{real}} = Y_t^{\text{dom}}, \quad (5.7)$$

and

$$P_t^d X_t + p_t^d I_t + \text{NX}_t^{d,\text{real}} = p_t^d \left(X_t^{\text{dom}} + A_1 K_{t-1} \right), \quad (5.8)$$

where C_t and X_t are the households' aggregate demands for the non-durable and investment good, respectively, $F^{-1} \left(X_t^{\text{dom}} \right)$ is the demand for intermediates used to produce X_t^{dom} units of the investment good, $\text{NX}_t^{c,\text{real}}$ and $\text{NX}_t^{d,\text{real}}$ are real net exports (Appendix B.1), and Y_t^{dom} and $X_t^{\text{dom}} + A_1 K_{t-1}$ are the sectoral outputs.⁴³

Households' aggregate income before interest and tax payments Y_t^{inc} is

$$Y_t^{\text{inc}} = Y_t^{\text{dom}} + \text{Div}_t, \quad (5.9)$$

where Y_t^{dom} are the payments from the firm producing the non-durable good and Div_t are the dividends disbursed by the firm producing the investment good.⁴⁴ Households' real net income before interest payments is

$$E_t^{\text{net}}(\mathbf{x}) = \psi_{0,t} \left(y Y_t^{\text{inc}} \right)^{1-\psi_1}, \quad (5.10)$$

where y still captures idiosyncratic income shocks, and $\psi_{0,t}$ and ψ_1 parametrize the non-linear tax schedule.

Finally, we will compute aggregate output as a quantity index

$$Y_t^{\text{GDP}} \equiv C_t + X_t + G_t + I_t + \text{TB}_t \quad (5.11)$$

using steady state prices ("chained dollars"), where TB_t is the quantity index for the trade balance (Appendix B.1).

where the rule (5.6) depends on CPI (or PPI inflation) instead of non-durable inflation π_t , and obtained similar results.

⁴³ Households' consumption C_t and investment in durables X_t and government spending G use both the local and foreign goods. On the contrary, the firm's investment I_t uses local goods only. Hence the different price indices in (5.8).

⁴⁴ Households claim the revenue of the firm producing non-durables. We do not make a distinction between the wage bill and profits of that firm for the reasons discussed in footnote 36.

5.2 Parametrization

As in our baseline calibration (Section 3), the real interest rate is $r^m = 1\%$ at the stationary equilibrium, aggregate income is $Y_t^{\text{inc}} \equiv 1$, the government maintains a constant ratio of debt to annual aggregate income of 26%, and the tax intercept ψ_0 ensures that the marginal tax rate is 30% in the long-run. Households import 23% of their durable spending at the steady state, and 19% of their non-durable spending (Hale et al., 2019). We set the elasticity of substitution between home and foreign varieties to $\rho \rightarrow 1$. This value lies between the short-run and long-run estimates of Boehm et al. (2023). We normalize the productivity A_0 in the sector producing the investment good so the relative price of durables is $p^d \equiv 1$ at the initial steady state. The investment technology is $\Phi(x) = 1/\phi(\sqrt{1+2\phi x} - 1)$ with $\phi \equiv 2$ as in Brunnermeier and Sannikov (2014). The productivity of the investment firm A_1 is chosen so there is no long-run growth.⁴⁵ The slope of the Phillips curve is $\kappa = 0.0031$ based on the evidence of Hazell et al. (2022).⁴⁶ For now, we focus on the case $\zeta \rightarrow +\infty$ where the relative price of durables is acyclical. We allow for relative price movements and a non-linear Phillips curve in Sections 5.3–5.4.⁴⁷ The Taylor coefficient on inflation is $\phi_\Pi = 1.5$. The effective lower bound on the interest rate is 3 percentage points lower than the steady state interest rate r^m , assuming a 3% nominal return on the liquid asset. Therefore, we set the effective lower bound to $\underline{r} = -2\%$. The government finances the stimulus checks by issuing debt. It repays this debt slowly by raising the tax intercept $\psi_{0,t}$ uniformly over 15 years and letting it decay to its long-run value ψ_0 over the next 5 years. Similarly, the firm producing the investment good disburses dividends Div_t uniformly over 15 years, and then lets them decay back to their long-run level over the next 5 years.

⁴⁵ This is standard in models with AK technology. We normalize the level of capital in steady state to $K \equiv 1$.

⁴⁶ Hazell et al. (2022) find that the slope of the Phillips curve is -0.0062 in terms of unemployment since 1980. The semi-elasticity of unemployment with respect to output is roughly -0.5 over the same period.

⁴⁷ Empirically, the relative price of new consumer durables is essentially acyclical, even when using transaction prices (instead of sticker prices) as in CPI data (McKay and Wieland, 2021; Cantelmo and Melina, 2018). Section 5.3 allows for relative price movements. In this case, the effect of stimulus checks wears off more rapidly as they become larger.

5.3 The Response to Stimulus Checks in General Equilibrium

We are now ready to quantify the effect of stimulus checks in general equilibrium. The economy experiences a demand-driven recession due to investment shocks $\{z_t\}$. We engineer these shocks so that aggregate output falls by 4% over three quarters, and then recovers linearly over the next two years (Appendix B.3). Starting from this recession, the government sends a nominal stimulus check in the first quarter to eligible households. We repeat this experiment for checks of various sizes.

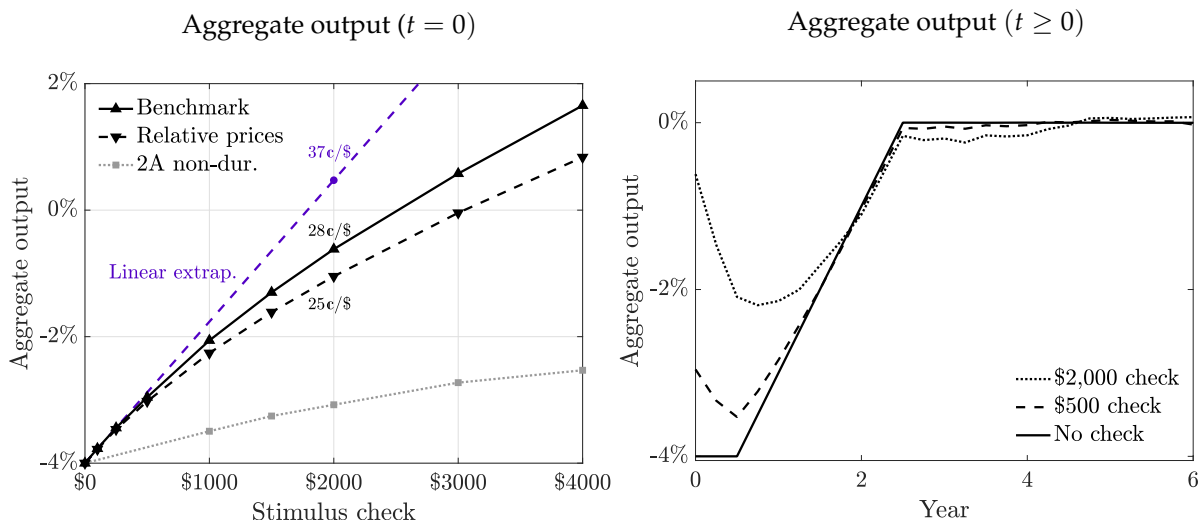
Aggregate output. The left panel of Figure 5.1 plots aggregate output in the first quarter in deviations from steady state for various sizes of stimulus checks. We first focus on the benchmark model that we presented in Sections 5.1–5.2 (solid black curve). Output is 4% below potential absent stimulus checks, which amounts to a \$670 decrease in average quarterly income. A large check of \$2,000 increases output by 28 cents per dollar, whereas a smaller check of \$300 increases output by 37 cents per dollar. Large checks thus remain effective but extrapolating from the response out of small checks overestimates their impact (dashed purple curve).⁴⁸ A larger check of \$2,500 is required to fully close the output gap.⁴⁹ For comparison, we also plot the output response in a canonical two-asset model of non-durables (dotted grey curve). The response to checks is much weaker in this model as it does not account for spending on durables.

Next, we extend our benchmark model and allow for relative price movements between durables and non-durables by lowering the supply elasticity of durables ($\zeta < \infty$). Relative price movements can dampen the response to aggregate shocks (McKay and Wieland, 2022; Orchard et al., 2022). We set the supply elasticity to $\zeta \equiv 1/0.049$ as in McKay and Wieland (2021, 2022). The effect of larger checks wears off more rapidly in this case (dashed black curve). A check of \$2,000 only

⁴⁸ Note that the response out of the \$300 check is lower than the static Keynesian multiplier associated with an MPX of 45% out of small checks (Figure 4.1). The reason is that: (i) only a fraction of households are eligible to the checks (66%); (ii) part of the extra spending leaks abroad through imports (20%); and (iii) labor incomes are taxed (at a marginal rate 30%). Accounting for (i)–(iii) yields a static Keynesian multiplier of 32 cents per dollar. In addition, future incomes also change in general equilibrium, and monetary and fiscal policy respond to the checks.

⁴⁹ Figure C.10 in Appendix C compares the response of aggregate output to stimulus checks in closed and open economies. As expected, stimulus checks are less effective at stimulating output in open economy since part of the extra spending leaks abroad through imports.

Figure 5.1: General equilibrium responses to stimulus checks



Notes: The left panel plots aggregate output in the first quarter in deviations from steady state as a function of the size of stimulus checks. The solid curve is our benchmark model (Sections 5.1–5.2). The dashed black curve is a version with relative price movements between durables and non-durables ($\zeta \equiv 1/0.049$). The purple line extrapolates the response out of a \$300 check. We also indicate the output increase (in cents per dollar sent) after a \$2,000 stimulus check. The grey curve is a canonical two-asset model of non-durables. The right panel reports the dynamic response of aggregate output in our benchmark model for stimulus checks of various sizes.

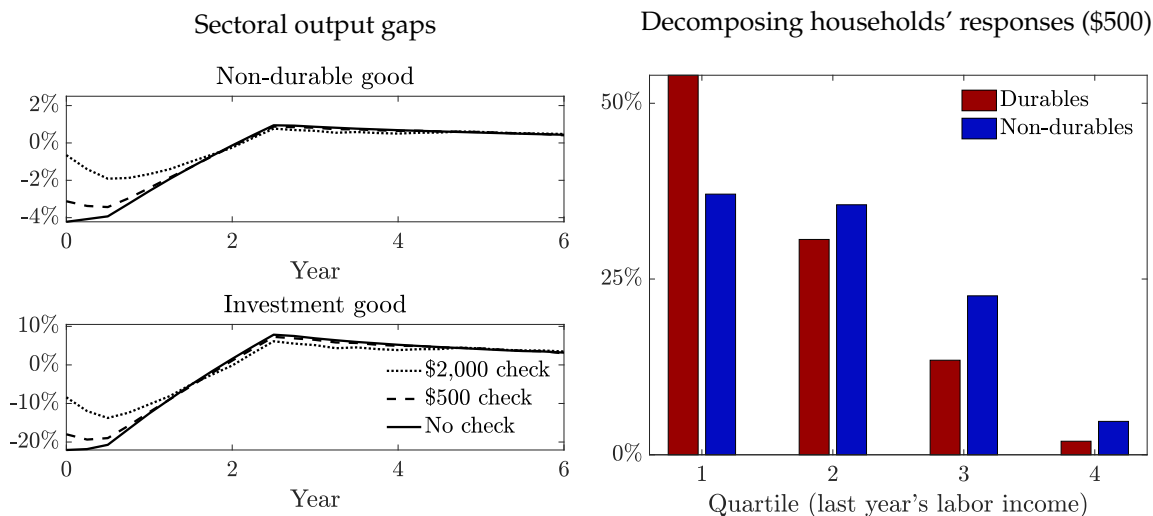
increases output by 25 cents per dollar. Thus, extrapolating from the response out of small checks overestimates the impact of larger ones even more, and a check of \$3,000 is needed to close the output gap.

The right panel of Figure 5.1 plots aggregate output over time in our benchmark model for two check sizes. A \$2,000 check closes most of the output gap in the first period, and about half of the cumulative output gap. A check of roughly \$4,000 closes the full cumulative output gap but stimulates output above potential in the short run (not shown).

Durables and non-durables. We now turn our attention separately to durables and non-durables. The left panel of Figure 5.2 plots the response of the sectoral output gaps for various stimulus checks.⁵⁰ The sector producing the investment good contracts proportionately more in the recession, both because households' durable

⁵⁰ Note that these output gaps do not exactly average out to the aggregate output gap reported in Figure 5.1 since intermediaries $F^{-1}(X_t^{\text{dom}})$ are counted in sectoral output (5.7) but not in aggregate output (5.11).

Figure 5.2: Durables and non-durables



Notes: The left panel plots the sectoral output gaps over time for various stimulus checks. The right panel plots the share of the households' equilibrium spending response out of a \$500 check accounted for by each quartile of the distribution of labor income over the previous year. The red bars correspond to durables, and the blue bars to non-durables.

spending is more cyclical and because of the demand shock that lowers the firm's investment. The two sectors recover roughly simultaneously. The right panel of Figure 5.2 decomposes the households' equilibrium spending response along the income distribution, both for durables (in red) and non-durables (in blue). Specifically, we plot the share of these responses accounted for by each quartile of the distribution of average labor income in the previous year (i.e., the basis of eligibility for checks). Lower-income households account for most of the aggregate spending responses, especially for durables, both because they have higher MPXs and because they are more likely to be eligible for checks.⁵¹

5.4 Supply Shocks and Inflation

We conclude the paper with an exercise that creates a larger role for supply side effects. The goal is to quantify the extent to which these forces could dampen the output response to stimulus checks and create inflationary pressures.

We add two features to our model. First, we allow for contractions in potential outputs in the two sectors (Y_t^{potent} and X_t^{potent}). Second, we introduce a non-linear

⁵¹ About 66% of households are eligible for checks, i.e., quartiles 1–2 receive the full check.

Phillips curve

$$\pi_t = \kappa \hat{y}_t + \kappa^* \max \{ \hat{y}_t, 0 \}^2 + \beta \pi_{t+1}, \quad (5.12)$$

when output is above potential. With this specification, the Phillips curve remains relatively flat while the economy is below potential. It steepens endogenously when sectoral outputs exceed potential.⁵² These features capture a rather extreme scenario: a “perfect storm” with both demand and supply shocks, and a strong inflationary response. While not representative of the typical recession, this scenario bears some resemblance to the 2020 recession and its recovery.⁵³

We assume that potential outputs Y_t^{potent} and X_t^{potent} decrease for three quarters and then mean revert linearly over the next 2 years (as aggregate output itself). We choose the initial drops so that potential output in each sector falls by half the contraction in actual output in that sector. Turning to the non-linear Phillips curve, there is much uncertainty in the literature about the appropriate value for κ^* . We purposefully choose a high value to allow inflation to play an important role. We set κ^* so the average slope of the Phillips curve is 0.1 as the output gap \hat{y}_t rises from zero to 2%. This output gap is similar to what we observed in the US in 2023 when inflation peaked (CBO). This slope lies at the upper end of conventional estimates in the literature (Mavroeidis et al., 2014) and is consistent with the findings of Cerrato and Gitti (2022) for the 2021-2022 recovery.⁵⁴

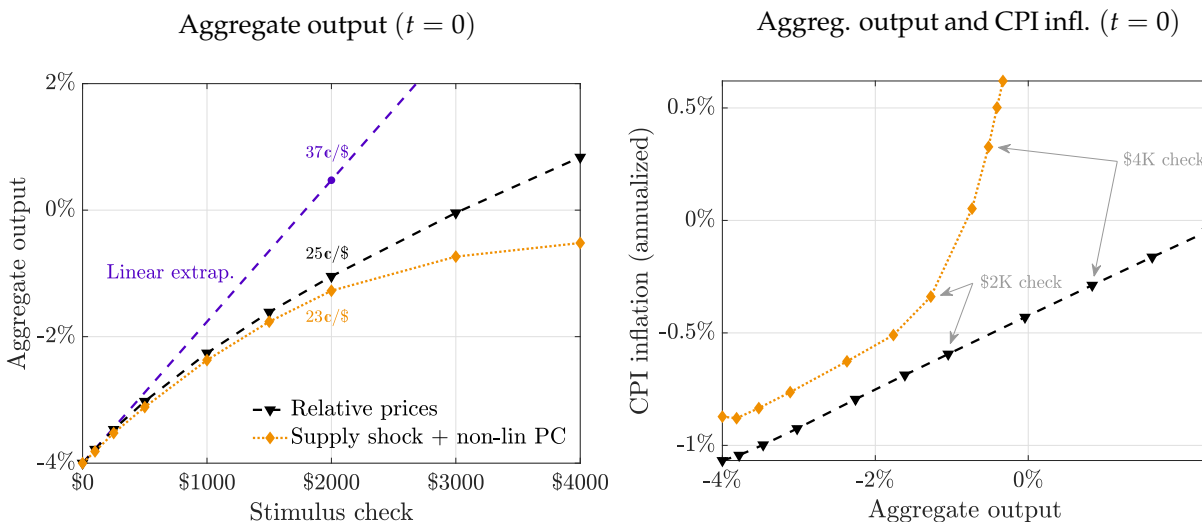
The left panel of Figure 5.3 plots aggregate output in the first quarter in deviations from steady state as a function of the size of checks. In turn, the right panel plots annualized CPI inflation (right panel) against aggregate output. The CPI price index averages the price indices for durables and non-durables using the households’ steady state spending shares (Appendix B.1). In our model with demand shocks only (dashed back curve, as in Figure 5.1) the economy starts in a deflation as output is below potential; the response of inflation to checks is relatively

⁵² Higgins (2021) argues that the Phillips curve was flat early on in 2020 around the time when stimulus checks were sent. Cerrato and Gitti (2022) reach the same conclusion, and find that the Phillips curve steepened subsequently during the 2021-2022 recovery as output exceeded potential.

⁵³ For example, US inflation was low during the 2001 recession and the Great recession whereas it rose in 2021. Our specification allows both for a *steepening* of the Phillips curve and an outward *shift* as the potential outputs contract (Hobijn et al., 2023; Ari et al., 2023).

⁵⁴ Cerrato and Gitti (2022) estimate that the slope of annualized inflation with respect to the unemployment rate was -0.85 during 2021-2022 recovery. Expressing this estimate in terms of quarterly inflation and output gap leads to a slope of roughly 0.1, assuming an unemployment elasticity of -0.5 (footnote 46).

Figure 5.3: Aggregate output and inflation



Notes: The left panel plots aggregate output in the first quarter in deviations from steady state as a function of the size of stimulus checks. The black dashed curve is our model with relative price movements (as in Figure 5.1). The orange dotted curve is the version of our model where we add a supply shock and a non-linear Phillips curve. The purple dashed line is the same as in Figure 5.1. The right panel plots annualized CPI inflation against aggregate output in the first period for the same checks as the left panel as well as two larger ones (\$5,000 and \$6,000).

modest.⁵⁵ Introducing the non-linear Phillips curve and the supply shock (dashed orange curve) raises the level of inflation slightly and makes it more responsive to checks as output exceeds its now lower potential level (-2%) and approaches its steady state level. The effect of checks on output wears off more rapidly as a result. A \$2,000 check only increases output by 23 cents per dollar (instead of 25) in this case, and the difference is even more pronounced for larger checks. A government that misdiagnoses the recession as being entirely demand-driven could send a check as large as \$3,000 to close the perceived output gap, i.e., the full 4% decline in output from steady state, when the true gap is smaller due to the supply shock. This would raise inflation meaningfully.

⁵⁵ A fall in the price of durables accounts for most of the deflation. Also, note that the economy can experience a deflation (in CPI terms) even when aggregate output is slightly above its steady state level. The reason is that the sector producing the investment good can still be below potential. Figure C.11 in Appendix C plots the sectoral output gaps with and without supply shock. The response of inflation to stimulus checks is maximized in the first quarter since there is no built-in lags in inflation in our model (not shown).

6 Conclusions

We study how households' marginal propensity to spend (MPX) varies as stimulus checks become larger. We augment a canonical incomplete markets model of durable spending by introducing a smooth adjustment hazard. The model can generate a decreasing, flat, or increasing MPX in the size of checks, depending on the shape of this hazard. We discipline the adjustment hazard by matching the evidence on (i) the MPX on durables and non-durables out of small checks; (ii) the short-run price elasticity of durables; (iii) the distribution of durable adjustment sizes; and (iv) the conditional probability of adjustment since the last purchase.

We find that the MPX declines with the size of checks, albeit slowly. The MPX neither surges as sometimes conjectured in the empirical literature, nor does it decline sharply as in a canonical two-asset model of non-durables.

As an application, we quantify the effect of stimulus checks in general equilibrium by embedding our spending model into an open-economy heterogeneous-agent New-Keynesian setting. In a typical recession, a large check of \$2,000 increases output by 25 cents per dollar in the quarter when it is sent, compared to 37 cents for a small check of \$300. Large checks thus remain effective, but extrapolating from the response out of small checks overestimates how much stimulus larger checks provide. We also use our model to assess the inflationary response to checks in recessions driven by a mix of demand and supply shocks.

Our analysis provides a useful, though incomplete answer when deciding how large stimulus checks should be in recessions. In particular, the optimal size of checks depends on how the government trades off the benefits of stimulating output with the costs of higher inflation. Checks are also used to insure households in recessions. Therefore, the optimal size of stimulus checks depends on the government's tolerance for inflation and its preference for insurance. Future work can build on the model that we have developed in this paper to quantify the optimal size of stimulus checks.

References

AARONSON, D., S. AGARWAL, AND E. FRENCH (2012): "The Spending and Debt Response to Minimum Wage Hikes," *American Economic Review*, 102, 3111–3139.

- ADAMS, W., L. EINAV, AND J. LEVIN (2009): "Liquidity Constraints and Imperfect Information in Subprime Lending," *American Economic Review*, 99, 49–84.
- AGARWAL, N. AND P. SOMAINI (2020): "Revealed Preference Analysis of School Choice Models," *Annual Review of Economics*, 12, 471–501.
- AGUIAR, M. A., M. BILS, AND C. BOAR (2023): "Who Are the Hand-to-Mouth?" Mimeo, New York University.
- ALVAREZ, F., H. LE BIHAN, AND F. LIPPI (2016a): "The Real Effects of Monetary Shocks in Sticky Price Models: A Sufficient Statistic Approach," *American Economic Review*, 106, 2817–51.
- ALVAREZ, F., F. LIPPI, AND A. OSKOLKOV (2023): "The Macroeconomics of Sticky Prices with Generalized Hazard Functions," *The Quarterly Journal of Economics*, 137, 989–1038.
- ALVAREZ, F., F. LIPPI, AND J. PASSADORE (2016b): "Are State- and Time-Dependent Models Really Different?" in *NBER Macroeconomics Annual 2016, Volume 31*, NBER Chapters, 379–457.
- ALVAREZ, F. E., K. BOROVIČKOVÁ, AND R. SHIMER (2021): "Consistent Evidence on Duration Dependence of Price Changes," NBER Working Papers 29112.
- ARGYLE, B. S., T. D. NADAULD, AND C. J. PALMER (2020): "Monthly Payment Targeting and the Demand for Maturity," *The Review of Financial Studies*, 33, 5416–5462.
- ARI, A., D. GARCIA-MACIA, AND S. MISHRA (2023): "Has the Phillips Curve Become Steeper?" IMF Working Papers 2023/100, International Monetary Fund.
- ARTUÇ, E., S. CHAUDHURI, AND J. MCLAREN (2010): "Trade Shocks and Labor Adjustment: A Structural Empirical Approach," *American Economic Review*, 100, 1008–1045.
- ATTANASIO, O., K. LARKIN, M. O. RAVN, AND M. PADULA (2022): "(S)Cars and the Great Recession," *Econometrica*, 90, 2319–2356.
- ATTANASIO, O. P., P. K. GOLDBERG, AND E. KYRIAZIDOU (2008): "Credit Constraints In The Market For Consumer Durables: Evidence From Micro Data On Car Loans," *International Economic Review*, 49, 401–436.
- AUCLERT, A. (2019): "Monetary policy and the redistribution channel," *American Economic Review*, 109, 2333–2367.
- AUCLERT, A., B. BARDÓCZY, M. ROGNLIE, AND L. STRAUB (2021): "Using the Sequence-Space Jacobian to Solve and Estimate Heterogeneous-Agent Models," *Econometrica*, 89, 2375–2408.
- AUCLERT, A., M. ROGNLIE, AND L. STRAUB (2018): "The Intertemporal Keyne-

- sian Cross," NBER Working Papers 25020, National Bureau of Economic Research, Inc.
- (2020): "Micro Jumps, Macro Humps: Monetary Policy and Business Cycles in an Estimated HANK Model," NBER Working Papers 26647.
- BACHMANN, R., B. BORN, O. GOLDFAYN-FRANK, G. KOCHARKOV, R. LUETTICKE, AND M. WEBER (2021): "A Temporary VAT Cut as Unconventional Fiscal Policy," NBER Working Papers 29442, National Bureau of Economic Research, Inc.
- BAKER, S. R., L. KUENG, L. MCGRANAHAN, AND B. T. MELZER (2018): "Do Household Finances Constrain Unconventional Fiscal Policy?" in *Tax Policy and the Economy, Volume 33*, NBER Chapters.
- BERAJA, M. (2023): "A Semistructural Methodology for Policy Counterfactuals," *Journal of Political Economy*, 131, 000–000.
- BERAJA, M., A. FUSTER, E. HURST, AND J. VAVRA (2019): "Regional Heterogeneity and the Refinancing Channel of Monetary Policy," *The Quarterly Journal of Economics*, 134, 109–183.
- BERGER, D., T. CUI, N. TURNER, AND E. ZWICK (2023): "Stimulating Durable Purchases," In preparation.
- BERGER, D., K. MILBRADT, F. TOURRE, AND J. VAVRA (2021): "Mortgage Prepayment and Path-Dependent Effects of Monetary Policy," *American Economic Review*, 111, 2829–2878.
- BERGER, D. AND J. VAVRA (2014): "Measuring How Fiscal Shocks Affect Durable Spending in Recessions and Expansions," *American Economic Review*, 104, 112–115.
- (2015): "Consumption Dynamics During Recessions," *Econometrica*, 83, 101–154.
- BERRY, S., J. LEVINSOHN, AND A. PAKES (1995): "Automobile Prices in Market Equilibrium," *Econometrica*, 63, 841–890.
- (2004): "Differentiated Products Demand Systems from a Combination of Micro and Macro Data: The New Car Market," *Journal of Political Economy*, 112, 68–105.
- BERTOLA, G. AND R. J. CABALLERO (1990): "Kinked Adjustment Costs and Aggregate Dynamics," in *NBER Macroeconomics Annual 1990, Volume 5*, NBER Chapters, 237–296.
- BOEHM, C. E., A. A. LEVCHENKO, AND N. PANDALAI-NAYAR (2023): "The Long and Short (Run) of Trade Elasticities," *American Economic Review*, 113, 861–905.

- BRUNNERMEIER, M. K. AND Y. SANNIKOV (2014): “A Macroeconomic Model with a Financial Sector,” *American Economic Review*, 104, 379–421.
- (1999): “Explaining Investment Dynamics in U.S. Manufacturing: A Generalized (S,s) Approach,” *Econometrica*, 67, 783–826.
- CANTELMO, A. AND G. MELINA (2018): “Monetary policy and the relative price of durable goods,” *Journal of Economic Dynamics and Control*, 86, 1–48.
- CERRATO, A. AND G. GITTI (2022): “The Recent Steepening of Phillips Curves,” Mimeo, University of California, Berkeley.
- CHEN, J., S. ESTEBAN, AND M. SHUM (2013): “When Do Secondary Markets Harm Firms?” *American Economic Review*, 103, 2911–2934.
- DEPARTMENT OF TRANSPORTATION (2023): “National Transportation Statistics, Table 1-17,” Tech. rep., United States.
- EBERLY, J. C. (1994): “Adjustment of Consumers’ Durables Stocks: Evidence from Automobile Purchases,” *Journal of Political Economy*, 102, 403–436.
- FAGERENG, A., M. B. HOLM, AND G. J. NATVIK (2021): “MPC Heterogeneity and Household Balance Sheets,” *American Economic Journal: Macroeconomics*, 13, 1–54.
- (2017): “Fiscal unions,” *American Economic Review*, 107, 3788–3834.
- FLODEN, M. AND J. LINDÉ (2001): “Idiosyncratic Risk in the United States and Sweden: Is There a Role for Government Insurance?” *Review of Economic Dynamics*, 4, 406–437.
- FUSTER, A., G. KAPLAN, AND B. ZAFAR (2021): “What Would You Do with \$500? Spending Responses to Gains, Losses, News, and Loans,” *Review of Economic Studies*, 88, 1760–1795.
- GANONG, P., F. E. GREIG, P. J. NOEL, D. M. SULLIVAN, AND J. S. VAVRA (2022): “Spending and Job-Finding Impacts of Expanded Unemployment Benefits: Evidence from Administrative Micro Data,” NBER Working Papers 30315.
- GAVAZZA, A. AND A. LANTERI (2021): “Credit Shocks and Equilibrium Dynamics in Consumer Durable Goods Markets,” *The Review of Economic Studies*, 88, 2935–2969.
- GILLINGHAM, K., F. ISKHAKOV, A. MUNK-NIELSEN, J. RUST, AND B. SCHJERNING (2022): “Equilibrium Trade in Automobiles,” *Journal of Political Economy*, 130, 2534–2593.
- GOLOSOV, M., M. GRABER, M. MOGSTAD, AND D. NOVGORODSKY (2021): “How Americans Respond to Idiosyncratic and Exogenous Changes in Household Wealth and Unearned Income,” NBER Working Papers 29000.
- GOLOSOV, M. AND R. E. LUCAS (2007): “Menu Costs and Phillips Curves,” *Journal*

- of *Political Economy*, 115, 171–199.
- GOWRISANKARAN, G. AND M. RYSMAN (2012): “Dynamics of Consumer Demand for New Durable Goods,” *Journal of Political Economy*, 120, 1173–1219.
- GREEN, D., B. T. MELZER, J. A. PARKER, AND A. ROJAS (2020): “Accelerator or Brake? Cash for Clunkers, Household Liquidity, and Aggregate Demand,” *American Economic Journal: Economic Policy*, 12, 178–211.
- GROSS, T., M. J. NOTOWIDIGDO, AND J. WANG (2020): “The Marginal Propensity to Consume over the Business Cycle,” *American Economic Journal: Macroeconomics*, 12, 351–384.
- GUERRIERI, V. AND G. LORENZONI (2017): “Credit Crises, Precautionary Savings, and the Liquidity Trap,” *The Quarterly Journal of Economics*, 132, 1427–1467.
- HALE, G., B. HOBIJN, F. NECHIO, AND D. WILSON (2019): “How Much Do We Spend on Imports?” *FRBSF Economic Letter*.
- HAVRANEK, T. AND A. SOKOLOVA (2020): “Do Consumers Really Follow a Rule of Thumb? Three Thousand Estimates from 144 Studies Say ‘Probably Not’,” *Review of Economic Dynamics*, 35, 97–122.
- HAZELL, J., J. HERREÑO, E. NAKAMURA, AND J. STEINSSON (2022): “The Slope of the Phillips Curve: Evidence from U.S. States,” *The Quarterly Journal of Economics*, 137, 1299–1344.
- HEATHCOTE, J., K. STORESLETTEN, AND G. L. VIOLANTE (2017): “Optimal Tax Progressivity: An Analytical Framework,” *The Quarterly Journal of Economics*, 132, 1693–1754.
- HEITFIELD, E. AND T. SABARWAL (2004): “What Drives Default and Prepayment on Subprime Auto Loans?” *The Journal of Real Estate Finance and Economics*, 29, 457–477.
- HIGGINS, P. C. (2021): “The Phillips Curve during the Pandemic: Bringing Regional Data to Bear,” Policy Hub* 2021-11, Federal Reserve Bank of Atlanta.
- HOBIJN, B., R. MILES, J. ROYAL, AND J. ZHANG (2023): “The Recent Steepening of Phillips Curves,” *Chicago Fed Letter*, 0.
- HOUSE, C. L. (2014): “Fixed costs and long-lived investments,” *Journal of Monetary Economics*, 68, 86 – 100.
- ISKHAKOV, F., T. H. JØRGENSEN, J. RUST, AND B. SCHJERNING (2017): “The endogenous grid method for discrete-continuous dynamic choice models with (or without) taste shocks,” *Quantitative Economics*, 8, 317–365.
- JERMANN, U. J. (1998): “Asset pricing in production economies,” *Journal of Monetary Economics*, 41, 257–275.

- JUSTINIANO, A. AND G. E. PRIMICERI (2008): "The Time-Varying Volatility of Macroeconomic Fluctuations," *American Economic Review*, 98, 604–641.
- KAPLAN, G., B. MOLL, AND G. L. VIOLANTE (2018): "Monetary Policy According to HANK," *American Economic Review*, 108, 697–743.
- KAPLAN, G. AND G. L. VIOLANTE (2014): "A Model of the Consumption Response to Fiscal Stimulus Payments," *Econometrica*, 82, 1199–1239.
- (2022): "The Marginal Propensity to Consume in Heterogeneous Agent Models," *Annual Review of Economics*, 14, 747–775.
- KAPLAN, G., G. L. VIOLANTE, AND J. WEIDNER (2014): "The Wealthy Hand-to-Mouth," *Brookings Papers on Economic Activity*, 45, 77–153.
- KUENG, L. (2018): "Excess Sensitivity of High-Income Consumers*," *The Quarterly Journal of Economics*, 133, 1693–1751.
- LAIBSON, D., P. MAXTED, AND B. MOLL (2021): "Present Bias Amplifies the Household Balance-Sheet Channels of Macroeconomic Policy," NBER Working Papers 29094.
- (2022): "A Simple Mapping from MPCs to MPXs," NBER Working Papers 29664.
- LEARY, M. T. AND R. MICHAELY (2011): "Determinants of Dividend Smoothing: Empirical Evidence," *The Review of Financial Studies*, 24, 3197–3249.
- LEWIS, D. J., D. MELCANGI, AND L. PILOSSOPH (2022): "Latent heterogeneity in the marginal propensity to consume," Mimeo, Duke University.
- LUENGO-PRADO, M. J. (2006): "Durables, nondurables, down payments and consumption excesses," *Journal of Monetary Economics*, 53, 1509–1539.
- MATĚJKA, F. AND A. MCKAY (2015): "Rational inattention to discrete choices: A new foundation for the multinomial logit model," *American Economic Review*, 105, 272–298.
- MAVROEIDIS, S., M. PLAGBORG-MØLLER, AND J. H. STOCK (2014): "Empirical Evidence on Inflation Expectations in the New Keynesian Phillips Curve," *Journal of Economic Literature*, 52, 124–188.
- MCFADDEN, D. (1973): *Conditional Logit Analysis of Qualitative Choice Behavior*, Institute of Urban and Regional Development, University of California.
- (2001): "Economic Choices," *American Economic Review*, 91, 351–378.
- MCKAY, A. AND J. F. WIELAND (2021): "Lumpy Durable Consumption Demand and the Limited Ammunition of Monetary Policy," *Econometrica*, 89, 2717–2749.
- (2022): "Forward Guidance and Durable Goods Demand," *American Eco-*

- conomic Review: Insights*, 4, 106–22.
- MIAN, A., K. RAO, AND A. SUFI (2013): “Household Balance Sheets, Consumption, and the Economic Slump,” *The Quarterly Journal of Economics*, 128, 1687–1726.
- MIAN, A. AND A. SUFI (2012): “The Effects of Fiscal Stimulus: Evidence from the 2009 Cash for Clunkers Program,” *The Quarterly Journal of Economics*, 127, 1107–1142.
- NEVO, A. (2001): “Measuring Market Power in the Ready-to-Eat Cereal Industry,” *Econometrica*, 69, 307–342.
- ORCHARD, J., V. A. RAMEY, AND J. F. WIELAND (2022): “Micro MPCs and Macro Counterfactuals: The Case of the 2008 Rebates,” Tech. rep., UCSD Mimeo.
- PARKER, J. A., N. S. SOULELES, D. S. JOHNSON, AND R. MCCLELLAND (2013): “Consumer Spending and the Economic Stimulus Payments of 2008,” *American Economic Review*, 103, 2530–2553.
- RUST, J. (1985): “Stationary Equilibrium in a Market for Durable Assets,” *Econometrica*, 53, 783–805.
- SOULELES, N. S. (1999): “The Response of Household Consumption to Income Tax Refunds,” *American Economic Review*, 89, 947–958.
- WILCOX, D. W. (1989): “Social Security Benefits, Consumption Expenditure, and the Life Cycle Hypothesis,” *Journal of Political Economy*, 97, 288–304.
- WOLF, C. K. (2021): “Interest Rate Cuts vs. Stimulus Payments: An Equivalence Result,” Mimeo, MIT.
- WOLF, C. K. AND A. MCKAY (2022): “What Can Time-Series Regressions Tell Us About Policy Counterfactuals?” NBER Working Papers 30358.

Online Appendix for: Durables and Size-Dependence in the Marginal Propensity to Spend

This online appendix contains a detailed description of the quantitative model and its numerical solution, as well as additional results for the article “Durables and Size-Dependence in the Marginal Propensity to Spend.”

Any references to equations, figures, or sections that are not preceded “A.,” “B.,” “C.,” or “D.” refer to the main article.

A Consumption and Investment Problem

In this appendix, we discuss how to solve the households' consumption and investment problem. Section A.1 states the problem recursively. Section A.2 discusses the numerical implementation. Finally, Section A.3 provides details about our numerical implementation.

A.1 Households' Problem

We now state the household's problem recursively. Relative to Section 2.5, the formulation below allows for movements in the price of durables (P^d) and non-durables (P^c) as in our general equilibrium analysis (Section 5). We also formulate the problem in a way that lends itself better to numerical implementation (Appendix A.2). All prices and real quantities are expressed relative to the domestic non-durable good (Appendix B.1). Households are still indexed by three idiosyncratic states: their stock of durables (d); their holdings of liquid asset (m); and their idiosyncratic income (y). We let $\mathbf{x} \equiv (d, m, y)$ to save on notation.

Continuation values. The continuation values $\{V_t(\cdot)\}$ can be characterized recursively.⁵⁶

1. **Discrete choice.** The household chooses whether to adjust its stock of durables. The value associated to the discrete choice problem is

$$V_t(\mathbf{x}) \equiv \max \left\{ V_t^{\text{adjust}}(\mathbf{x}) - \epsilon, V_t^{\text{not}}(\mathbf{x}) \right\}, \quad (\text{A.1})$$

where $V_t^{\text{adjust}}(\mathbf{x})$ is the value of adjusting the stock of durables, $V_t^{\text{not}}(\mathbf{x})$ is the value of not adjusting, and ϵ is a taste shifter that follows a logistic distribution whose mean and variance are controlled by $\kappa > 0$ and $\eta^2 > 0$,

⁵⁶ The terminal condition for $V_{t+1}(\cdot)$ is either an initial guess when solving for the stationary equilibrium, or the stationary value function without stimulus checks when solving for transitions.

respectively.⁵⁷ Therefore,

$$V_t(\mathbf{x}) = \eta \log \left(\exp \left(\frac{V_t^{\text{adjust}}(\mathbf{x}) - \kappa}{\eta} \right) + \exp \left(\frac{V_t^{\text{not}}(\mathbf{x})}{\eta} \right) \right) \quad (\text{A.2})$$

The adjustment hazard associated to this discrete choice problem is

$$S_t(\mathbf{x}) = \frac{\exp \left(\frac{V_t^{\text{adjust}}(\mathbf{x}) - \kappa}{\eta} \right)}{\exp \left(\frac{V_t^{\text{adjust}}(\mathbf{x}) - \kappa}{\eta} \right) + \exp \left(\frac{V_t^{\text{not}}(\mathbf{x})}{\eta} \right)} \quad (\text{A.3})$$

The continuation values are given by

$$V_t^{\text{adjust}}(\mathbf{x}) \equiv W_t^D(\mathcal{Y}_t(\mathbf{x}; T_t) + \Delta_t^D d, y) \quad (\text{A.4})$$

$$V_t^{\text{not}}(\mathbf{x}) \equiv W_t^C((1 - (1 - \iota)\delta)d, \mathcal{Y}_t(\mathbf{x}; T_t) - \Delta_t^C d - \iota \delta P_t^d d, y) \quad (\text{A.5})$$

The households gets to choose a new stock of durables if it adjusts, and maintains its stock otherwise by offsetting a share ι of the depreciation (Berger and Vavra, 2015). These continuation values depend on the household's initial cash-on-hand after interest payment and stimulus check

$$\begin{aligned} \mathcal{Y}_t(\mathbf{x}; T_t) \equiv & \psi_{0,t} \left(y Y_t^{\text{inc}} \right)^{1-\psi_1} + \frac{1 + r_{t-1}^m}{1 + \pi_t} m \\ & - r_{t-1}^b (1 - \theta) \hat{P}_t^d d + t_t, \end{aligned} \quad (\text{A.6})$$

where Y_t^{inc} is real aggregate income and t_t are real stimulus checks. The interest rate on credit r_{t-1}^b is equal to the return on the liquid asset r_{t-1}^m plus a spread of 3.5% (Section 3.1). The inflation rate π_t accounts for the fact that the budget constraints are expressed in real terms, i.e., all prices are expressed relative to the one of the non-durable domestic good. The credit that a household contracts in period $t - 1$ depends on the expected nominal price of its durables next period (as in Gavazza and Lanteri, 2021). The real price \hat{P}_t^d is thus equal to the real price of durables P_t^d for all periods $t \geq 1$ in our perfect

⁵⁷ An equivalent formulation consists of introducing two additive taste shifters e^{adjust} and e^{not} (one for each option) which are distributed according to a generalized extreme value distribution of type-I. See Artuç et al. (2010) for the derivation of (A.2) and (A.3) in this case.

foresight economy. However, these two prices need not be equal in the very first period $t = 0$ since the price of durables and inflation can jump after an aggregate shock. Therefore, $\hat{P}_t^d \equiv \mathbb{E}_{t-1} [P_t^d] \times (1 + \mathbb{E}_{t-1} [\pi_t]) / (1 + \pi_t)$ in $t = 0$. In turn, the remaining terms in (A.4)–(A.5) are

$$\Delta_t^D \equiv (1 - \delta) P_t^d - (1 - \theta) \hat{P}_t^d \quad (\text{A.7})$$

$$\Delta_t^C \equiv (1 - \theta) \times \left\{ \hat{P}_t^d - P_{t+1}^d (1 + \pi_{t+1}) (1 - (1 - \iota) \delta) \right\} \quad (\text{A.8})$$

which capture, respectively, the net profit that the household makes when selling its old durable (after repaying its outstanding credit) for Δ_t^D , and the credit repayment on the principal for Δ_t^C .⁵⁸ In the fully state-dependent limit $\eta \rightarrow 0$, the value (A.2) and the hazard (A.3) become

$$V_t(\mathbf{x}) = \max \left\{ V_t^{\text{adjust}}(\mathbf{x}) - \kappa, V_t^{\text{not}}(\mathbf{x}) \right\} \quad (\text{A.9})$$

and

$$S_t(\mathbf{x}) = \begin{cases} 1 & \text{if } V_t^{\text{adjust}}(\mathbf{x}) - \kappa > V_t^{\text{not}}(\mathbf{x}) \\ 0 & \text{otherwise} \end{cases} \quad (\text{A.10})$$

2. Durable adjustment. If the household decides to adjust its stock of durables, it chooses how much durables to purchase

$$\begin{aligned} W_t^D(m, y) &\equiv \max_{d', m'} W_t^C(d', m', y) \\ &\text{s.t. } \left[P_t^d - (1 - \theta) P_{t+1}^d (1 + \pi_{t+1}) \right] d' + m' \leq m, \end{aligned} \quad (\text{A.11})$$

where m is real cash-on-hand before the household purchases its new stock of durables. As explained above, households' credit depends on the expected price of durables next period. The price index for durables P_t^d is expressed relative to the price of the domestic non-durable, which grows at rate π_{t+1} over time. The continuation value W_t^C reflects the subsequent optimal consumption-saving choice that occurs in the same period.

⁵⁸ While holding their stock of durables, households repay their outstanding credit at the same rate at which the value of their durables depreciates.

3. **Consumption-saving.** Finally, the household chooses how much to consume and save in liquid asset

$$W_t^C(d, m, y) \equiv \max_{c, m'} u(c, d) + \beta \int V_{t+1}(d, m', y') \Gamma(dy'; y) \quad (\text{A.12})$$

$$\text{s.t. } P_t^c c + m' \leq m \quad \text{and} \quad m' \geq 0,$$

where m is the household's real cash-on-hand when it chooses non-durable consumption c , and m' is the real holdings of liquid asset for next period.

A.2 Numerical Implementation

We now describe how we solve numerically for the value functions defined above, and how we iterate on the associated policy functions to obtain aggregate quantities.

Value functions. We proceed as follows:

1. **Guess.** Fix $\mathcal{V}_{T+1}(\mathbf{x}) \equiv \int V_{T+1}(d, m, y') \Gamma(dy'; y)$ for the terminal period.
2. **Consumption-saving.** Fix the continuation states (d, y) . If the household's borrowing constraint $m' \geq 0$ is not binding, a necessary condition for an optimum to (A.12) is

$$u_c(c, d) = \beta P_t^c \partial_m \mathcal{V}_{t+1}(d, m', y), \quad (\text{A.13})$$

together with the budget constraint $c = (m - m') / P_t^c$. This condition is not sufficient, however, since the problem is typically non-convex.^{59,60} To recover

⁵⁹ The reason is that the continuation value involves the upper envelope (A.1). Random taste shocks for adjustment, i.e., the smooth hazard (A.3), can make continuation value *smooth* (i.e. no kinks) but not necessarily *concave*.

⁶⁰ Condition (A.13) is necessary for an optimum (even when $\eta = 0$). The argument is similar to the one in Clausen and Strub (2012). Consider a simplified version of the problem of interest: $\max_c f(c) + G(-c)$ with $f(\cdot)$ and $G(\cdot)$ smooth except for a convex kink in $G(\cdot)$ at $\bar{c} \in \mathbb{R}$. Suppose (by contradiction) that the optimizer is \bar{c} . Then, $f'(\bar{c}) \geq G'_+(-\bar{c})$ and $f'(\bar{c}) \leq G'_-(-\bar{c})$. However, $G'_+(-\bar{c}) > G'_-(-\bar{c})$ since $G(\cdot)$ admits a convex kink at \bar{c} . This leads to the desired contradiction. Therefore, the optimizer cannot be the point where the kink occurs, and condition (A.13) is necessary. The argument generalizes to multiple kinks and multiple assets.

policy functions, i.e., maps $m \mapsto (c, m')$, we proceed as follows. We first obtain a map $m' \mapsto m$ using the endogenous grid method (EGM) of [Carroll \(2006\)](#). The (generalized) inverse of this map (as a function of m) might contain several points for m' since the problem is non-convex. These points define a set of candidates, together with the borrowing constraint $m' = 0$. The optimum is found by comparing the values of the objective in [\(A.12\)](#) associated to each candidate. More specifically, we recover the policy functions $m \mapsto (c, m')$ using an approach similar to [Druehl and Jørgensen \(2017\)](#). We split the map $m' \mapsto m$ into monotonic segments, i.e., either increasing or decreasing. Fixing some m on the grid of interest, we interpolate linearly the value of m' at m using each segment. We add $\max\{m', 0\}$ to the set of candidates. The borrowing constraint $m' = 0$ and the upper bound of the grid for m also belong to this set of candidates. Finally, we compare the value of the objective for this set of candidates for m' .⁶¹ The policy function $m \mapsto m'$ is the one that provides the highest value, and $m \mapsto c$ is recovered using the budget constraint $c = (m - m') / P_t^c$. Using the resulting policy function $m'_t(\cdot)$, we compute the value $W_t^C(\mathbf{x})$ using [\(A.12\)](#), and the marginal values

$$\partial_d W_t^C(\mathbf{x}) = u_d((m - m'_t(\cdot)) / P_t^c, d) + \beta \partial_d \mathcal{V}_{t+1}(d, m'_t(\cdot), y) \quad (\text{A.14})$$

$$\partial_m W_t^C(\mathbf{x}) = 1 / P_t^c u_c((m - m'_t(\cdot)) / P_t^c, d) \quad (\text{A.15})$$

for the durable and the liquid asset.

3. **Durable adjustment.** A necessary condition for an optimum to [\(A.11\)](#) is

$$\begin{aligned} & \partial_d W_t^C(d', m', y) \\ & - \left[P_t^d - (1 - \theta) P_{t+1}^d (1 + \pi_{t+1}) \right] \partial_m W_t^C(d', m', y) = 0 \end{aligned} \quad (\text{A.16})$$

where

$$m' = m - \left[P_t^d - (1 - \theta) P_{t+1}^d (1 + \pi_{t+1}) \right] d' \quad (\text{A.17})$$

⁶¹ An alternative approach is to focus only on the couple (m'_0, m'_1) such that m is bracketed by the couple (m_0, m_1) that was recovered by the EGM for (m'_0, m'_1) . In principle, this approach might miss the correct value of m' if the grid for liquid asset is too coarse. Our approach does not suffer from this problem, but it requires considering a few more candidates for m' .

Again, (A.16) is typically not sufficient for an optimum.⁶² We thus define a set of candidates d' that satisfy either (A.16) or $d' = \bar{d}$ where \bar{d} is the upper bound of our numerical grid for durables. We compute the value (A.11) associated to these candidates. The policy function for d' is the one that provides the highest value. We compute the value $W^D(\mathbf{x})$ using (A.11), and the marginal value

$$\partial_m W_t^D(m, y) = \partial_m W_t^C(d'(\cdot), m'(\cdot), y), \quad (\text{A.18})$$

and proceed to Step 4.

4. **Continuation values.** Compute the values (A.4)–(A.5) and the marginal values

$$\partial_d V_t^{\text{adjust}}(\mathbf{x}) = \left\{ -r_{t-1}^b (1 - \theta) \hat{P}_t^d + \Delta_t^D \right\} \partial_m W_t^D(\cdot) \quad (\text{A.19})$$

$$\begin{aligned} \partial_d V_t^{\text{not}}(\mathbf{x}) &= (1 - (1 - \iota) \delta) \partial_d W_t^C(\cdot) + \\ &\left\{ -r_{t-1}^b (1 - \theta) \hat{P}_t^d - \Delta_t^C - \iota \delta P_t^d \right\} \partial_m W_t^C(\cdot) \end{aligned} \quad (\text{A.20})$$

for the durable stock, with Δ_t^D and Δ_t^C defined by (A.7)–(A.8), and

$$\partial_m V_t^{\text{adjust}}(\mathbf{x}) = \frac{1 + r_{t-1}^m}{1 + \pi_t} \partial_m W_t^D(\cdot) \quad \text{and} \quad \partial_m V_t^{\text{not}}(\mathbf{x}) = \frac{1 + r_{t-1}^m}{1 + \pi_t} \partial_m W_t^C(\cdot) \quad (\text{A.21})$$

for the liquid asset.

5. **Discrete choice.** Compute the value (A.2) and the marginal values

$$\partial_z V_t(\mathbf{x}) = \mathcal{S}_t(\mathbf{x}) \partial_z V_t^{\text{adjust}}(\mathbf{x}) + \{1 - \mathcal{S}_t(\mathbf{x})\} \partial_z V_t^{\text{not}}(\mathbf{x}) \quad (\text{A.22})$$

for the durable stock and the liquid asset $z \in \{d, m\}$, where $\mathcal{S}_t(\mathbf{x})$ is the adjustment hazard (A.3).

6. **Update.** Compute the expected utility $\mathcal{V}_t(\mathbf{x}) \equiv \int V_t(d, m, y') \Gamma(dy'; y)$. Similarly, compute the marginal utilities $\partial_z \mathcal{V}_t(\mathbf{x}) \equiv \int \partial_z V_t(d, m, y') \Gamma(dy'; y)$ for the durable stock and the liquid asset $z \in \{d, m\}$. Finally, iterate on Step 2 until convergence when solving for the stationary equilibrium, or until $t = 0$ when solving for transitions.

⁶² The solution is necessarily interior, however, since $d' = 0$, cannot be optimal.

A.3 Computational Details

Numerical parameters. We use 175-point grids for the stock of durables d and the liquid asset m . We discretize the income process on a 7-point grid using the method of Rouwenhorst (1995). We use a stochastic simulation given the non-convexities inherent to our model.⁶³ To iterate on the distribution, we use the policy functions computed above, together with the income process Γ and we randomly assign households between adjustment and no adjustment according the adjustment hazard (A.3). The hazard and the policy functions are interpolated linearly between grid points. When computing our stationary moments (Section 3), we simulate 15,000 households over 3,000 quarters with a burn of 400 quarters. In general equilibrium, we sample 200,000 households from this stationary distribution, and simulate them over 125 quarters after a burn of 400 quarters.

Smoothing the responses. In Sections 3–4, we compare the properties of our model with a purely state-dependent version ($\eta \rightarrow 0$). To obtain slightly smoother responses, we introduce a very small variance $\eta = 0.0025$. The difference with our model and baseline calibration is that this variance is arbitrarily small, whereas we discipline this parameter in our model to match a rich set of micro moments.

B General Equilibrium

In this appendix, we describe the general equilibrium setup in more details. Section B.1 describes the price indices and the open economy features of our model

⁶³ A non-stochastic simulation (e.g., Young, 2010) typically produces a different stationary distribution in presence of non-convexities. To understand why, consider a simplified example. Suppose that the stock of durables d is the only state and that there is no depreciation $\delta = 0$. There are three evenly-spaced points $\underline{d} < \hat{d} < \bar{d}$. Let us assume that the hazard satisfies $\mathcal{S}(\underline{d}) = 1$ and $\mathcal{S}(\hat{d}) = \mathcal{S}(\bar{d}) = 0$, and it is linear between these points. Conditional on adjustment, the policy function satisfies $d'(\underline{d}) = \bar{d}$ and $d'(\hat{d}) = d'(\bar{d}) = \underline{d}$, and it is linear between these points. Suppose that the household starts with a stock $d = 1/3\underline{d} + 2/3\hat{d}$. In this case, the stationary distribution is a mass point at d . Now, suppose that the functions \mathcal{S} and d' are discretized on the three points $\underline{d} < \hat{d} < \bar{d}$. Starting at d , the probability of adjustment is $1/3$, both for the stochastic simulation (when interpolating the hazard linearly between grid points) and for the non-stochastic simulation (where households are allocated to neighboring grid points based on their proximity to those). By construction, the stochastic simulation induces the correct stationary distribution with a mass point at d . On the contrary, the non-stochastic simulation induces a stationary distribution with two mass points at \hat{d} and \bar{d} .

(net exports, the real exchange rate, etc.). Section B.2 states and characterizes the firm's investment problem. Section B.3 explains how we construct efficiently the sequence of investment shocks that generates any particular recession of interest. Finally, Section B.4 discusses fiscal policy.

B.1 Price Indices, Trade Balance and Exchange Rate

This appendix provides the expressions for the price indices, the trade balance, and the equilibrium exchange rate.

Price indices. We express the domestic prices and price indices, the exchange rate, and the trade balance relative to the price of the domestic non-durable good.⁶⁴ The real exchange rate is the cost of acquiring a non-durable good from the foreign country. The price indices at home for the non-durable and investment goods baskets are

$$P_t^c \equiv \left[\alpha_c + (1 - \alpha_c) (e_t)^{1-\rho} \right]^{\frac{1}{1-\rho}} \quad \text{and} \quad P_t^d \equiv \left[\alpha_d (p_t^d)^{1-\rho} + (1 - \alpha_d) (e_t)^{1-\rho} \right]^{\frac{1}{1-\rho}}, \quad (\text{B.1})$$

where e_t is the real exchange rate and p_t^d is the relative price of the domestic investment good, using the fact that the nominal prices of foreign goods are normalized to 1 (Section 5.1). Similarly, the price indices abroad are

$$P_t^{c,*} \equiv \left[\alpha_c + (1 - \alpha_c) (1/e_t)^{1-\rho} \right]^{\frac{1}{1-\rho}} \quad \text{and} \quad P_t^{d,*} \equiv \left[\alpha_d + (1 - \alpha_d) (p_t^d/e_t)^{1-\rho} \right]^{\frac{1}{1-\rho}} \quad (\text{B.2})$$

The *level* of the price of the domestic non-durable good is

$$P_t^{\text{dom}} = \prod_{s=0}^t (1 + \pi_s), \quad (\text{B.3})$$

where the inflation rate π_t is given by the Phillips curve (5.2). The CPI price index is

$$\text{CPI}_t \equiv \left\{ \omega^{c,\text{CPI}} + (1 - \omega^{c,\text{CPI}}) p_t^d \right\} P_t^{\text{dom}}, \quad (\text{B.4})$$

where $\omega^{c,\text{CPI}} \equiv 1 / (1 + X/C)$ is the spending share of domestic households on the

⁶⁴ Similarly, we express the foreign price indices (B.2) relative to the foreign non-durable good.

non-durable good at the stationary equilibrium. The PPI index is defined similarly, with weight $\omega^{c,\text{PPI}} \equiv 1 / (1 + \{X + Z\} / \{C + G + F^{-1}(X + Z)\})$, which is the output share of the non-durable good at the stationary equilibrium.

Net exports and trade balance. Let

$$\text{IM}_t^c \equiv (1 - \alpha_c) \left(\frac{e_t}{P_t^c} \right)^{-\rho} (C_t + G_t) \quad \text{and} \quad \text{IM}_t^d \equiv (1 - \alpha_d) \left(\frac{e_t}{P_t^d} \right)^{-\rho} X_t \quad (\text{B.5})$$

denote the quantities imported of the non-durable and investment good, respectively, where we have used the fact that the nominal prices of foreign goods are normalized to 1. Similarly, let

$$\text{EX}_t^c \equiv (1 - \alpha_c) \left(\frac{1/e_t}{P_t^{c,*}} \right)^{-\rho} (C^* + G^*) \quad \text{and} \quad \text{EX}_t^d \equiv (1 - \alpha_d) \left(\frac{p^d/e_t}{P_t^{d,*}} \right)^{-\rho} X^* \quad (\text{B.6})$$

denote the quantities exported, where consumption C^* , government spending G^* and investment X^* in the rest of the world are constant and equal to the steady state levels at home, i.e., $C^* = C$, $G^* = G$ and $X^* = X$, so there are no net imports initially. The quantity indices for net exports are $\text{NX}_t^z \equiv \text{EX}_t^z - \text{IM}_t^z$ for the non-durable and investment goods $z \in \{c, d\}$. The quantity index for the trade balance is $\text{TB}_t \equiv \text{NX}_t^c + \text{NX}_t^d$. Net exports in real terms are $\text{NX}_t^{z,\text{real}} \equiv p_t^z \text{EX}_t^z - e_t \text{IM}_t^z$ for the non-durable and investment goods $z \in \{c, d\}$. Finally, the trade balance in real terms is $\text{TB}_t^{\text{real}} \equiv \text{NX}_t^{c,\text{real}} + \text{NX}_t^{d,\text{real}}$.

Exchange rate. The nominal exchange rate satisfies uncovered interest parity. Therefore, the real exchange rate satisfies

$$e_t = (1 + \pi_{t+1}) \frac{1 + r^*}{1 + r_t^m} e_{t+1} \quad (\text{B.7})$$

where r^* is the foreign interest rate, which is constant and equal to the steady state level at home $r^m = 1\%$. The terminal condition is $\lim_{t \rightarrow +\infty} e_t = 1$ by purchasing power parity and using the fact that the foreign nominal price is normalized to 1.⁶⁵

⁶⁵ We work with a finite horizon in our simulation and assume that $e_t = 1$ after 20 years.

B.2 Firm's Problem

The firm producing the investment good chooses how much to produce with intermediate (non-durable) goods, and how much to invest in capital to produce in the following period. These two problems are separable, so we characterize them sequentially.

Intermediates. The firm solves

$$\max_{X_t^{\text{dom}}} p_t^d X_t^{\text{dom}} - \left(\frac{X_t^{\text{dom}}}{A_0} \right)^{\frac{1+\zeta}{\zeta}} \quad (\text{B.8})$$

since the production function is $X_t^{\text{dom}} = A_0 M_t^{\frac{\zeta}{1+\zeta}}$ where M_t are intermediates. Therefore,

$$p_t^d = \left(\frac{X_t^{\text{dom}}}{X^{\text{potent}}} \right)^{1/\zeta}, \quad (\text{B.9})$$

which is expression (5.4) in the text, where $X^{\text{potent}} \equiv \left(\frac{\zeta}{1+\zeta} \right)^{\zeta} A_0^{1+\zeta}$ is potential output in the sector producing the investment good.

Investment. The firm's investment problem is

$$\begin{aligned} \max_{\{I_t, K_t\}} \sum_t Q_t p_t^d \{A_1 K_{t-1} - I_t\} \\ \text{s.t. } K_t \leq \left\{ 1 - \delta^K + \Phi(I_t/K_{t-1}) + z_t \right\} K_{t-1} \quad \text{and} \quad K_t \geq 0 \end{aligned} \quad (\text{B.10})$$

with initial condition $K_{-1} \equiv K$ where K is steady state capital. The price of the investment good p_t^d is expressed relative to the price of the non-durable good (Section B.1). The firm's stochastic discount factor Q_t is expressed in real terms and satisfies $Q_{t+1}/Q_t \equiv (1 + \pi_{t+1}) / (1 + r_t)$ and $Q_0 \equiv 1$. At optimum,

$$\begin{aligned} \frac{1}{\Phi'(x_t)} \frac{1 + r_t}{1 + \pi_{t+1}} \frac{p_t^d}{p_{t+1}^d} \\ = A_1 + \frac{1}{\Phi'(x_{t+1})} \left\{ 1 - \delta^K + \Phi(x_{t+1}) - x_{t+1} \Phi'(x_{t+1}) + z_{t+1} \right\} \end{aligned} \quad (\text{B.11})$$

with terminal condition $\lim_{T \rightarrow +\infty} x_T = \Phi^{-1}(\delta^K)$, where $x_t \equiv I_t/K_{t-1}$ and where we have used the definition of the firm's stochastic discount factor. The initial value problem (i.e., finding x_0) associated with this difference equation can be solved using a standard shooting algorithm.⁶⁶ The sequence of capital can then be constructed recursively using the law of motion of capital

$$K_t = \left\{ 1 - \delta^K + \Phi(x_t) + z_t \right\} K_{t-1}, \quad (\text{B.12})$$

with initial condition $K_{-1} \equiv K$.

Dividends. The firm's dividends are $\text{Div}_t = \text{Div} + \Psi_t \widehat{\text{Div}}$, where Div is the steady state dividend, and $\{\Psi_t\}$ takes the value 1 over 15 years and then decreases linearly to 0 over the next 5 years (Section 5.2). The change in dividends $\widehat{\text{Div}}$ over that period ensures that $\sum_t Q_t \text{Div}_t = \sum_t Q_t \Pi_t$ where Π_t are real profits. Therefore,

$$\text{Div}_t = \text{Div} + \Psi_t \frac{\sum_s Q_s \{\Pi_s - \text{Div}\}}{\sum_s Q_s \Psi_s} \quad (\text{B.13})$$

Finally, real profits are

$$\Pi_t \equiv p_t^d X_t^{\text{dom}} - \left(\frac{X_t^{\text{dom}}}{A_0} \right)^{\frac{1+\zeta}{\zeta}} + p_t^d (A_1 K_{t-1} - I_t), \quad (\text{B.14})$$

using the fact that $p_t^c \equiv 1$ in the non-durables sector (Appendix B.1).

B.3 Investment Shocks

We are interested in constructing a sequence of investment shocks $\{z_t\}$ that produces a particular recession, i.e., a path for aggregate output

$$Y_t^{\text{GDP}} \equiv C_t + X_t + I_t + G + \text{TB}_t \quad (\text{B.15})$$

⁶⁶ Expression (B.11) defines a unique map $x_t \mapsto x_{t+1}$ since the right-hand side is increasing in $x \geq 0$ as $\Phi(x) - x\Phi'(x)$ is also increasing given our choice $\Phi(x) = 1/\kappa(\sqrt{1+2\kappa x} - 1)$ with $\kappa \equiv 2$ and $1 - \delta^K + z_{t+1} > 0$ when z_{t+1} is positive (during a recession) or sufficiently small. This is the case in our numerical simulations (Appendix B.3).

as defined in Section 5.1. We show below that this sequence of shocks can be constructed in a straightforward way despite the non-linearities inherent to the demand side of our economy. In the following, we let $C_t(\cdot)$, $X_t(\cdot)$ and $TB_t(\cdot)$ denote total demands and the quantity index for the trade balance as a function of households' aggregate income before interest and tax payments $\{Y_t^{inc}\}$.

Lemma 1. *Consider a sequence of aggregate output $\{Y_t^{GDP}\}$ that converges to its steady state level $Y_t^{GDP} \rightarrow Y^{GDP}$ as $t \rightarrow +\infty$. There exists a (unique) sequence of investment shocks $\{z_t\}$ that induces this output in equilibrium. It can be constructed in four steps.*

Step 1 (Net investments). Fix an initial guess for incomes $\{Y_t^{inc}\}$, e.g., $Y_t^{inc} = Y^{inc}$ for each period $t \geq 0$. Back out the sequence of investments $\{I_t\}$ residually from the resource constraint

$$I_t \equiv Y_t^{GDP} - C_t\left(\{Y_t^{inc}\}\right) - X_t\left(\{Y_t^{inc}\}\right) - G - TB_t\left(\{Y_t^{inc}\}\right)$$

Step 2 (Investment shocks). Fix an initial guess for capital $\{K_t\}$, e.g., $K_{t-1} = K$ for each period $t \geq 0$. Compute the investment rates $x_t \equiv I_t/K_{t-1}$ using the sequence of investment from the previous step. Back out the sequence of investment shocks $\{z_t\}$ from the firm's Euler equation

$$z_{t+1} = \frac{\Phi'(x_{t+1})}{\Phi'(x_t)} \frac{1+r_t}{1+\pi_{t+1}} \frac{p_t^d}{p_{t+1}^d} - (A_1 - x_{t+1}) \Phi'(x_{t+1}) - \left\{1 - \delta^K + \Phi(x_{t+1})\right\}$$

with the normalization $z_0 \equiv 0$.⁶⁷ Given this sequence of investment rates and investment shocks, compute a new sequence of capital $\{K'_t\}$ using the law of motion

$$K'_t = \left\{1 - \delta^K + \Phi(x_t) + z_t\right\} K'_{t-1},$$

for each $t \geq 0$, with initial condition $K'_{-1} = K$. Update the initial guess for capital $\{K_t\}$ using $\{K'_t\}$ and repeat Step 2 until convergence. This yields a sequence of investment shocks $\{z_t\}$ such that the firm chooses investments $\{I_t\}$ given equilibrium prices.

⁶⁷ The investment rates $\{x_t\}$ depend on the *expected* shocks $\{z_{t+1}\}$, as is apparent from the firm's Euler equation (B.11). We normalize $z_0 \equiv 0$ because the purpose of these shocks is to act as aggregate demand shifters by affecting investment (not the initial stock of capital).

Step 3 (Incomes and prices). Update incomes, prices, taxes, and the interest rate: households' aggregate income Y_t^{inc} is given by (5.9) where Div_t is given by (B.13); prices are computed using equations (5.2), (5.4) and (B.1); taxes are given by the constraints (B.18)–(B.19); and the interest rate satisfies the rule (5.6). Repeat the previous steps until convergence. The resulting sequence of investment shocks $\{z_t\}$ is the one that implements the sequence of aggregate output $\{Y_t^{\text{GDP}}\}$ in equilibrium.

Proof. The sequence of shocks $\{z_t\}$ induces aggregate outputs $\{Y_t^{\text{GDP}}\}$ in equilibrium if and only if the following conditions are satisfied: (i) the firm's Euler equation (B.11); (ii) the law of motion of capital (B.12); (iii) incomes, prices and taxes are given by the expressions described in Step 2; and (iv) aggregate output satisfies (B.15) with consumption, investment and the trade balance given by $C_t(\cdot)$, $X_t(\cdot)$ and $\text{TB}_t(\cdot)$.⁶⁸ The result simply combines these equilibrium conditions. \square

B.4 Fiscal Policy

Budget constraint. The government's budget constraint is

$$B_t^g + P_t^c G + t_t = \frac{1 + r_{t-1}}{1 + \pi_t} B_{t-1}^g + \int \left(y Y_t^{\text{inc}} - \psi_{0,t} \left(y Y_t^{\text{inc}} \right)^{1-\psi_1} \right) d\mu_{t-1} + \Sigma_t \quad (\text{B.16})$$

Instead of introducing passive financial intermediaries, we suppose that the government claims the net payments on credit from households

$$\Sigma_t \equiv (1 - \theta) \times \left\{ \left(1 + r_{t-1}^b \right) \hat{P}_t^d D_{t-1} - P_{t+1}^d (1 + \pi_{t+1}) D_t \right\} \quad (\text{B.17})$$

The pre-determined stock of durables is $D_{t-1} \equiv \int d \times \mu_{t-1}(d\mathbf{x})$. The price \hat{P}_t^d was defined in Appendix A.1.

Taxes. The tax intercept is $\psi_{0,t} = \psi_0 + \Psi_t \hat{\psi}_0$, where ψ_0 is the intercept at steady state and $\{\Psi_t\}$ was defined in Appendix B.1. The change $\hat{\psi}_0$ ensures that the government's tax revenues are equal to its spending in present discounted value. Therefore, the tax intercept is

⁶⁸ Necessity uses the fact that the firm's problem (B.10) is convex.

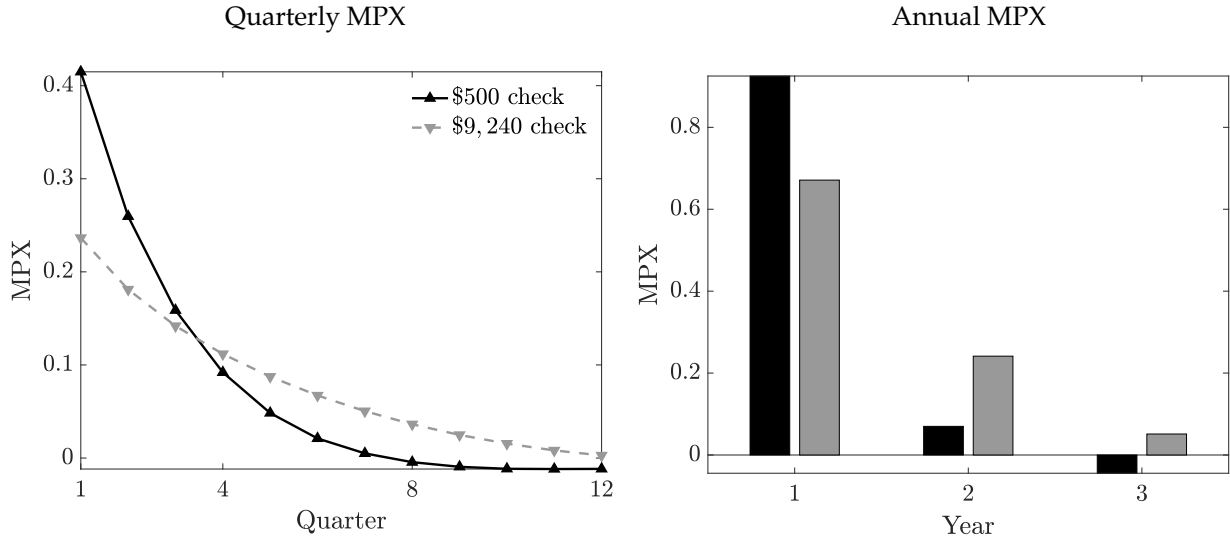
$$\psi_{0,t} = \psi_0 + \Psi_t \frac{\sum_t Q_t \Omega_t + \frac{1+r_{-1}}{1+\pi_0} B_{-1}^g}{\sum_t Q_t \Psi_t \int (yE_t)^{1-\psi_1} d\mu_{t-1}} \quad (\text{B.18})$$

where

$$\Omega_t \equiv \int yE_t d\mu_{t-1} - \psi_0 \int (yE_t)^{1-\psi_1} d\mu_{t-1} + \Sigma_t - t_t - P_t^c G_t \quad (\text{B.19})$$

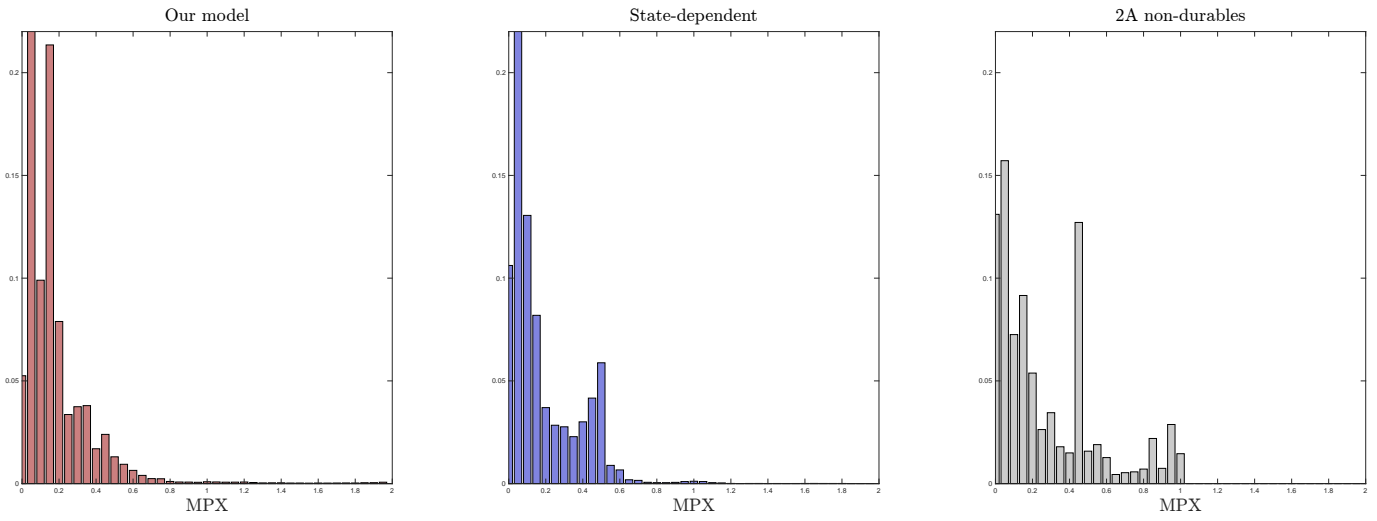
C Additional Quantitative Results

Figure C.1: Dynamic responses in our model



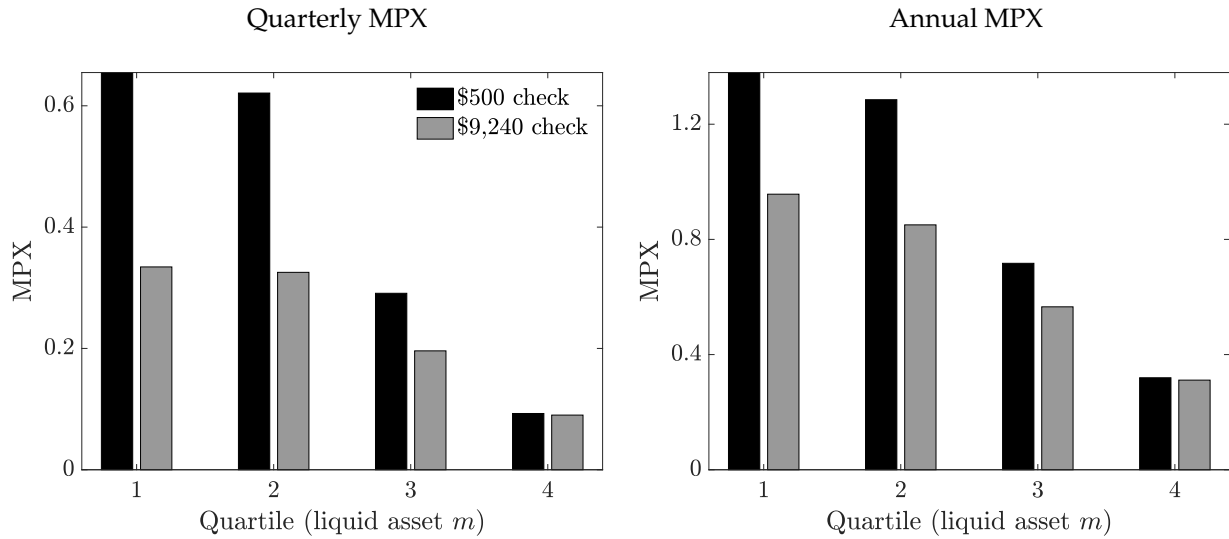
Notes: The left panel plots the total MPX over time to a check received in the first quarter. We repeat this experiment for checks of \$500 and \$9,240 (the average lottery gain in [Fagereng et al., 2021](#)). The right panel reports the associated annual MPXs.

Figure C.2: Distribution of MPXs (out of \$500)



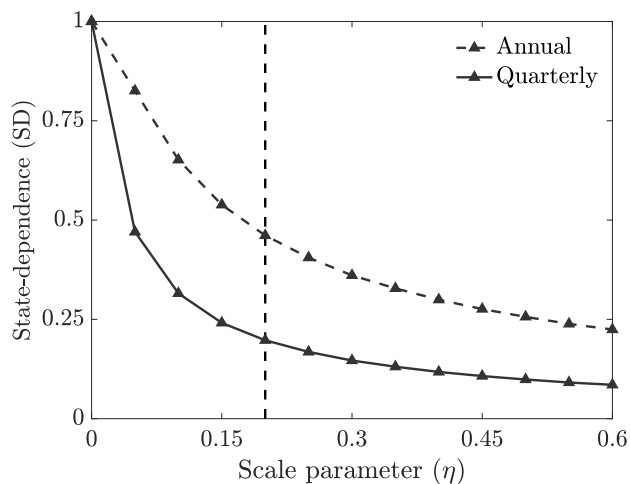
Notes: This figure plots the distribution of MPXs out of \$500 in our model (in red), in the fully state-dependent model (in blue), and in the two-asset model of non-durables (in grey).

Figure C.3: MPX and liquid assets



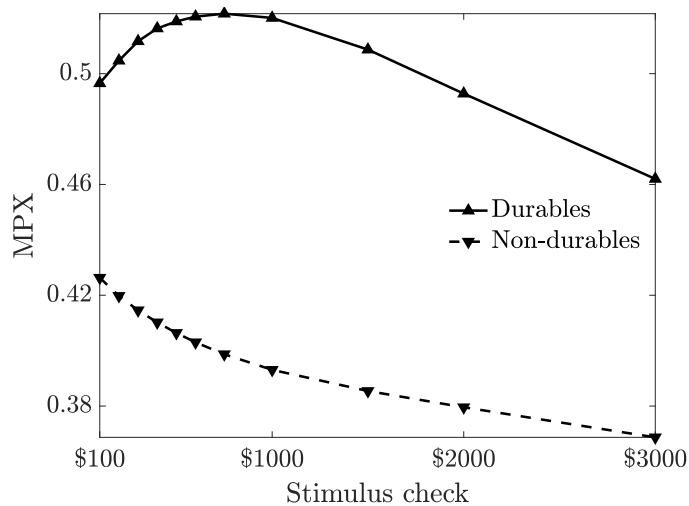
Notes: The left panel plots the total MPX in the first quarter in our model for each quartile of the distribution of liquid assets. We repeat this experiment for checks of \$500 and \$9,240 (the average lottery gain in [Fagereng et al., 2021](#)). The right panel reports the same at the annual frequency.

Figure C.4: State- vs. time-dependent adjustments



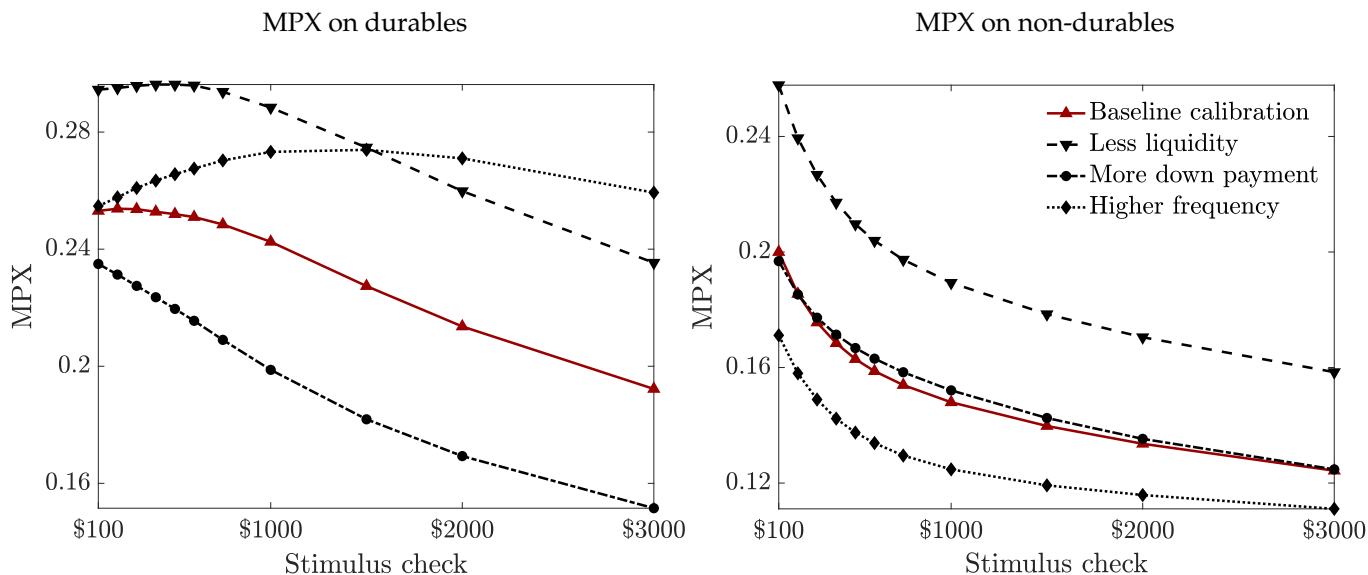
Notes: The figure plots our state-dependence index SD in (3.1) as a function of the scale parameter η . All other parameters are re-calibrated to match the targets discussed in Section 3.2. The vertical dashed line is our preferred calibration $\eta = 0.2$.

Figure C.5: Size-dependence in the MPX in our model (annual)



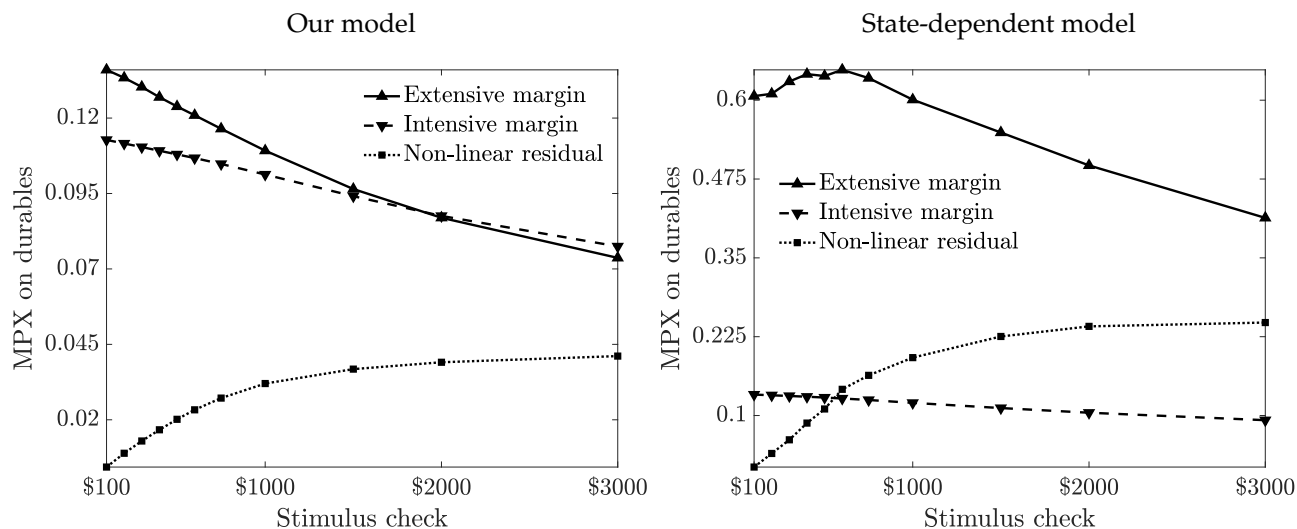
Notes: This figure plots the MPX on durables and non-durables at the annual frequency in our model as a function of the size of stimulus checks.

Figure C.6: Sensitivity analysis



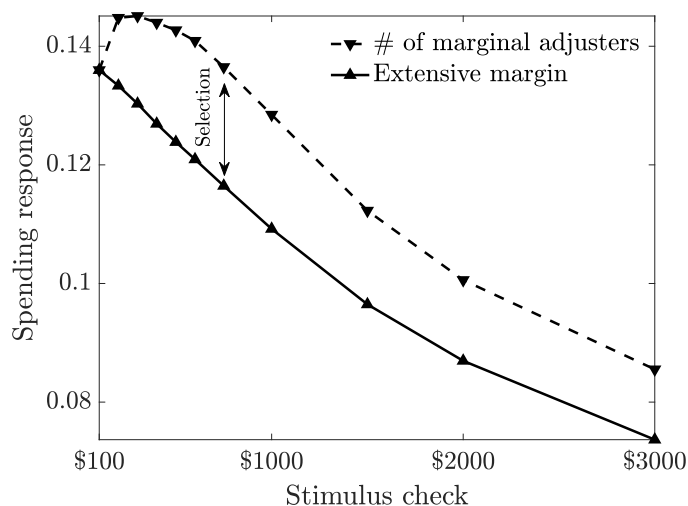
Notes: This figure plots the MPX on durables (left) and non-durables (right) at the quarterly frequency in our model (red) and in three alternative calibrations with lower liquidity (13% of average annual income instead of 26%), more down payment ($\theta = 30\%$ instead of $\theta = 20\%$), and higher frequency of adjustment (35% instead of 25%).

Figure C.7: Decomposing the MPX on durables



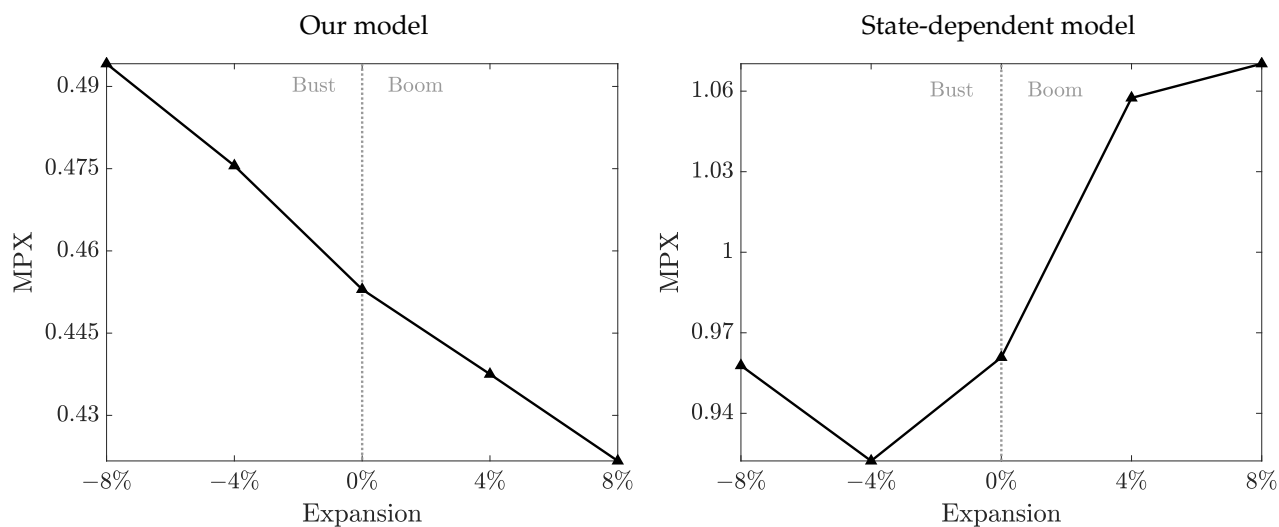
Notes: The left panel decomposes the MPX on durables in our model. The solid and dashed curves are the extensive and intensive margins. The dotted curve is the non-linear residual that captures the interaction between the two margins. The right panel is the same for the purely state-dependent model.

Figure C.8: Decomposing the extensive margin in our model



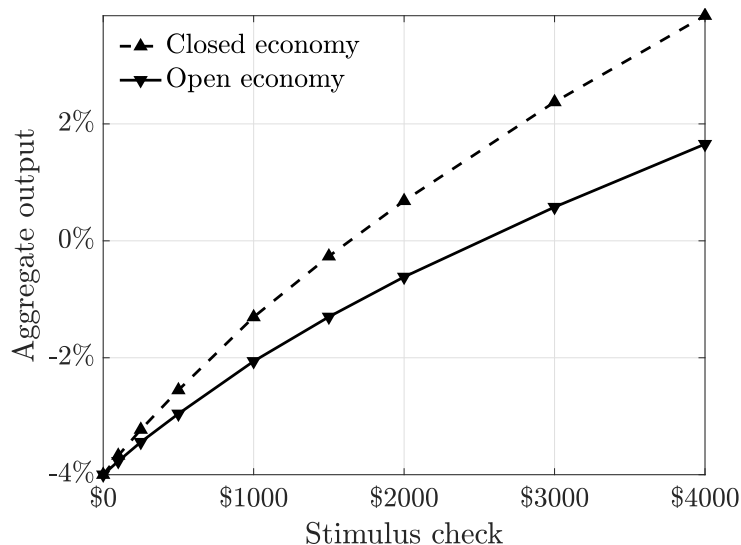
Notes: This figure decomposes the extensive margin into the two components in the first term of expression (4.1). The solid curve is the extensive margin. The dashed curve captures the rate at which households adjust $\{S(d, m + T, y) - S(d, m, y)\} X/T$ where X ensures that the two curves coincide for a check of \$100. By construction, the difference between these two curves captures the selection effect.

Figure C.9: Aggregate conditions (MPX out of \$500)



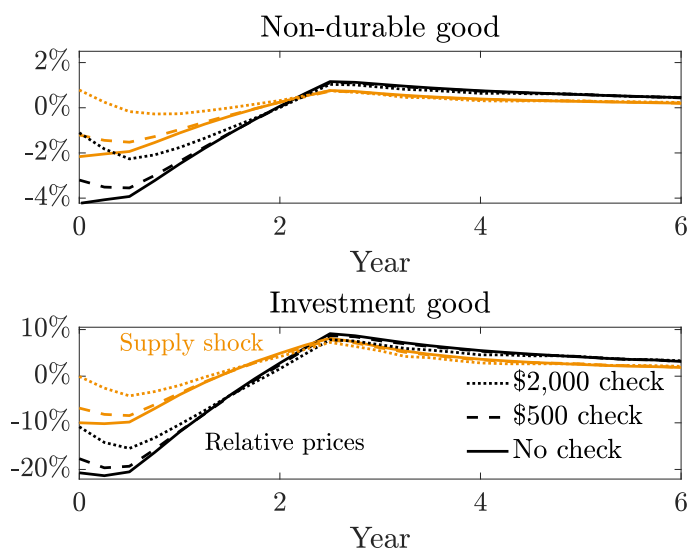
Notes: The left panel plots the MPX out of \$500 in our model at various points of the business cycle. The stimulus checks are received unexpectedly after three quarters of constant expansion (or contraction), following by a linear mean-reversion over eight quarters. The right panel plots the same for the purely state-dependent model.

Figure C.10: Aggregate output ($t = 0$) in closed and open economy



Notes: This figure plots aggregate output (in deviations from steady state) in the first quarter as a function of the size of stimulus checks. The solid curve is our the general equilibrium model presented in Sections 5.1–5.2. The dashed curve is a closed-economy version where households only spend on domestic varieties so $\alpha_d^F = \alpha_c^F = 0$.

Figure C.11: Sectoral output gaps with a supply shock



Notes: This figure plots the sectoral output gaps over time for various stimulus checks. The black and orange curves correspond to the same models as in Figure 5.3.

D Alternative Models

This appendix describes the two alternative models that we discuss in the paper. Section D.1 presents a two-asset model of non-durables. Section D.2 presents a Calvo-Plus model of durables.

D.1 Two-Asset Model of Non-Durables

In Sections 3–5, we compare the predictions of our model to those of a two-asset model of non-durables similar to Kaplan and Violante (2022). We state the household’s problem recursively and discuss the calibration. Households are indexed by three idiosyncratic states: their holdings of illiquid financial asset (b); their holdings of liquid financial asset (m); and their idiosyncratic income (y). As before, we let $\mathbf{x} \equiv (b, m, y)$ denote the vector of states.

Continuation values. The continuation values $\{V_t(\cdot)\}$ can be characterized recursively as follows:⁶⁹

1. **Discrete choice.** The household chooses whether to adjust its stock of illiquid asset. The value associated to the discrete choice problem is

$$V_t(\mathbf{x}) \equiv \max \left\{ V_t^{\text{adjust}}(b + m, y) - \kappa, V_t^{\text{not}}(b, m, y) \right\} \quad (\text{D.1})$$

where V_t^{adjust} is the continuation value when adjusting the stock of illiquid assets, V_t^{not} is the continuation value when not adjusting, and $\kappa > 0$ is the adjustment cost.

2. **Illiquid asset adjustment.** If the household decides to adjust its stock of illiquid assets, it chooses its new stock of illiquid assets

$$V_t^{\text{adjust}}(m, y) \equiv \max_{b', m'} V_t^{\text{not}}(b', m', y) \quad (\text{D.2})$$

$$\text{s.t. } b' + m' \leq m, \quad b' \geq 0$$

The continuation value V_t^{not} reflects the subsequent optimal consumption-saving choice that occurs in the same period.

⁶⁹ Again, the terminal condition for $V_{t+1}(\cdot)$ is the stationary value without stimulus checks.

3. **Consumption-saving.** If the household decides not to adjust its stock of illiquid assets, it chooses how much to consume and save in liquid asset

$$V_t^{\text{not}}(\mathbf{x}) \equiv \max_{c, m'} u(c) + \beta \int V_{t+1}(b, m', y') \Gamma(dy'; y) \quad (\text{D.3})$$

$$\text{s.t. } P_t^c c + m' \leq m \quad \text{and} \quad m' \geq 0$$

Calibration. The calibration strategy follows [Kaplan and Violante \(2022\)](#) closely. We set $u(c) = 1 / (1 - \sigma) c^{1-\sigma}$ with inverse elasticity of intertemporal substitution $\sigma \rightarrow 1$, as is usual in models of non-durable spending. We set the (real) return on cash to -2% per year and the spread to 6% per year.⁷⁰ We discipline internally two parameters: the discount factor (β); and the adjustment cost (κ). We calibrate these parameters to match a share of total hand-to-mouth households of 41% , and a share of wealthy hand-to-mouth (with positive holdings of b) of 27% as in [Kaplan and Violante \(2022\)](#).

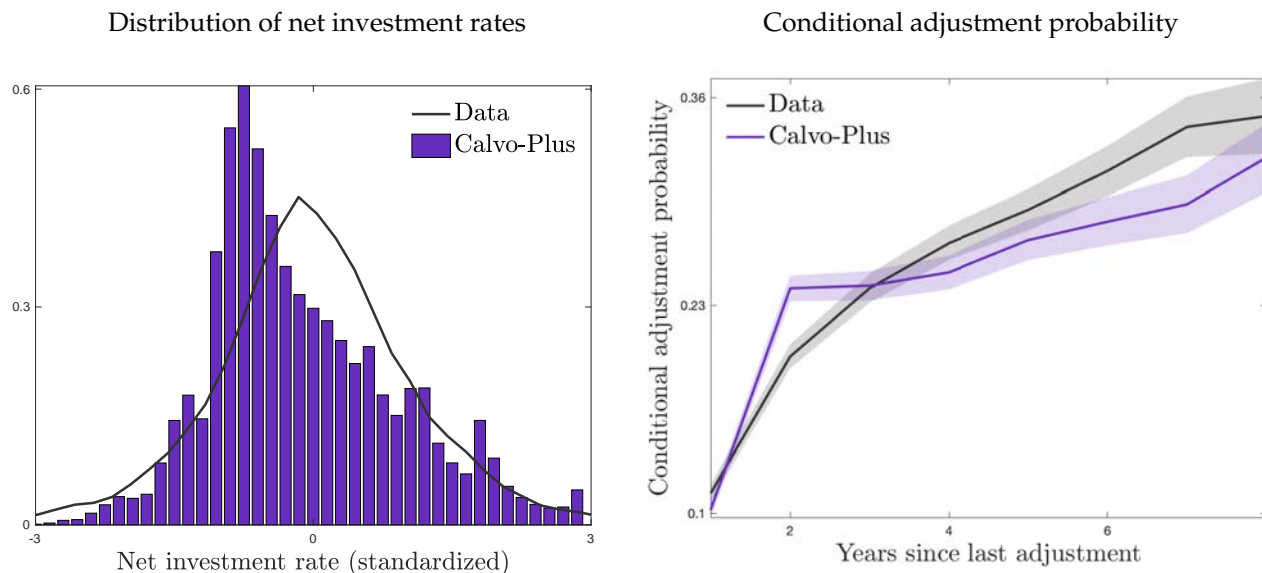
D.2 Calvo-Plus Model

Our smooth adjustment hazard (2.1) can be microfounded by introducing random taste shocks for adjustment (as in [McFadden, 1973](#)) to generate some time-dependence in durable adjustment. The distribution of shocks is smooth and has full support. An alternative approach would be to assume that the distribution is degenerate on two points $\{0, \kappa\}$. Either households can adjust freely or they face a constant fixed cost $\kappa > 0$. While a degenerate distribution is harder to justify empirically, this type of “Calvo-Plus” models is sometimes used in the price setting literature ([Nakamura and Steinsson, 2010](#)). [McKay and Wieland \(2021\)](#) use a related device for durable spending (amongside other frictions) to study the response to monetary policy shocks.⁷¹ This two-point distribution still generates a

⁷⁰ The real effective lower bound on the interest rate is -2% in our durables model (Section 5.2). In the two-asset model of non-durables, this would imply that the lower bound is binding even in steady state. Instead, we assume that monetary policy can decrease the interest rate by 3% in both model before it hits its effective lower bound. Indeed, $r^m - \underline{r} = 3\%$ in our durables model.

⁷¹ [McKay and Wieland \(2021\)](#) assume that households are *forced* to adjust, as opposed to being *allowed* to adjust for free. Effectively, households face a constant adjustment cost κ and occasionally experience an infinite disutility of *not* adjusting. This formulation is equivalent to the Calvo-Plus one: households who are given the choice to adjust freely do so with probability one, which amounts to forcing them to adjust.

Figure D.1: Untargeted moments in the Calvo-Plus model



Notes: The left panel plots the distribution of net investment rates (standardized) across two consecutive PSID waves between which households adjusted their stock of durables. The black curve is the data, while the purple bars are the Calvo-Plus model. The right panel plots the adjustment probability conditional on a household not having adjusted so far. The confidence intervals are bootstrapped (10%).

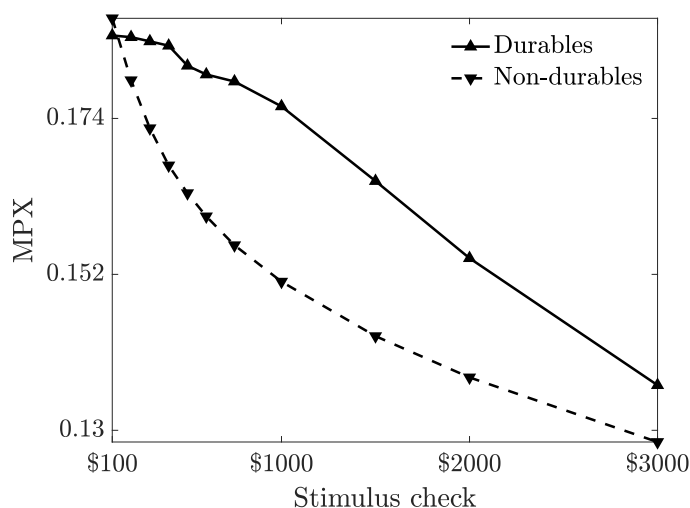
discontinuous hazard with (s, S) bands but the intercept is shifted up (see Figure 2.1). Because this distribution is used in the literature, we find it useful to inspect the ability of this formulation to match the micro level moments discussed in Section 3. To make sure that the models are comparable, we match the same short-run price elasticity of durable demand (Figure 3.1) as in our model, which is informative about the degree of time-dependence (and hence the “Calvo-ness”). All other parameters are re-calibrated to match the targets discussed in Section 3.2.

Figure D.1 plots two of the untargeted moments that we inspected in Section 3.3, but this time for the Calvo-Plus model. Overall, the distribution of adjustment rates provides a poorer fit to the data compared to our model (left panel of Figure 3.2). The distribution is skewed and the model generates a lot of very small adjustments, as is expected in a Calvo-Plus model.⁷² The conditional probability of adjustment is somewhat steeper between years 1 and 2 (right panel of Figure D.1), as in our model. After that, the conditional probability is very flat, as expected in

⁷²This distribution is standardized, as usual (Alvarez et al., 2016a). This explains why the mode (corresponding to very small adjustments) is not located exactly at zero.

a Calvo-Plus model, whereas it increases steadily in the data. In fact, the Calvo-Plus is almost purely time-dependent: the measure of state-dependence that we introduced in Section 3.4 is 10% at the quarterly frequency and 11% at the annual one, compared to 23% and 50% in our model (Figure C.4). Unsurprisingly, the Calvo-Plus model generates a lower MPX on durables out of a \$500 check (18%) compared to our model (25%) and the preferred estimate of Orchard et al. (2022) (30%). The MPX on durables and non-durables are roughly equal to each other in the Calvo-Plus model, whereas the MPX on durables is about one and a half times as large as the MPX on non-durables in our model and in the data (Section 3.2). Figure D.2 plots the size-dependence in the MPX on durables and non-durables in the Calvo-Plus model. The MPX on durables is not only lower in the Calvo-Plus model, it also declines faster relative to our model (Figure 4.1) as the Calvo-Plus model is more time-dependent.

Figure D.2: Size-dependence in the MPX in the Calvo-Plus model



Notes: This figure plots the MPX on durables and non-durables in the Calvo-Plus model as a function of the size of stimulus checks.

References

- ALVAREZ, F., H. LE BIHAN, AND F. LIPPI (2016a): “The Real Effects of Monetary Shocks in Sticky Price Models: A Sufficient Statistic Approach,” *American Economic Review*, 106, 2817–51.
- ARTUÇ, E., S. CHAUDHURI, AND J. MCLAREN (2010): “Trade Shocks and Labor

- Adjustment: A Structural Empirical Approach," *American Economic Review*, 100, 1008–1045.
- (2015): "Consumption Dynamics During Recessions," *Econometrica*, 83, 101–154.
- CARROLL, C. D. (2006): "The method of endogenous gridpoints for solving dynamic stochastic optimization problems," *Economics Letters*, 91, 312–320.
- CLAUSEN, A. AND C. STRUB (2012): "Envelope theorems for non-smooth and non-concave optimization," ECON - Working Papers 062, Department of Economics - University of Zurich.
- DRUEDAHL, J. AND T. H. JØRGENSEN (2017): "A general endogenous grid method for multi-dimensional models with non-convexities and constraints," *Journal of Economic Dynamics and Control*, 74, 87–107.
- FAGERENG, A., M. B. HOLM, AND G. J. NATVIK (2021): "MPC Heterogeneity and Household Balance Sheets," *American Economic Journal: Macroeconomics*, 13, 1–54.
- GAVAZZA, A. AND A. LANTERI (2021): "Credit Shocks and Equilibrium Dynamics in Consumer Durable Goods Markets," *The Review of Economic Studies*, 88, 2935–2969.
- (2022): "The Marginal Propensity to Consume in Heterogeneous Agent Models," *Annual Review of Economics*, 14, 747–775.
- MCFADDEN, D. (1973): *Conditional Logit Analysis of Qualitative Choice Behavior*, Institute of Urban and Regional Development, University of California.
- MCKAY, A. AND J. F. WIELAND (2021): "Lumpy Durable Consumption Demand and the Limited Ammunition of Monetary Policy," *Econometrica*, 89, 2717–2749.
- NAKAMURA, E. AND J. STEINSSON (2010): "Monetary Non-neutrality in a Multi-sector Menu Cost Model," *The Quarterly Journal of Economics*, 125, 961–1013.
- ORCHARD, J., V. A. RAMEY, AND J. F. WIELAND (2022): "Micro MPCs and Macro Counterfactuals: The Case of the 2008 Rebates," Tech. rep., UCSD Mimeo.
- ROUWENHORST, G. (1995): *Asset Pricing Implications of Equilibrium Business Cycle Models*, vol. Chapter 10, *Frontiers of Business Cycle Research*, Princeton University Press.
- YOUNG, E. R. (2010): "Solving the incomplete markets model with aggregate uncertainty using the Krusell-Smith algorithm and non-stochastic simulations," *Journal of Economic Dynamics and Control*, 34, 36–41.