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Risk, Uncertainty and Monetary Policy  
Geert Bekaert, Marie Hoerova, and Marco Lo Duca  
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### **ABSTRACT**

The VIX, the stock market option-based implied volatility, strongly co-moves with measures of the monetary policy stance. When decomposing the VIX into two components, a proxy for risk aversion and expected stock market volatility (“uncertainty”), we find that a lax monetary policy decreases both risk aversion and uncertainty, with the former effect being stronger. The result holds in a structural vector autoregressive framework, controlling for business cycle movements and using a variety of identification schemes for the vector autoregression in general and monetary policy shocks in particular.

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## 1. Introduction

A popular indicator of risk aversion in financial markets, the VIX index, shows strong co-movements with measures of the monetary policy stance. Figure 1 considers the cross-correlogram between the real interest rate (the Fed funds rate minus inflation), a measure of the monetary policy stance, and the logarithm of end-of-month readings of the VIX index. The VIX index essentially measures the “risk-neutral” expected stock market variance for the US S&P500 index. The correlogram reveals a very strong positive correlation between real interest rates and future VIX levels. While the current VIX is positively associated with future real rates, the relationship turns negative and significant after 13 months: high VIX readings are correlated with expansionary monetary policy in the medium-run future.

The strong interaction between a “fear index” (Whaley (2000)) in the asset markets and monetary policy indicators may have important implications for a number of literatures. First, the recent crisis has rekindled the idea that lax monetary policy can be conducive to financial instability. The Federal Reserve’s pattern of providing liquidity to financial markets following market tensions, which became known as the “Greenspan put,” has been cited as one of the contributing factors to the build-up of a speculative bubble prior to the 2007-09 financial crisis.<sup>1</sup> Whereas some rather informal stories have linked monetary policy to risk-taking in financial markets (Rajan (2006), Adrian and Shin

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<sup>1</sup> Investors increasingly believed that when market conditions were to deteriorate, the Fed would step in and inject liquidity until the outlook improved. Such perception may encourage excessive risk-taking and lead to higher valuations and narrower credit spreads. See, for example, “Greenspan Put may be Encouraging Complacency,” Financial Times, December 8, 2000.

(2008), Borio and Zhu (2008)), it is fair to say that no extant research establishes a firm empirical link between monetary policy and risk aversion in asset markets.<sup>2</sup>

Second, Bloom (2009) and Bloom, Floetotto and Jaimovich (2009) show that heightened “economic uncertainty” decreases employment and output. It is therefore conceivable that the monetary authority responds to uncertainty shocks, in order to affect economic outcomes. However, the VIX index, used by Bloom (2009) to measure uncertainty, can be decomposed into a component that reflects actual expected stock market volatility (uncertainty) and a residual, the so-called variance premium (see, for example, Carr and Wu (2009)), that reflects risk aversion and other non-linear pricing effects, perhaps even Knightian uncertainty. Establishing which component drives the strong co-movements between the monetary policy stance and the VIX is therefore particularly important.

Third, analyzing the relationship between monetary policy and the VIX and its components may help clarify the relationship between monetary policy and the stock market, explored in a large number of empirical papers (Thorbecke (1997), Rigobon and Sack (2004), Bernanke and Kuttner (2005)). The extant studies all find that expansionary (contractionary) monetary policy affects the stock market positively (negatively). Interestingly, Bernanke and Kuttner (2005) ascribe the bulk of the effect to easier monetary policy lowering risk premiums, reflecting both a reduction in economic and financial volatility and an increase in the capacity of financial investors to bear risk. By using the VIX and its two components, we test the effect of monetary policy on stock market risk, but also provide more precise information on the exact channel.

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<sup>2</sup> For recent empirical evidence that monetary policy affects the riskiness of loans granted by banks see, for example, Altunbas, Gambacorta and Marquéz-Ibañez (2010), Ioannidou, Ongena and Peydró (2009), Jiménez, Ongena, Peydró and Saurina (2009), and Maddaloni and Peydró (2010).

This article characterizes the dynamic links between risk aversion, economic uncertainty and monetary policy in a simple vector-autoregressive (VAR) system. Such analysis faces a number of difficulties. First, because risk aversion and the stance of monetary policy are jointly endogenous variables and display strong contemporaneous correlation (see Figure 1), a structural interpretation of the dynamic effects requires identifying restrictions. Monetary policy may indeed affect asset prices through its effect on risk aversion, as suggested by the literature on monetary policy news and the stock market, but monetary policy makers may also react to a nervous and uncertain market place by loosening monetary policy. In fact, Rigobon and Sack (2003) find that the Federal Reserve does systematically respond to stock prices.<sup>3</sup>

Second, the relationship between risk aversion and monetary policy may also reflect the joint response to an omitted variable, with business cycle variation being a prime candidate. Recessions may be associated with high risk aversion (see Campbell and Cochrane (1999) for a model generating counter-cyclical risk aversion) and at the same time lead to lax monetary policy. Our VARs always include a business cycle indicator.

Third, measuring the monetary policy stance is the subject of a large literature (see, for example, Bernanke and Mihov (1998a)); and measuring policy shocks correctly is difficult. Models featuring time-varying risk aversion and/or uncertainty, such as Bekaert, Engstrom and Xing (2009), imply an equilibrium contemporaneous link between interest rates and risk aversion and uncertainty, through precautionary savings effects for example. Such relation should not be associated with a policy shock. However, our

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<sup>3</sup> The two papers by Rigobon and Sack (2003, 2004) use an identification scheme based on the heteroskedasticity of stock market returns. Given that we view economic uncertainty as an important endogenous variable in its own right with links to the real economy and risk premiums, we cannot use such an identification scheme.

results are robust to alternative measures of the monetary policy stance and of monetary policy shocks. In particular, the results are robust to identifying monetary policy shocks using a standard structural VAR, high frequency Fed funds futures changes following Gürkaynak, Sack and Swanson (2005), and monthly surprises based on the daily Fed funds futures following the approach in Bernanke and Kuttner (2005).

The remainder of the paper is organized as follows. In Section 2, we detail the measurement of the key variables in the VAR, including monetary policy indicators, monetary policy shocks and business cycle indicators. First and foremost, we provide intuition on how the VIX is related to the actual expected variance of stock returns and to risk preferences. While the literature has proposed a number of risk appetite measures (see Baker and Wurgler (2007) and Coudert and Gex (2008)), our measure is monotonically increasing in risk aversion in a variety of economic settings. This motivates our empirical strategy in which we split the VIX into a pure volatility component (“uncertainty”) and a residual, which should be more closely associated with risk aversion. In Section 3, we analyze the dynamic relationship between monetary policy and risk aversion and uncertainty in standard structural VARs. The results are remarkably robust to a long list of robustness checks with respect to VAR specification, variable definitions and alternative identification methods. In Section 4, we use two alternative methods to identify monetary policy shocks relying on Fed futures data.

Our main findings are as follows. A lax monetary policy decreases risk aversion in the stock market after about nine months. This effect is persistent, lasting for more than two years. Moreover, monetary policy shocks account for a significant proportion of the variance of risk aversion. The effects of monetary policy on uncertainty are similar but

somewhat weaker. On the other hand, periods of both high uncertainty and high risk aversion are followed by a looser monetary policy stance but these results are less robust and much weaker statistically. Finally, it is the uncertainty component of the VIX that has the statistically stronger effect on the business cycle, not the risk aversion component.

## **2. Measurement**

This section details the measurement of the key inputs to our analysis: risk aversion and uncertainty; the monetary policy stance and monetary policy shocks; and finally, business cycle variation. Our data start in January 1990 (the start of the model-free VIX series) but we perform our analysis using two different end-points for the sample: July 2007, yielding a sample that excludes recent data on the crisis; and August 2010. The crisis period presents special challenges as stock market volatilities peaked at unprecedented levels and the Fed funds target rate reached the zero lower bound. We detail how we address these challenges below. Table 1 describes the basic variables we use and assigns them a short-hand label.

### **2.1 Measuring Risk Aversion and Uncertainty**

To measure risk aversion and uncertainty, we use a decomposition of the VIX index. The VIX represents the option-implied expected volatility on the S&P500 index with a horizon of 30 calendar days (22 trading days). This volatility concept is often referred to as “implied volatility” or “risk-neutral volatility,” as opposed to the actual (or “physical”) expected volatility. Intuitively, in a discrete state economy, the physical volatility would use the actual state probabilities to arrive at the physical expected variance, whereas the risk-neutral variance would make use of probabilities that are adjusted for the pricing of risk.

The computation of the actual VIX index relies on theoretical results showing that option prices can be used to replicate any bounded payoff pattern; in fact, they can be used to replicate Arrow-Debreu securities (Breedon and Litzenberger (1978), Bakshi and Madan (2000)). Britten-Jones and Neuberger (2000) and Bakshi, Kapadia and Madan (2003) show how to infer “risk-neutral” expected volatility for a stock index from option prices. The VIX index measures implied volatility using a weighted average of European-style S&P500 call and put option prices that straddle a 30-day maturity and cover a wide range of strikes (see CBOE (2004) for more details). Importantly, this estimate is model-free and does not rely on an option pricing model.

While the VIX obviously reflects stock market uncertainty, it conceptually must also harbor information about risk and risk aversion. Indeed, financial markets often view the VIX as a measure of risk aversion and fear in the market place. Because there are well-accepted techniques to measure the physical expected variance, we can split the VIX into a measure of stock market or economic uncertainty, and a residual that should be more closely associated with risk aversion. The difference between the squared VIX and an estimate of the conditional variance is typically called the variance premium (see, e.g., Carr and Wu (2009)).<sup>4</sup> The variance premium is nearly always positive and displays substantial time-variation. Recent finance models attribute these facts either to non-Gaussian components in fundamentals and (stochastic) risk aversion (see, for instance, Bekaert and Engstrom (2010), Bollerslev, Tauchen and Zhou (2009), Drechsler and Yaron (2011)) or Knightian uncertainty (see Drechsler (2009)). In the Appendix, we use a one-period discrete economy with power utility to illustrate the difference between

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<sup>4</sup> In the technical finance literature, the variance premium is actually the negative of the variable that we use. By switching the sign, our indicator increases with risk aversion, whereas the variance premium becomes more negative with risk aversion.



“risk neutral” and “physical” expected volatility and demonstrate that the variance premium is indeed increasing in risk aversion.

To decompose the VIX index into a risk aversion and an uncertainty component, we first estimate the expected future realized variance. It is customary in the literature to do so by projecting future realized monthly variances (computed using squared 5-minute returns) onto a set of current instruments. We follow this approach using daily data on monthly realized variances, the squared VIX, the dividend yield and the real three-month T-bill rate. By using daily data, we gain considerable statistical power relative to the standard methods employing end-of-month data. For example, forecasting models estimated from daily data easily “beat” models using only end-of-month data, even for end-of-month samples.

To select a good forecasting model, we conduct a horserace between a total of eight volatility forecasting models. The first five models use OLS regressions with different predictors: a one-variable model with either the past realized variance or the squared VIX; a two-variable model with both the squared VIX and the past realized variance; a three-variable model adding the past dividend yield; and a four-variable model adding the past real three-month T-bill rate. We also consider three models that do not require estimation: half-half weights on the past squared VIX and past realized variance; the past realized variance; the past squared VIX. We consider two model selection criteria: out-of-sample root-mean-squared error and mean absolute errors, and, for the estimated models, stability (especially through the crisis period).

This procedure leads us to select a two-variable model where the squared VIX and the past realized variance are used as predictors. The performance of the three and four

variable models is very comparable to this model, but the univariate estimated models and the non-estimated models perform consistently and significantly worse. Moreover, the model that we selected is the most stable of the well-performing forecasting models we considered, with the coefficients economically and statistically unaltered during the crisis period. In the online Appendix, we give a detailed account of the forecasting horserace. The resulting coefficients from the two-variable projection are as follows:<sup>5</sup>

$$\text{RVAR}_t = -0.00002 + 0.299 \text{VIX}_{t-22}^2 + 0.442 \text{RVAR}_{t-22} + e_t \quad (1)$$

(0.00012) (0.067) (0.130)

The standard errors reported in parentheses are corrected for serial correlation using 30 Newey-West (1987) lags.

The fitted value from the two-variable projection is the estimated physical expected variance (“uncertainty”). We use the logarithm of this estimate in our analysis and label it UC. We call the difference between the squared VIX and UC “risk aversion” (the logarithm of which is labeled as RA). We plot the risk aversion and uncertainty estimates in Figure 2, along with 90% confidence intervals.<sup>6</sup> To construct the confidence bounds, we retain the coefficients from the forecasting projection together with their asymptotic covariance matrix. We then draw 100 alternative parameter coefficients from the distribution of these estimates, which generates alternative RA and UC estimates. In Section 3.2.4, we use these bootstrapped series to account for the sampling error in the risk aversion and uncertainty estimates in our VARs.

## 2.2 Measuring Monetary Policy

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<sup>5</sup> This estimation was conducted using a winsorized sample but the estimation results for the non-winsorized sample are in fact very similar.

<sup>6</sup> The estimated uncertainty series is less “jaggedy” than it would be if only the past realized variance would be used to compute it (as in Bollerslev, Tauchen and Zhou, 2009), which in turn helps smooth the risk aversion process.

To measure the monetary policy stance, we use the real interest rate (RERA), i.e., the Fed funds end-of-the-month target rate minus the CPI annual inflation rate. In Section 3.2.1, we consider alternative measures of the monetary policy stance for robustness. Our first such measure is the Taylor rule residual, the difference between the nominal Fed funds rate and the Taylor rule rate (TR rate). The TR rate is estimated as in Taylor (1993):

$$TR_t = Inf_t + NatRate_t + 0.5 (Inf_t - TargInf) + 0.5 OG_t \quad (2)$$

where  $Inf$  is the annual inflation rate,  $NatRate$  is the “natural” real Fed funds rate (consistent with full employment), which Taylor assumed to be 2%,  $TargInf$  is a target inflation rate, also assumed to be 2%, and  $OG$  (output gap) is the percentage deviation of real GDP from potential GDP; with the latter obtained from the Congressional Budget Office. As other alternative measures of the monetary policy stance, we consider the nominal Fed funds rate instead of the real rate, and (the growth rate of) the monetary aggregate M1, which is commonly assumed to be under tight control of the central bank. We multiply M1 (growth) by minus one so that a positive shock to this variable corresponds to monetary policy tightening, in line with all other measures of monetary policy we use.

Measuring the monetary policy stance is challenging since late 2008, as the Fed funds rate reached the zero lower bound (the Fed funds target was set in the range 0-0.25% as of December 2008) and the Federal Reserve turned to unconventional monetary policies, such as large-scale asset purchases. We approximate the “true” nominal Fed funds rate in the period December 2008 - August 2010 by taking it to be the minimum between 0.125% (i.e., the mid-point of the 0-0.25% range) and the TR rate, estimated using

equation (2) above. Rudebusch (2009) has also advocated using the TR rate estimate as a proxy for the “true” Fed funds rate post-2008.

In our analysis in Sections 4.1 and 4.2, we use monetary policy surprises derived from Fed funds futures data. In Section 4.1, we rely on monetary policy surprises proposed by Gürkaynak, Sack and Swanson (2005), henceforth GSS.<sup>7</sup> GSS compute the monetary policy surprises as high-frequency changes in the futures rate around the FOMC announcements. Their “tight” (“wide”) window estimates begin ten (fifteen) minutes prior to the monetary policy announcement and end twenty (forty-five) minutes after the policy announcement, respectively. The data span the period from January 1990 through June 2008. In Section 4.2, we use the unexpected change in the Fed funds rate on a monthly basis, defined as the average Fed funds target rate in month  $t$  minus the one-month futures rate on the last day of the month  $t-1$ . This approach follows Kuttner (2001) and Bernanke and Kuttner (2005) (henceforth BK); see their equation (5). As pointed out by BK, rate changes that were unanticipated as of the end of the prior month may well include a systematic response to economic news, such as employment, output and inflation occurring during the month. To overcome this problem, we calculate “cleansed” monetary surprises that are orthogonal to a set of economic data releases. They are calculated as residuals in a regression of the “simple” monetary policy surprise, onto the unexpected component of the industrial production index, the Institute of Supply Management Purchasing Managers Index (the ISM index), the payroll survey, and unemployment (see Section 2.3 below for a description). Finally, in the regression, we allow for heterogeneous coefficients before and after 1994, to take into account a change in the reaction of the Fed to economic data releases, as documented in BK.

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<sup>7</sup> We are very grateful to R. Gürkaynak for sharing the data with us.

To extend the sample of monetary policy surprises until August 2010, we proceed in two steps. First, we collect data on monetary policy surprises at the zero lower bound from Wright (2011, Table 5). The surprises are based on a structural VAR in financial variables at the daily frequency, starting in November 2008 (and calculated beyond the end of our sample in August 2010). The shocks are positive (negative) when monetary policy is unexpectedly accommodative (restrictive). They also have a standard deviation equal to one by construction. For comparability with the GSS data, we rescale Wright's shocks by multiplying them by minus the standard deviation of the GSS's shocks, before appending them to the time series of GSS shocks. Second, to fill the gap between the data from GSS (June 2008) and Wright (November 2008), we calculate monetary policy surprises using Federal funds futures, following BK.

### **2.3 Measuring Business Cycle Variation**

We use industrial production as our benchmark indicator of business cycle variation at the monthly frequency. In a robustness exercise in Section 3.2.2, we also consider non-farm employment and the ISM index as alternative business cycle indicators.

In Sections 4.1 and 4.2, we use data on economic news surprises following the methodology in Ehrmann and Fratzscher (2004).<sup>8</sup> In our analysis, we rely on unexpected components of news about the industrial production index, the ISM index, the payroll survey, and unemployment. The unexpected component of each news release is calculated as the difference between the released data and the median expectation according to surveys. We use the Money Market Survey (MMS) for the period 1990-2001 and Bloomberg for the period 2002-2010. The shocks are standardized over the sample period.

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<sup>8</sup> We are very grateful to M. Ehrmann and M. Fratzscher for sharing their dataset with us.

### 3. Structural Monetary VARs

In this Section, we follow the identified monetary VAR literature and interpret the shock in the monetary policy equation as the monetary policy shock. Our benchmark VAR, analyzed in Section 3.1, consists of four-variables: our risk aversion and uncertainty proxies ( $ra_t$  and  $uc_t$ ), the real interest rate as a measure of monetary policy stance ( $mp_t$ ), and the log-difference of industrial production as a business cycle indicator ( $bc_t$ ). We consider alternative VARs as part of an extensive series of robustness checks discussed in Section 3.2. The business cycle is the most important control variable as it is conceivable that, for example, news indicating weaker than expected growth in the economy may simultaneously make a cut in the Fed funds target rate more likely and cause people to be effectively more risk averse, because their consumption moves closer to their “habit stock,” or because they fear a more uncertain future.

#### 3.1 Structural Four-Variable VAR

We collect the four variables of our benchmark VAR in the vector  $Z_t = [bc_t, mp_t, ra_t, uc_t]'$ . Without loss of generality, we ignore constants. Consider the following structural VAR:

$$A Z_t = \Phi Z_{t-1} + \varepsilon_t \quad (3)$$

where  $A$  is a 4x4 full-rank matrix and  $E[\varepsilon_t \varepsilon_t'] = I$ . Of main interest are the dynamic responses to the structural shocks  $\varepsilon_t$ . Of course, we start by estimating the reduced-form VAR:

$$Z_t = B Z_{t-1} + C \varepsilon_t \quad (4)$$

where  $B$  denotes  $A^{-1} \Phi$  and  $C$  denotes  $A^{-1}$ . Our estimated VARs include 3 lags. In the Online Appendix, we include a table with some key reduced-form VAR statistics,

showing that the Schwarz criterion selects a one-lag VAR, whereas the Akaike criterion selects three lags. Moreover, residual specification tests (Johansen, 1995) show that the VAR with 3 lags clearly eliminates all serial correlation in the residuals.

We need 6 restrictions on the VAR to identify the system. Our first set of restrictions uses a standard Cholesky decomposition of the estimate of the variance-covariance matrix. We order the business cycle variable first, followed by the real interest rate, with risk aversion and uncertainty ordered last. This captures the fact that risk aversion and uncertainty, stock market based variables, respond instantly to monetary policy shocks, while the business cycle variable is relatively more slow-moving. Effectively, this imposes six exclusion restrictions on the contemporaneous matrix A, making it lower-triangular.

Our second set of restrictions combines five contemporaneous restrictions (also imposed under the Cholesky decomposition above) with the assumption that monetary policy has no long-run effect on the level of industrial production. This long-run restriction is inspired by the literature on long-run money neutrality: money should not have a long run effect on real variables.<sup>9</sup> Following Blanchard and Quah (1989), the model with a long-run restriction (LR) involves a long-run response matrix, denoted by D:

$$D \equiv (I - B)^{-1} C. \tag{5}$$

The system with five contemporaneous restrictions and one long-run exclusion restriction corresponds to the following contemporaneous matrix A and long-run matrix D:<sup>10</sup>

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<sup>9</sup> Bernanke and Mihov (1998b) and King and Watson (1992) marshal empirical evidence in favor of money neutrality using data on money growth and output growth.

<sup>10</sup> Both identification schemes satisfy necessary and sufficient conditions for global identification of structural vector autoregressive systems (see Rubio-Ramírez, Waggoner and Zha (2010)).

$$A = \begin{bmatrix} a_{11} & a_{12} & 0 & 0 \\ a_{21} & a_{22} & 0 & 0 \\ a_{31} & a_{32} & a_{33} & 0 \\ a_{41} & a_{42} & a_{43} & a_{44} \end{bmatrix} \text{ and } D = \begin{bmatrix} d_{11} & 0 & d_{13} & d_{14} \\ d_{21} & d_{22} & d_{23} & d_{24} \\ d_{31} & d_{32} & d_{33} & d_{34} \\ d_{41} & d_{42} & d_{43} & d_{44} \end{bmatrix} \quad (6)$$

We couch our main results in the form of impulse-response functions (IRFs henceforth), estimated in the usual way, and focus our discussion on significant responses. We compute 90% bootstrapped confidence intervals based on 1000 replications. Figure 3 graphs the complete results for the pre-crisis sample but in our discussion we mention the corresponding full sample (till August 2010) results in parentheses. A complete graph for the full sample, mimicking Figure 3, is reproduced in the Online Appendix (Figure OA1).

Panels A and B show the interactions between the real rate (RERA) and risk aversion (RA). A one standard deviation negative shock to the real rate, a 34 (42) basis points decrease under both identification schemes, lowers risk aversion by 0.032 (0.019) in the model with contemporaneous restrictions and by 0.035 (0.019) in the model with contemporaneous/long-run restrictions after 9 (19) months. The impact reaches a maximum of 0.056 (0.020) after 20 (23) months and remains significant up and till lag 40 (40) in both models. So, laxer monetary policy lowers risk aversion under both identification schemes and in both the pre-crisis and full samples. The impact in the full sample is quantitatively weaker, and is only statistically significant at the 68% confidence level. However, such tighter confidence bounds are common in the VAR literature (see Christiano, Eichenbaum, and Evans (1996), Sims and Zha (1999)). The impact of a one standard deviation positive shock to risk aversion, equivalent to 0.347 (0.363) on the real rate is mostly negative but not statistically significant in both models,



As Panel C shows, a positive shock to the real rate increases uncertainty (UC) in the medium-run (after a short-lived negative impact), between lags 11 and 38 in the model with contemporaneous restrictions and between lags 11 - 40 in the model with contemporaneous/long-run restrictions. The maximum positive impact is 0.060 and 0.063 at lag 21 in the models with contemporaneous and contemporaneous/long-run restrictions, respectively (in the full sample, the max impact is 0.018 and it is borderline statistically insignificant even at the 68% confidence level). In the other direction, reported in Panel D, the real rate decreases in the short-run following a positive one standard deviation shock to uncertainty, equivalent to 0.244 (0.274). In both models, the impact is (borderline) statistically insignificant in the pre-crisis sample (in the full sample, the impact is significant at the 90% confidence level between lags 7 and 47, reaching a maximum of 19 basis points at lag 18).

As for interactions with the business cycle variable (Panels E through J), a contractionary monetary policy shock leads to a decline in industrial production growth (DIPI) in the medium-run, but the impact is statistically insignificant in all specifications. In the other direction, monetary policy reacts as expected to business cycle fluctuations: a one standard deviation positive shock to industrial production growth, equivalent to 0.005 (0.006), leads to a higher real rate. Specifically, in the model with contemporaneous restrictions, the real rate increases by a maximum of 14 (15) basis points after 6 (11) months, with the impact being significant between lags 1 and 20 (at lag 1, and between lags 3-31). The impact is also positive in the model with contemporaneous/long-run restrictions but it is not statistically significant. Interactions between risk aversion and industrial production growth are mostly statistically insignificant. Positive uncertainty

shocks lower industrial production growth between lags 6-15 (2-18), while the impact in the opposite direction is statistically insignificant. This is consistent with the analysis in Bloom (2009), who found that uncertainty shocks generate significant business cycle effects, using the VIX as a measure of uncertainty.<sup>11</sup>

Finally, increases in risk aversion predict future increases in uncertainty under both identification schemes (Panel L). Uncertainty has a positive, albeit short-lived effect on risk aversion (Panel K).

Our main result for the pre-crisis sample is that monetary policy has a medium-run statistically significant effect on risk aversion. This effect is also economically significant. In Figure 4, we show what fraction of the structural variance of the four variables in the VAR is due to monetary policy shocks. They account for over 20% of the variance of risk aversion at horizons longer than 37 and 29 months in the models with contemporaneous and contemporaneous/long-run restrictions, respectively. Monetary policy shocks also increase uncertainty and Figure 4 shows that they are only marginally less important drivers of the uncertainty variance than they are of the risk aversion variance. Finally, while monetary policy appears to relax policy in response to both risk aversion and uncertainty shocks, these effects are statistically weaker.

The results for the full sample including the crisis period overall confirm our results for the pre-crisis sample but are less statistically significant. Given the measurement problems mentioned before, and the rather extreme volatility the VIX experienced, this is not entirely surprising.

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<sup>11</sup> Popescu and Smets (2009) analyze the business cycle behavior of measures of perceived uncertainty and financial risk premia in Germany. They find that financial risk aversion shocks are more important in driving business cycles than uncertainty shocks. Gilchrist and Zakrajšek (2011) document that innovations to the excess corporate bond premium, a proxy for the time-varying price of default risk, cause large and persistent contractions in economic activity.

## **3.2 Robustness**

In this subsection, we consider five types of robustness checks: 1) measurement of the monetary policy stance; 2) measurement of the business cycle variable; 3) alternative orderings of variables; 4) accounting for the sampling error in RA and UC estimates; and 5) conducting the analysis using a six variable monetary VAR with the Fed funds rate and price level measures CPI and PPI entering as separate variables. We also verified that our results remain robust to the use of both shorter and longer VAR lag-lengths. We estimated a VAR with 1 lag, as selected by the Schwarz criterion, as well as a VAR with 4 lags (we did not go beyond four lags as otherwise the saturation ratio, the ratio of data points to parameters, drops below 10). Our results were unaltered.

### **3.2.1 Measuring Monetary Policy**

Table 2 reports summary statistics on the interaction of alternative measures of the monetary policy stance with risk aversion (Panel A) and with uncertainty (Panel B). The results confirm that a looser monetary policy stance lowers risk aversion in the short to medium run. This effect is persistent, lasting for about two years. In some cases, the immediate effect has the reverse sign however. In the other direction, monetary policy becomes laxer in response to positive risk aversion shocks but the effect is statistically significant in less than half the cases. As for the effect of monetary policy on uncertainty, monetary tightening increases uncertainty in the medium run but this effect is not significant when using the Fed fund rate. In the other direction, higher uncertainty leads to laxer monetary policy in all specifications but the effect is only significant when using the Fed fund rate under contemporaneous identifying restrictions.

### **3.2.2 Measuring Business Cycle Variation**

We consider the log-difference of employment and the log of the ISM index as alternative business cycle indicators. Unlike industrial production and employment, the ISM index is a stationary variable, implying that VAR shocks do not have a long run effect on it. Our long-run restriction on the effect of monetary policy is thus stronger when applied to the ISM: it restricts the total effect of monetary policy on the ISM to be zero. Nevertheless, our main results from Section 3.1 are confirmed for each specification with an alternative business cycle variable. We present a full set of IRFs (the equivalent of Figure 3) for the VARs with the log-difference of employment and the log of the ISM index as business cycle measures in the Online Appendix (Figures OA4 and OA5, respectively).

### **3.2.3 Alternative Orderings of Variables**

In one alternative ordering, we reverse the order of risk aversion and uncertainty in our benchmark VAR. In another robustness check, we order the real interest rate last, thus allowing it to respond instantaneously to RA and UC shocks. We consistently find that looser monetary policy lowers risk aversion and uncertainty in a statistically significant fashion in the medium-run. In the other direction, the effects are less robust. In the specification with RA and UC reversed, monetary policy mostly responds to UC shocks, but the response to RA shocks is statistically insignificant. In the specification with RERA ordered last, monetary policy responds to both positive RA and UC shocks by loosening its stance, and the effect is statistically significantly different from zero. We present a full set of IRFs for the reversed ordering of RA and UC and for the specification with RERA ordered last in the Online Appendix (Figures OA6 and OA7, respectively).

### **3.2.4 Sampling Error in RA and UC**

We check that our VAR results are robust to accounting for the sampling error in the RA and UC estimation. We draw 100 alternative RA and UC series from the distribution of RA and UC estimates (as described in section 2.1), and feed those into our bootstrapped VAR. We estimate 100 VAR replications per set of alternative RA and UC series. We then construct the usual 90% confidence bounds. The results are very similar to those obtained without taking uncertainty surrounding RA and UC estimates into account, and are presented in the Online Appendix (Figure OA8).

### **3.2.5 Six-variable Monetary VAR**

We also estimate a six-variable monetary VAR following Christiano, Eichenbaum and Evans (1999) and featuring the nominal Fed funds rate as the measure of monetary policy stance and price level measures CPI and PPI as additional variables.<sup>12</sup> To identify monetary policy shocks, we use a Cholesky ordering with CPI and industrial production ordered first, followed by the Fed funds rate and PPI, and risk aversion and uncertainty ordered last.

We present impulse-responses to monetary policy shocks in Figure 5. Again, we discuss results for the pre-crisis sample, but summarize the full sample results in parentheses. A positive monetary policy shock corresponds to a 15 basis points (30 in the full sample) increase in the Fed funds rate. A contractionary monetary shock leads to a statistically significant decrease in the CPI between lags 3 and 23 (2 and 8) and in the PPI between lags 23 and 50 (effect insignificant in the full sample). Furthermore, in the pre-crisis sample, industrial production declines following a monetary contraction after about

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<sup>12</sup> We estimate the model with four lags, as suggested by the Akaike criterion. All variables are in logarithms except for the Fed funds rate. Note that industrial production now enters the VAR in levels.

10 months, though the effect is not statistically significant (similarly, the effect is insignificant in the full sample). Importantly, the reactions of both risk aversion and uncertainty are remarkably similar to those uncovered in our benchmark four-variable VARs. Looser monetary policy decreases risk aversion by 0.024 (0.023) after 12 (19) months. The effect reaches a maximum of 0.040 (0.025) at lag 23 (24), and remains statistically significant till lag 35 (till lag 37, significant under 68% confidence bounds). The effects remain economically important as monetary policy shocks account for over 12% (3%) of the variance of risk aversion at horizons longer than 40 months (see Panel F of Figure 5) but these percentages are nonetheless lower than in our four-variable VAR. As for uncertainty, a higher Fed funds rate increases uncertainty between lags 12 and 31 (16 and 36), with the maximum impact of 0.040 (0.033) at lag 23 (22), which is also consistent with our previous findings. In non-reported results, monetary policy responds to both positive RA and UC shocks by loosening its stance. The effect is statistically significant under 90% confidence bounds between lags 2 and 7 (6 and 15) for RA and between lags 5 and 26 (3 and 20) for UC.

#### **4. Alternative Identification of Monetary Policy Shocks**

In this Section, we employ two alternative methodologies to identify monetary policy shocks: 1) monetary surprises based on high-frequency Fed funds futures and 2) monthly surprises calculated using daily Fed funds futures.

##### **4.1 Identification using High-Frequency Fed Funds Futures**

Our VAR set-up to identify monetary policy shocks and their structural relationship with risk aversion and uncertainty follows the Sims (1980, 1998) identification tradition. With financial market values changing continuously during the month, the use of

monthly data for this purpose certainly may cast some doubt on this identification scheme. We therefore use an alternative identification methodology that makes use of high frequency data to infer restrictions on the monthly VAR. The approach, inspired by and building on the procedure described in D'Amico and Farka (2011), consists of three steps.

In the first step, we measure the structural monetary policy and business cycle shocks directly. For monetary policy, we rely on a well-established literature that uses high frequency changes in Fed funds futures rates (see, for example, Faust, Swanson and Wright, 2004) to measure monetary policy shocks, and we detailed their measurement in Section 2. Likewise, for business cycle shocks, we use news announcements. Under certain assumptions, these shocks can be viewed as measuring the structural shocks  $\varepsilon_t$  in the VAR. For monetary policy shocks, this is plausible because usually only one shock occurs per month, and the use of high frequency futures data helps ensure that the identified shock is plausibly orthogonal to other shocks. As to the business cycle shocks, there are a number of potentially important complicating issues, such as the correlation between the different news announcements and the structural shock to the actual business cycle variable used in the VAR, and the scale of the shocks when more than one occurs within a particular month. However, these issues become moot when business cycle shocks do not generate significant contemporaneous effects on our financial variables, which ends up being the case.

In the second step, we measure the high frequency effects of monetary policy and economic news surprises on risk aversion and uncertainty. We regress daily changes in risk aversion and uncertainty (as proxies for unexpected changes to these variables),

respectively, on the monetary policy surprises based on high-frequency futures (using the “tight” window shocks)<sup>13</sup> and the four monthly economic news surprises concerning industrial production ( $\Delta IP$ ), the ISM index ( $\Delta ISM$ ), non-farm payroll and employment ( $\Delta EMP$ ), as described in Section 2.3.<sup>14</sup> The resulting coefficients for the pre-crisis sample (with heteroskedasticity-robust standard errors in parentheses) are as follows:

$$\Delta RA_t = -0.039 + 0.047 \Delta MP_t - 0.005 \Delta IP_t - 0.004 \Delta ISM_t - 0.004 \Delta EMP_t \quad (7)$$

(0.007) (0.020) (0.014) (0.016) (0.017)

$$\Delta UC_t = -0.009 + 0.013 \Delta MP_t + 0.002 \Delta IP_t - 0.002 \Delta ISM_t - 0.008 \Delta EMP_t \quad (8)$$

(0.003) (0.010) (0.005) (0.005) (0.011)

The coefficients on the business cycle news surprises are not statistically different from zero and economically small. However, the responses to the monetary policy surprises are quantitatively larger and statistically significant at the 5% level for RA and at the 16% level for UC. The coefficients on  $\Delta MP$  give us direct evidence on the contemporaneous responses of RA and UC to *structural* disturbances in MP. We already note that these responses confirm that risk aversion reacts positively to monetary policy shocks and does so more strongly than uncertainty. By the same token, we conclude that the contemporaneous responses of RA and UC to a business cycle shock in our VARs are equal to zero.

In the third step, we use the estimates of structural responses of RA and UC to monetary policy and business cycle shocks in our VAR analysis. This requires a number of additional assumptions. In particular, we assume that there are no further policy or business cycle shocks during the month and thus that the monthly shock equals the daily

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<sup>13</sup> Results for the monetary policy surprises calculated using the “wide” window are very similar.

<sup>14</sup> We treat both the non-farm payroll and the negative of the unemployment surprises as news about employment ( $\Delta EMP$ ) as they have similar information content. Whenever they come out on the same day (which is mostly the case), we sum them up.



shock identified from high frequency data. Furthermore, we assume that the contemporaneous daily change in risk aversion and uncertainty identifies the monthly change in unexpected risk aversion and uncertainty due to these policy and business cycle shocks. In other words, we assume that the high-frequency regressions effectively yield four coefficients in the  $A^{-1}$  matrix of our structural VAR. Because we need 6 restrictions in total, we impose two more restrictions from a Cholesky ordering to achieve identification. In one identification scheme (Model 1), we impose that both industrial production and monetary policy do not instantaneously respond to RA; in another scheme, we impose the same restrictions on the reaction to UC (Model 2).<sup>15</sup> Because the identifying assumptions on monetary policy shocks have more support in the extant literature than the assumptions we made regarding the business cycle shocks, we also consider a robustness check where we only impose the high-frequency responses to monetary policy surprises in the monthly VAR. We then need four additional restrictions from a Cholesky ordering to complete identification and use the three contemporaneous restrictions in the BC equation (the usual assumption on sluggish adjustment of macro to financial data) and a zero response by monetary policy to either RA (Model 3) or UC (Model 4).

For the full sample, all the estimated coefficients in the second step regressions are not statistically different from zero, but the effect of monetary policy shocks on risk aversion is again positive with a t-stat of close to 1. If we were to impose that the contemporaneous responses of RA and UC to monetary policy and business cycle shocks are all equal to zero, models 1 and 2 would be under-identified. We thus estimate only

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<sup>15</sup> Imposing zero-response restrictions to RA and UC in the BC equation would lead to an under-identified model.

models 3 and 4 for the full sample, i.e., imposing the zero-response to monetary policy surprises from the second step regression, plus three contemporaneous restrictions in the BC equation and a zero response by monetary policy to either RA or UC. As before, we report results for the full sample in parentheses (and present IRFs in the Online Appendix, Figure OA2).

For the two models imposing four restrictions from the first step, we present impulse-responses to monetary policy shocks in Figure 6. Looser monetary policy (corresponding to a 29 basis points decrease in the real rate) lowers risk aversion on impact and between lags 8 and 12, with a maximum impact of 0.055 in the model with no contemporaneous response of business cycle and monetary policy to RA. The maximum impact is 0.061 and the effect is significant between lags 7 and 17 in the model with no contemporaneous response of business cycle and monetary policy to UC.

As Panel B shows, a positive shock to the real rate increases uncertainty on impact in the model with no contemporaneous response of the business cycle and monetary policy to RA. The effect is positive but not statistically significant in the medium run. In the model with no contemporaneous response of business cycle and monetary policy to UC, the positive effect of the real rate shock on uncertainty is statistically significant on impact and between lags 10-14, with a maximum impact of 0.059 at lag 14.

Lastly, the impact of monetary policy on industrial production growth is not statistically significant (Panel C). Note that with different measures for the business cycle, such as employment, the VAR does produce the expected and statistically significant response to monetary policy.

For the two models imposing two restrictions (for the monetary policy shocks only) from the first step, we present impulse-responses to monetary policy shocks in Figure 7. Looser monetary policy, corresponding to a 33 (42) basis points decrease in the real rate, lowers risk aversion on impact and between lags 4-36 (14-37, significant at 68% confidence bounds), with a maximum impact of 0.055 at lag 15 (0.023 at lag 17) both in the model with no contemporaneous response of monetary policy to RA and in the model with no contemporaneous response of monetary policy to UC (and the three zero restrictions in the BC equation).

As Panel B shows, a positive shock to the real rate increases uncertainty on impact and between lags 4-36, with a maximum impact of 0.058 at lag 16 both in the model with no contemporaneous response of monetary policy to RA and in the model with no contemporaneous response of monetary policy to UC (and the three zero restrictions in the BC equation). (The impact of the monetary policy shock on uncertainty is positive but not statistically significant at 68% confidence bounds for the full sample.)

Lastly, the impact of monetary policy on industrial production growth is again not statistically significant (Panel C).

#### **4.2 Identification using Daily Fed Funds Futures**

In this section, we adopt the approach of Bernanke and Kuttner (2005) to study the dynamic response of risk aversion and uncertainty to monetary policy. The key feature of their approach is the calculation of a monthly monetary policy surprise using Federal funds futures contracts. This variable identifies the monetary policy shock and is included in the VAR as an exogenous variable. The endogenous variables in the VAR are RA, UC and the log difference of industrial production (DIPI).

We present impulse-responses to “cleansed” monetary policy shocks<sup>16</sup> in Figure 7 for the pre-crisis sample and in the Online Appendix for the full sample (Figure OA3). As before, below we discuss results for the full sample in parentheses. The results generally confirm that monetary policy surprises have a positive impact on both RA and UC, and have the expected negative effect on industrial production. However, the results are less strong statistically than under our other identification schemes.

A one standard deviation negative shock to the “cleansed” surprise, equivalent to 8.6 basis points (9 basis points), decreases RA on impact by 0.061 and UC by 0.054 (decreases RA by 0.053 and UC by 0.026). The IRFs are significant on impact at the 80% confidence level for RA and at the 70% level for UC (at the 80% level for RA; not statistically significant for UC). These results are robust to the use of alternative business cycle indicators (non-farm employment and the ISM index).

## **5. Conclusions**

A number of recent studies point at a potential link between loose monetary policy and excessive risk-taking in financial markets. Rajan (2006) conjectures that in times of ample liquidity supplied by the central bank, investment managers have a tendency to engage in risky, correlated investments. To earn excess returns in a low interest rate environment, their investment strategies may entail risky, tail-risk sensitive and illiquid securities (“search for yield”). Moreover, a tendency for herding behavior emerges due to the particular structure of managerial compensation contracts. Managers are evaluated vis-à-vis their peers and by pursuing strategies similar to others, they can ensure that they do not under perform. This “behavioral” channel of monetary policy transmission can

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<sup>16</sup> The monetary policy surprise is standardized by subtracting the mean and dividing by the standard deviation.

lead to the formation of asset prices bubbles and can threaten financial stability. Yet, there is no empirical evidence on the links between risk aversion in financial markets and monetary policy.

This article has attempted to provide a first characterization of the dynamic links between risk, uncertainty and monetary policy, using a simple vector-autoregressive framework. We decompose implied volatility into two components, risk aversion and uncertainty, and study the interactions between each of the components and monetary policy under a variety of identification schemes for monetary policy shocks. We consistently find that lax monetary policy increases risk appetite (decreases risk aversion) in the future, with the effect lasting for more than two years and starting to be significant after nine months. The effect on uncertainty is similar but the immediate response of uncertainty to monetary policy shocks in high frequency regressions is weaker than that of risk aversion. Conversely, high uncertainty and high risk aversion lead to laxer monetary policy in the near-term future but these effects are not always statistically significant. These results are robust to controlling for business cycle movements. Consequently, our VAR analysis provides a clean interpretation of the stylized facts regarding the dynamic relations between the VIX and the monetary policy stance depicted in Figure 1. The primary component driving the co-movement between past monetary policy stance and current VIX levels (first column of Figure 1) is risk aversion but uncertainty also reacts to monetary policy. Both components of the VIX lie behind the negative relation in the opposite direction (second column of Figure 1).

We hope that our analysis will inspire further empirical work and research on the exact theoretical links between monetary policy and risk-taking behavior in asset

markets. A recent literature, mostly focusing on the origins of the financial crisis, has considered a few channels that deserve further scrutiny. Adrian and Shin (2008) stress the balance sheets of financial intermediaries and repo growth; Adalid and Detken (2007) and Alessi and Detken (2008) stress the buildup of liquidity through money growth and Borio and Lowe (2002) emphasize rapid credit expansion.<sup>17</sup> Recent work in the consumption-based asset pricing literature attempts to understand the structural sources of the VIX dynamics (see Bekaert and Engstrom (2010), Bollerslev, Tauchen and Zhou (2009), Drechsler and Yaron (2011)). Yet, none of these models incorporates monetary policy equations. In macroeconomics, a number of articles have embedded term structure dynamics into the standard New-Keynesian workhorse model (Bekaert, Cho, Moreno (2010), Rudebusch and Wu (2008)), but no models accommodate the dynamic interactions between monetary policy, risk aversion and uncertainty, uncovered in this article.

The policy implications of our work are potentially very important. Because monetary policy significantly affects risk aversion and uncertainty and these financial variables may affect the business cycle, we seem to have uncovered a monetary policy transmission mechanism missing in extant macroeconomic models. Fed chairman Bernanke (see Bernanke (2002)) interprets his work on the effect of monetary policy on the stock market (Bernanke and Kuttner (2005)) as suggesting that monetary policy would not have a sufficiently strong effect on asset markets to pop a “bubble” (see also Bernanke and Gertler (2001), Gilchrist and Leahy (2002), and Greenspan (2002)).

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<sup>17</sup> In fact, we considered the effects of repo, money and credit growth on our results by including them in a four-variable VAR together with RA, UC, and RERA (replacing the BC variable). We consistently found that the direct effect of monetary policy on risk aversion and uncertainty we uncovered in our benchmark VARs is preserved.

However, if monetary policy significantly affects risk appetite in asset markets, this conclusion may not hold. If one channel is that lax monetary policy induces excess leverage as in Adrian and Shin (2008), perhaps monetary policy is potent enough to weed out financial excess. Conversely, in times of crisis and heightened risk aversion, monetary policy can influence risk aversion and uncertainty in the market place, and therefore affect real outcomes.

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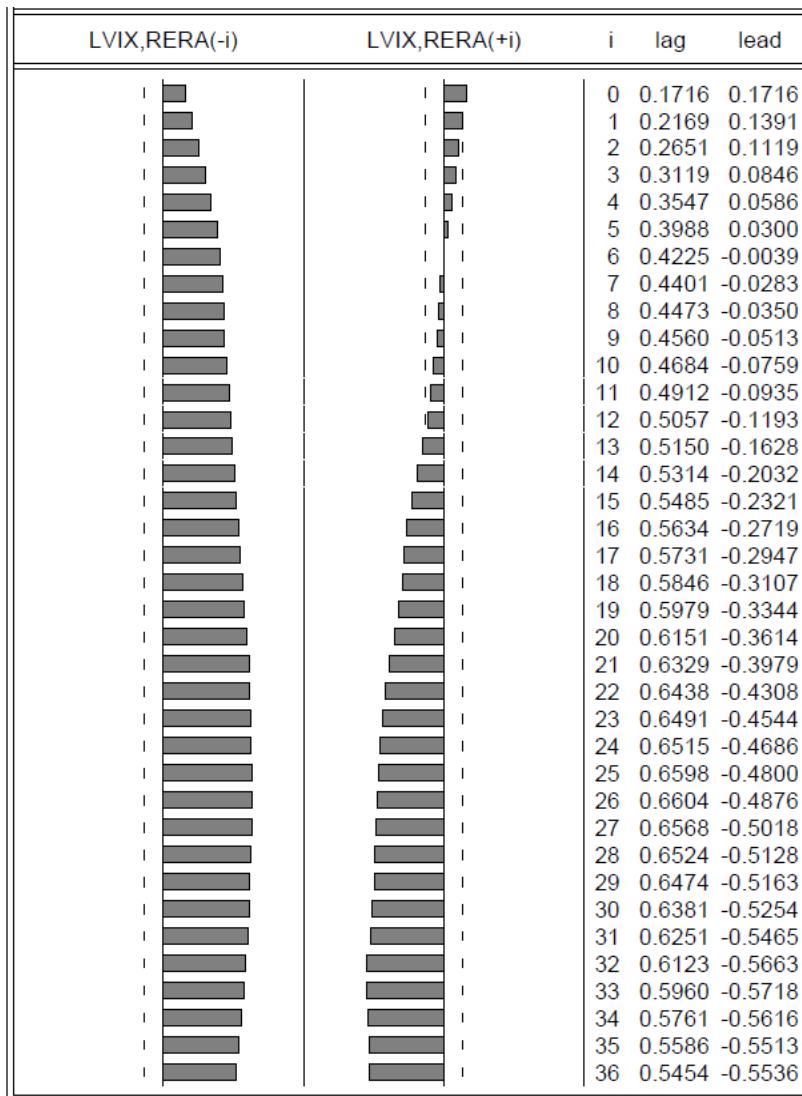
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**Figure 1: Cross-correlogram LVIX RERA**



Notes: The first column presents the (lagged) cross-correlogram between the log of the VIX (LVIX) and past values of the real interest rate (RERA). The second column presents the (lead) cross-correlogram between LVIX and future values of RERA. Dashed vertical lines indicate 95% confidence intervals for the cross-correlation. The third column presents the cross-correlation values. The index i indicates the number of months either lagged or led for the real interest rate variable.

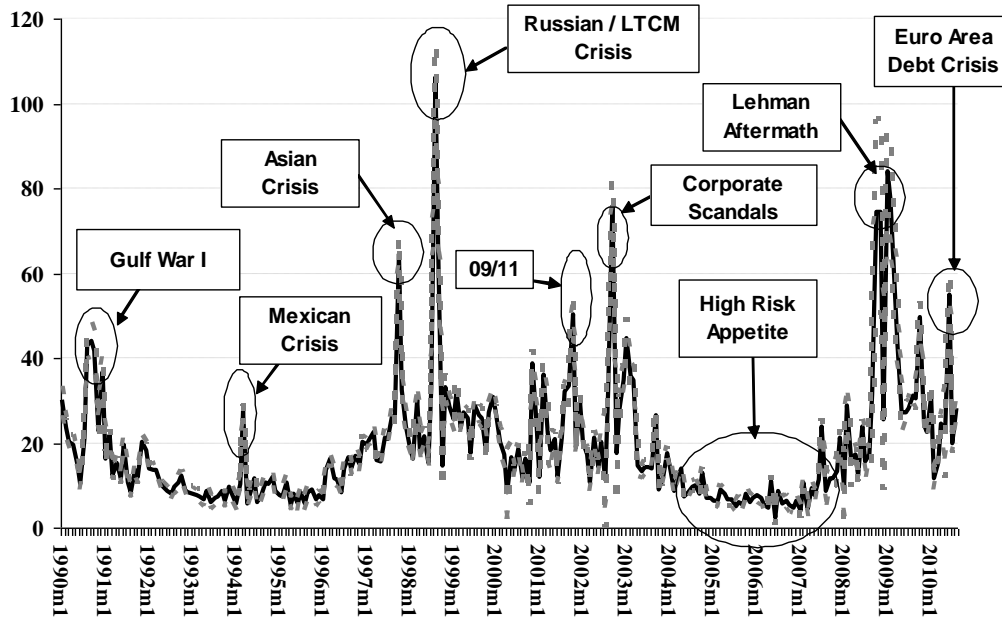
**Table 1: Description of variables**

Name	Label	Description (source)
Consumer price index	CPI	Consumer price index, all items
Dividend yield		Dividend yield of the Standard & Poor 500 index
Fed funds rate	FED	Fed funds target rate
Implied volatility	LVIX	Implied volatility of options on the Standard & Poor 500 index, $\text{Log}(\text{VIX} / \sqrt{12})$
(Growth of) Industrial production	(D)IPI	Log (difference of) total industrial production index
ISM index	ISM	ISM Purchasing Managers index
M1 money aggregate growth	M1	Month-on-month growth of M1
(Growth of) Non-farm employment	(D)EMP	Log (difference of) non-farm employment
Producer price index	PPI	Producer price index for intermediate materials
Real interest rate	RERA	FED minus annual CPI inflation rate
Realized variance	RVAR	Realized variance [see Section 2.1]
Risk aversion	RA	Log (risk aversion) [see Section 2.1]
Taylor Rule deviations	TRULE	FED minus Taylor rule rate [see Section 2.2]
Three-month T-bill		Secondary market yield
Uncertainty (conditional variance)	UC	Log (uncertainty) [see Section 2.1]

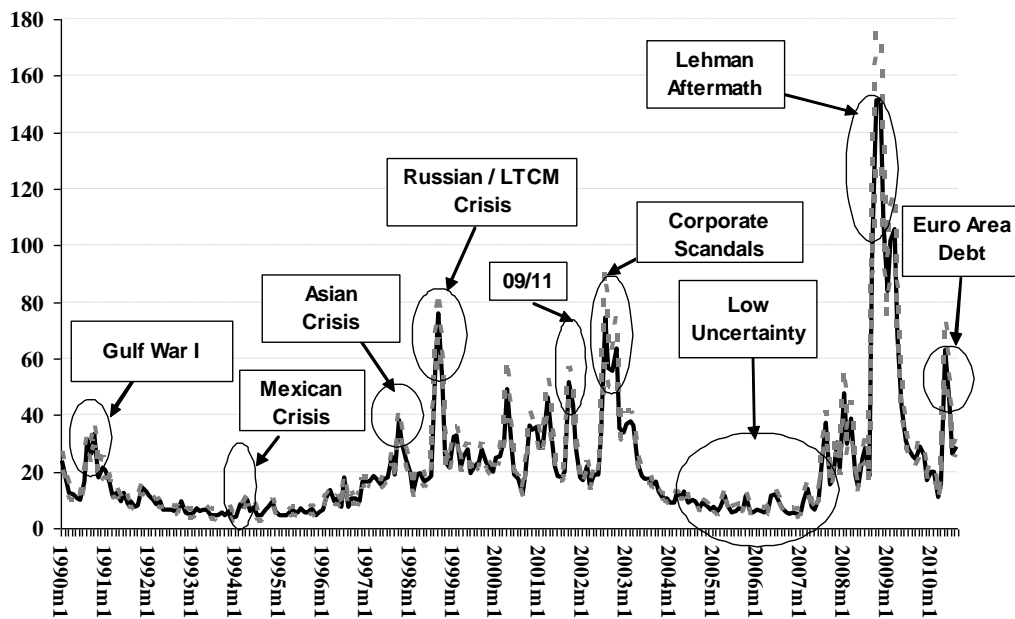
Notes: Monthly frequency, end-of-the-month data (seasonally adjusted where applicable). Unless otherwise mentioned, the data are from Thomson Datastream.

Figure 2: Risk aversion and uncertainty

Panel A: Risk aversion

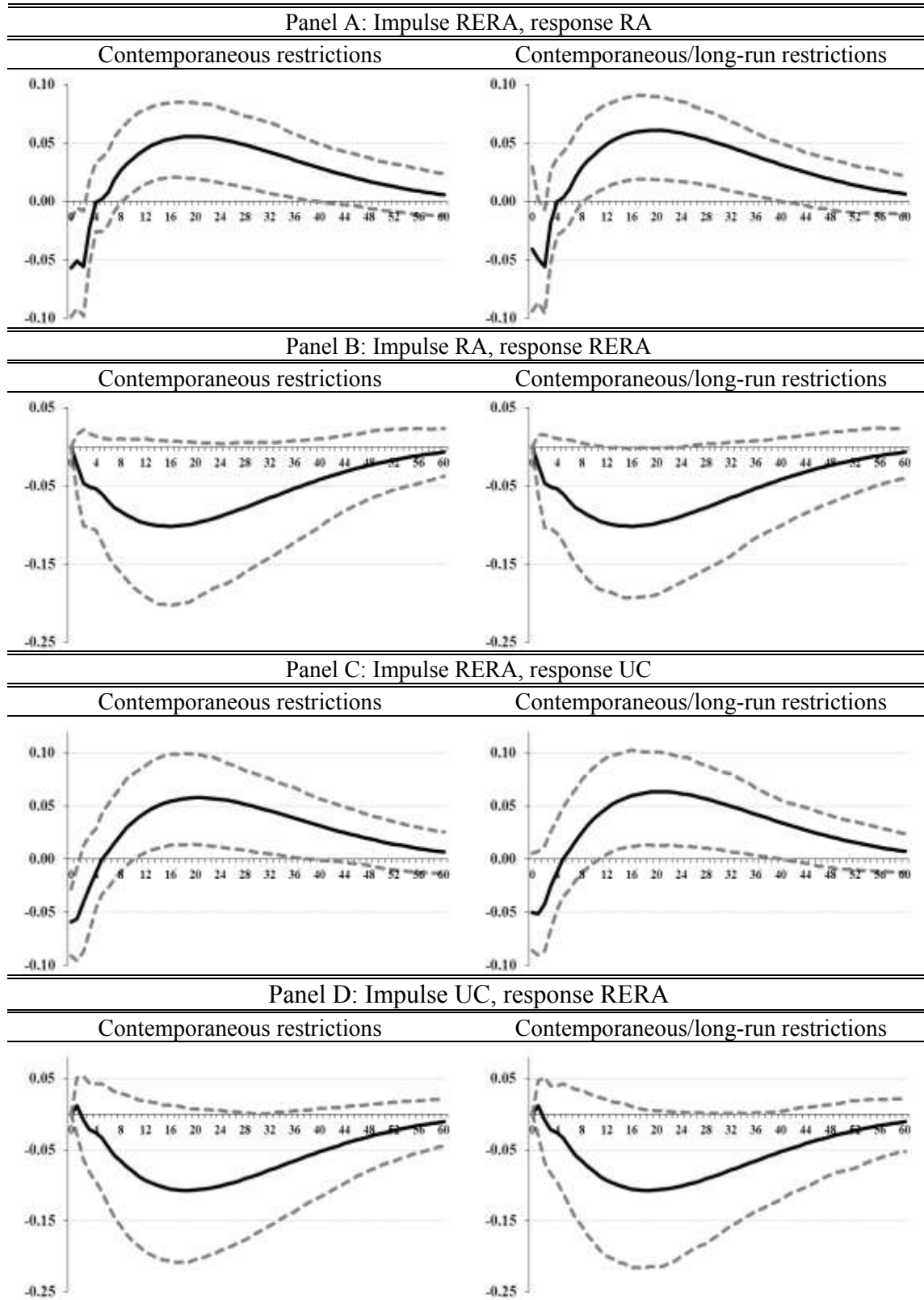


Panel B: Uncertainty

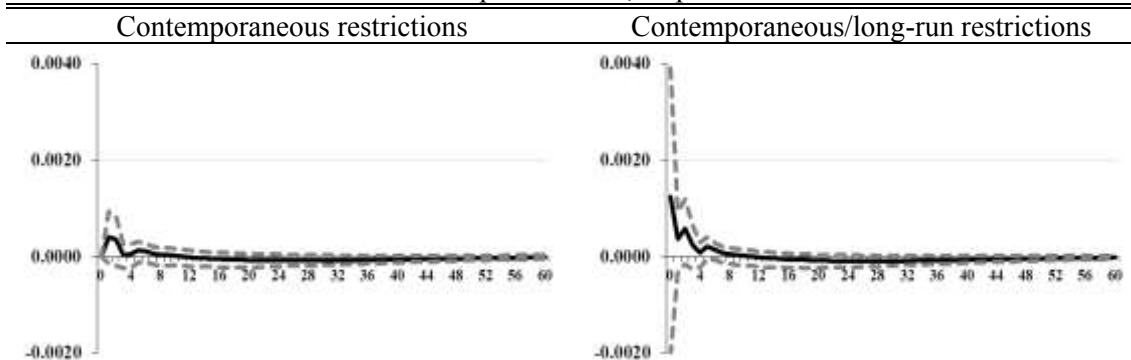


Notes: Plots of risk aversion and uncertainty for our sample period (January 1990 – August 2010).

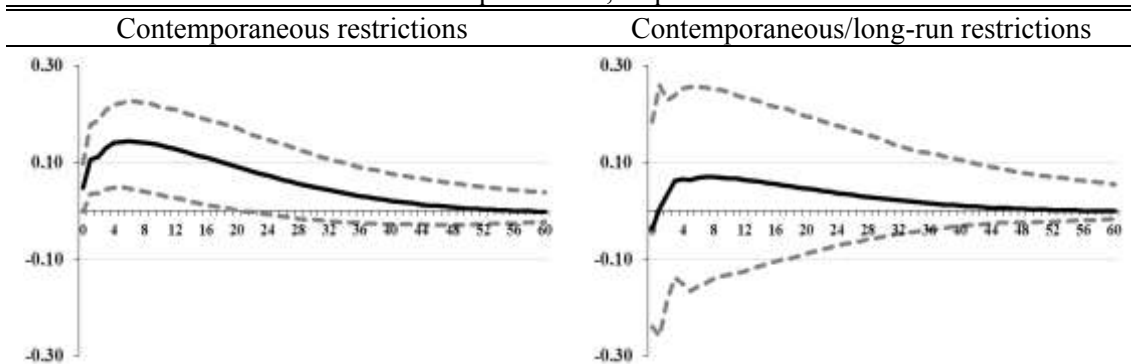
**Figure 3: Structural-form IRFs for the 4-variable VAR (DIPI, RERA, RA, UC)**



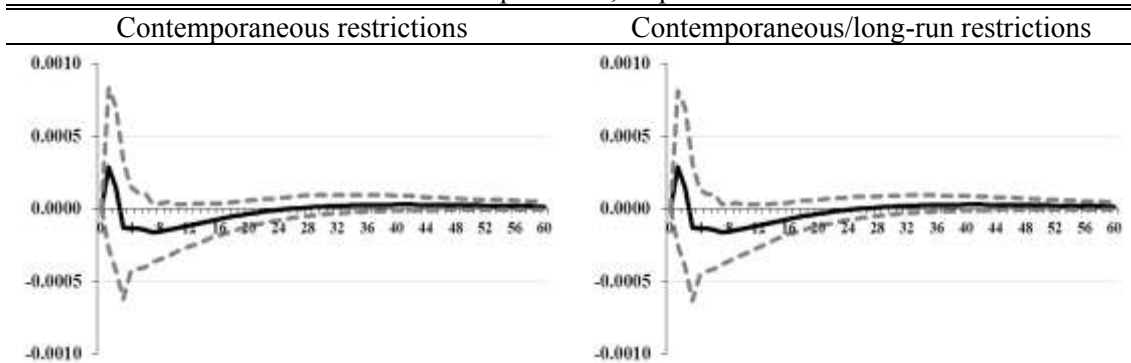
Panel E: Impulse RERA, response DIPI



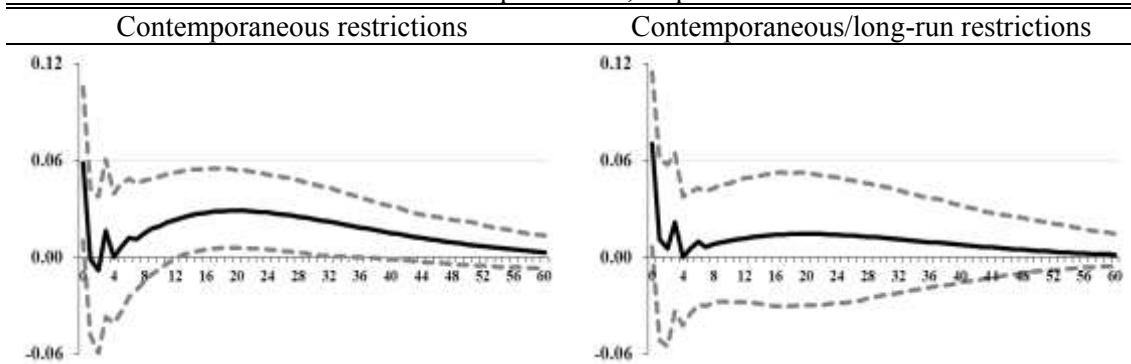
Panel F: Impulse DIPI, response RERA



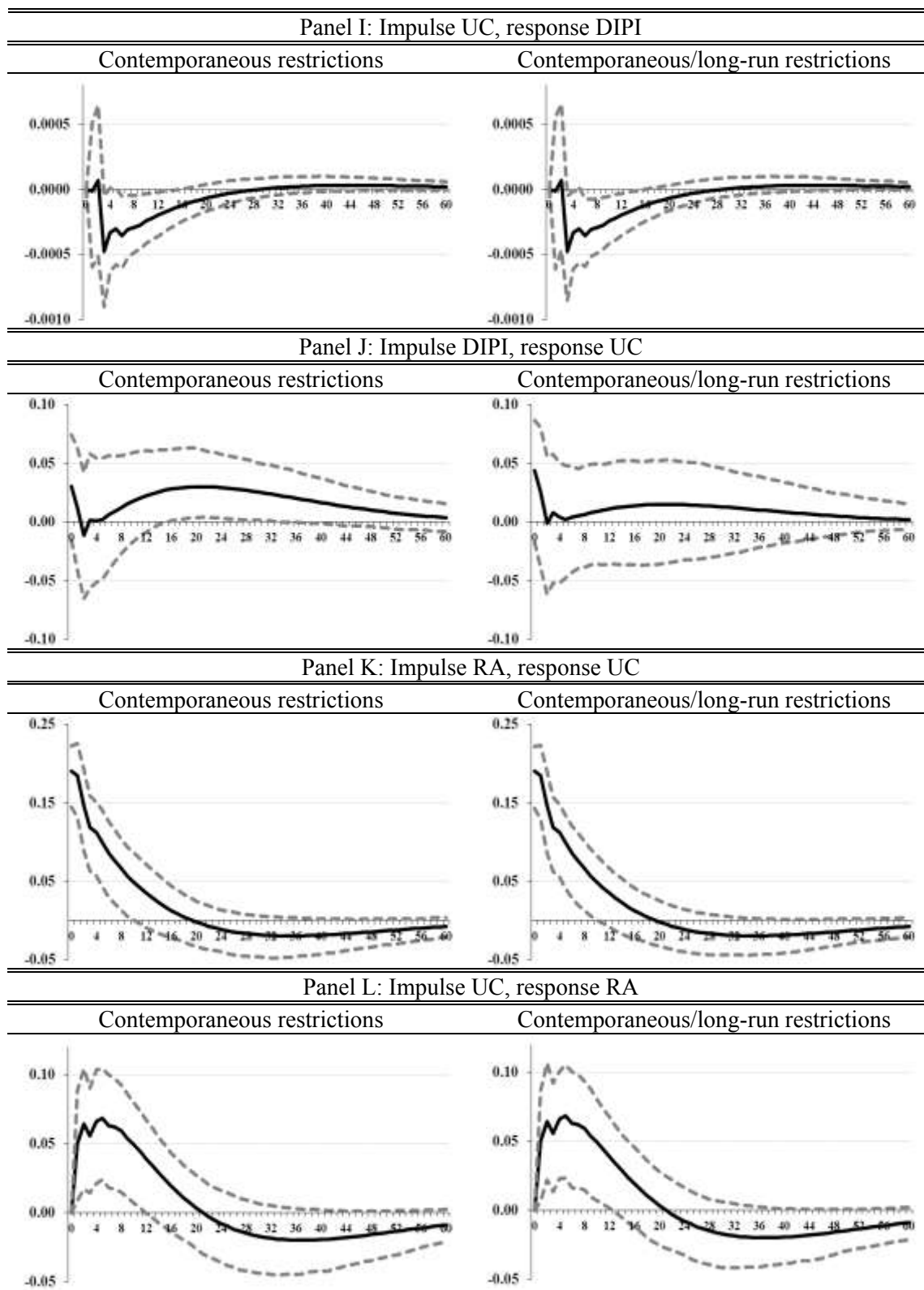
Panel G: Impulse RA, response DIPI



Panel H: Impulse DIPI, response RA

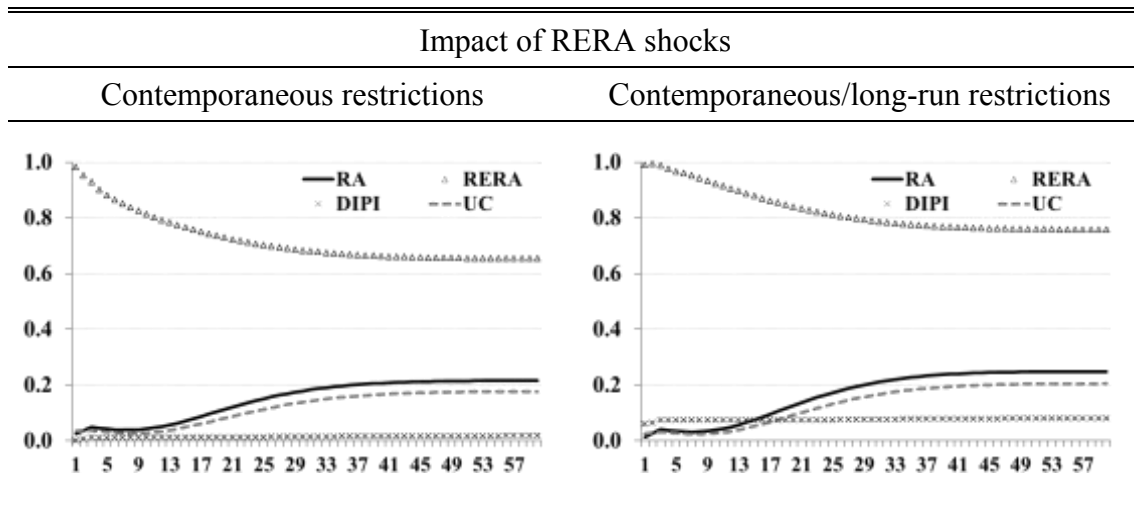






Notes: Estimated structural impulse-response functions (black lines) and 90% bootstrapped confidence intervals (grey dashed lines) for the model with 3 lags (selected by Akaike), based on 1000 replications. Panels on the left present results of the model with contemporaneous (Cholesky) restrictions, panels on the right present results of the model with contemporaneous/long-run restrictions.

**Figure 4: Structural variance decompositions**



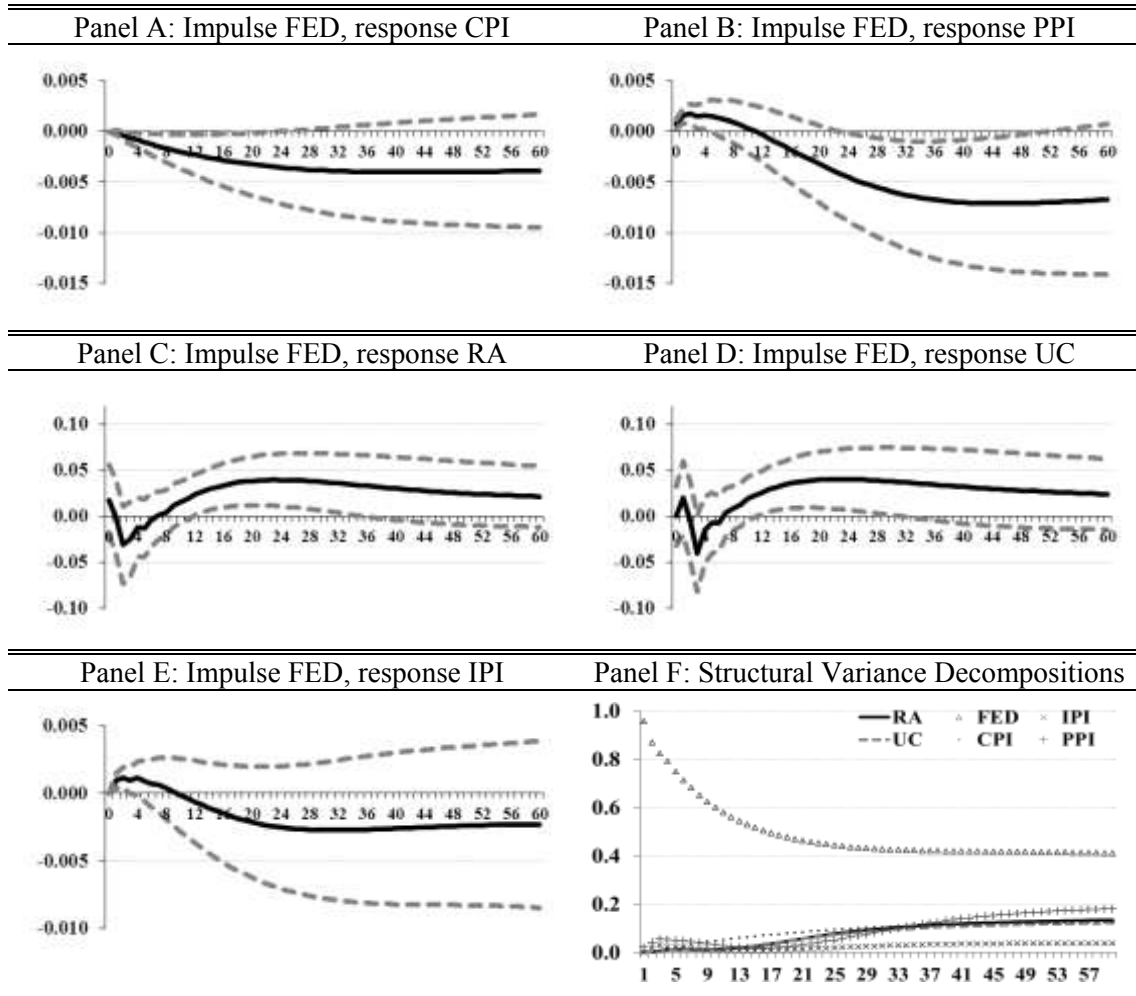
Notes: Fractions of the structural variance due to RERA shocks for the four variables DIPI, RERA, RA and UC (model with 3 lags, selected by Akaike). The panel on the left presents results of the model with contemporaneous restrictions, the panel on the right presents results of the model with contemporaneous/long-run restrictions.

**Table 2: Robustness to monetary policy measures**

Panel A: Monetary policy instrument – risk aversion pair				
MP instrument	Impulse MP, response RA		Impulse RA, response MP	
	sign	significant from-to (month)	sign	significant from-to (month)
Real interest rate				
- COR	-/+	0 - 2 (-), 9 - 40 (+)	-	--
- CLR	-/+	2 (-), 9 - 40 (+)	-	12 - 24
Taylor rule				
- COR	-/+	0 (-), 8 - 44 (+)	-	--
- CLR	+	9 - 44	-	--
Fed funds rate				
- COR	+	21 - 38	-	0 - 10
- CLR	+	19 - 38	-	0 - 7
(-1) M1 growth				
- COR	-/+	--	-	--
- CLR	-/+	--	-	--
(-1) M1				
- COR	+	5 - 26	-	--
Panel B: Monetary policy instrument – uncertainty pair				
MP instrument	Impulse MP, response UC		Impulse UC, response MP	
	sign	significant from-to (month)	sign	significant from-to (month)
Real interest rate				
- COR	-/+	0 - 1 (-), 11 - 38 (+)	-	--
- CLR	+	0 - 3 (-), 11 - 40 (+)	-	--
Taylor rule				
- COR	-/+	0 - 1 (-), 15 - 42 (+)	-	--
- CLR	-/+	0 - 1 (-), 17 - 43 (+)	-	--
Fed funds rate				
- COR	-/+	--	-	14 - 31
- CLR	-/+	--	-	--
(-1) M1 growth				
- COR	+	3 - 12	-	--
- CLR	+	3 - 12	-	--
(-1) M1				
- COR	+	5 - 19	-	--

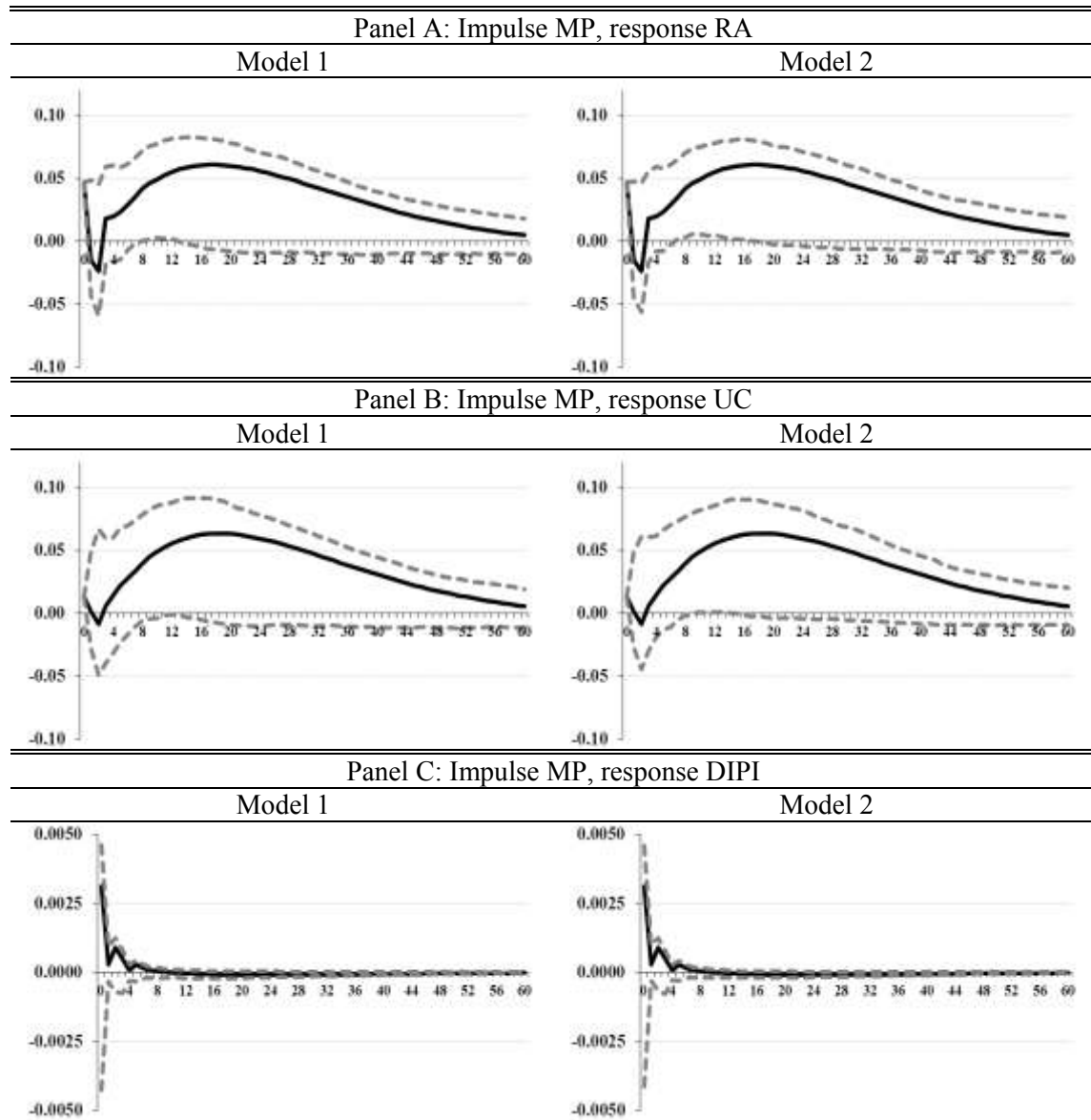
Notes: Table 4 summarizes results for the interactions between monetary policy (as represented by four different measures) and risk aversion (RA) in Panel A and between monetary policy and uncertainty (UC) in panel B in the four-variable model with DIPI, MP, RA and UC. The MP measures considered are: real rate, Taylor rule deviations, Fed funds rate, the negative of the M1 growth. Each Panel lists the range of months for which impulse-response functions (VARs with contemporaneous (COR) and contemporaneous/long-run (CLR) restrictions, respectively) were statistically significant within the 90% confidence interval in the direction indicated in the column “sign”. The last row in each panel considers a specification with M1 and industrial production both entering in levels rather than growth rates (COR restrictions only).

**Figure 5: Monetary policy shock in the 6-variable VAR (CPI EMP FED PPI RA UC)**



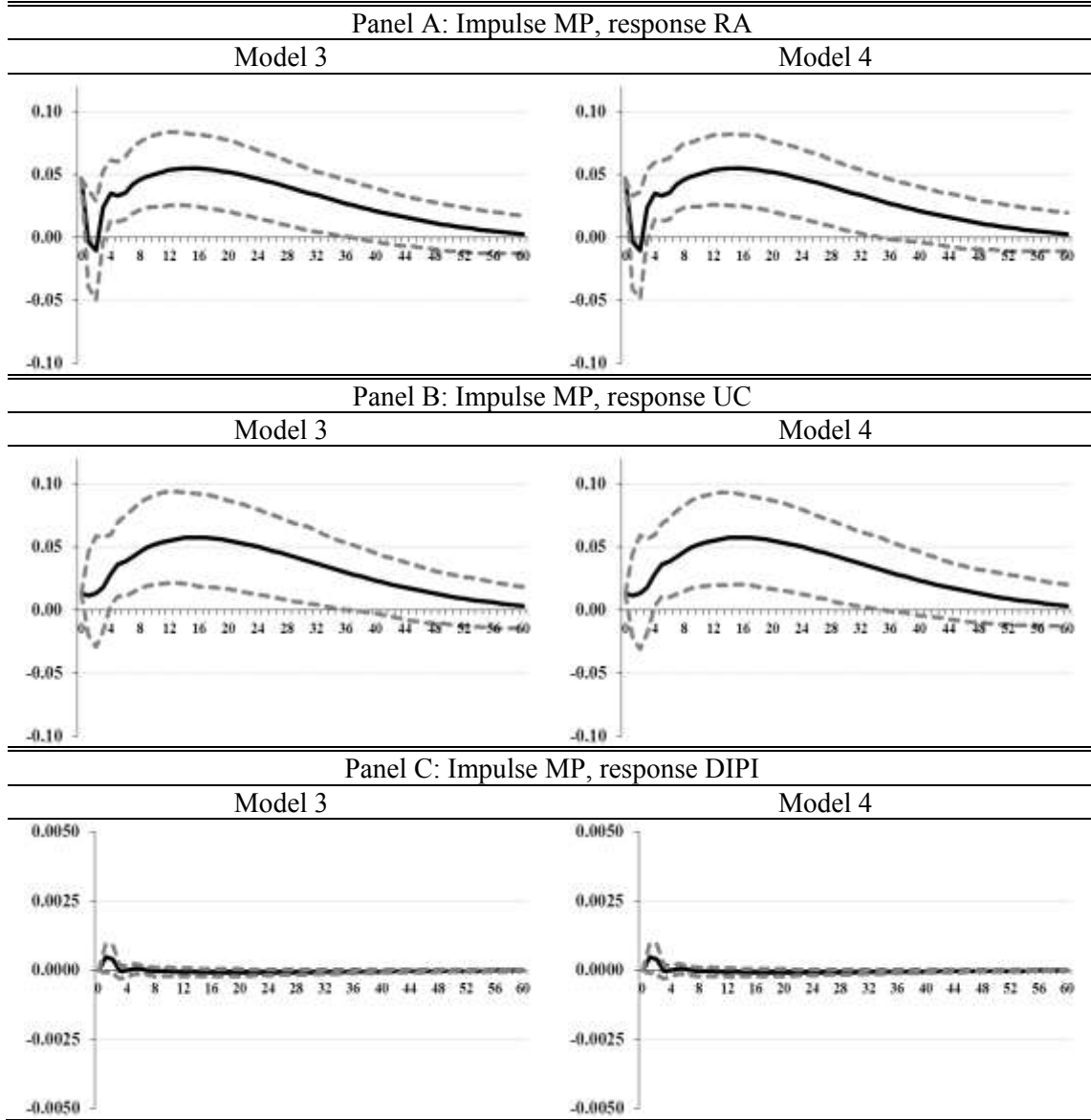
Notes: Panels A-E: Estimated structural impulse-responses (black lines) to a monetary policy shock in the 6-variable model and 90% bootstrapped confidence intervals (dashed grey lines), for the model with 4 lags (selected by Akaike), based on 1000 replications. Panel F: Fractions of the structural variance due to FED shocks for the six variables.

**Figure 6: Identification using high-frequency futures and business cycle news announcements**



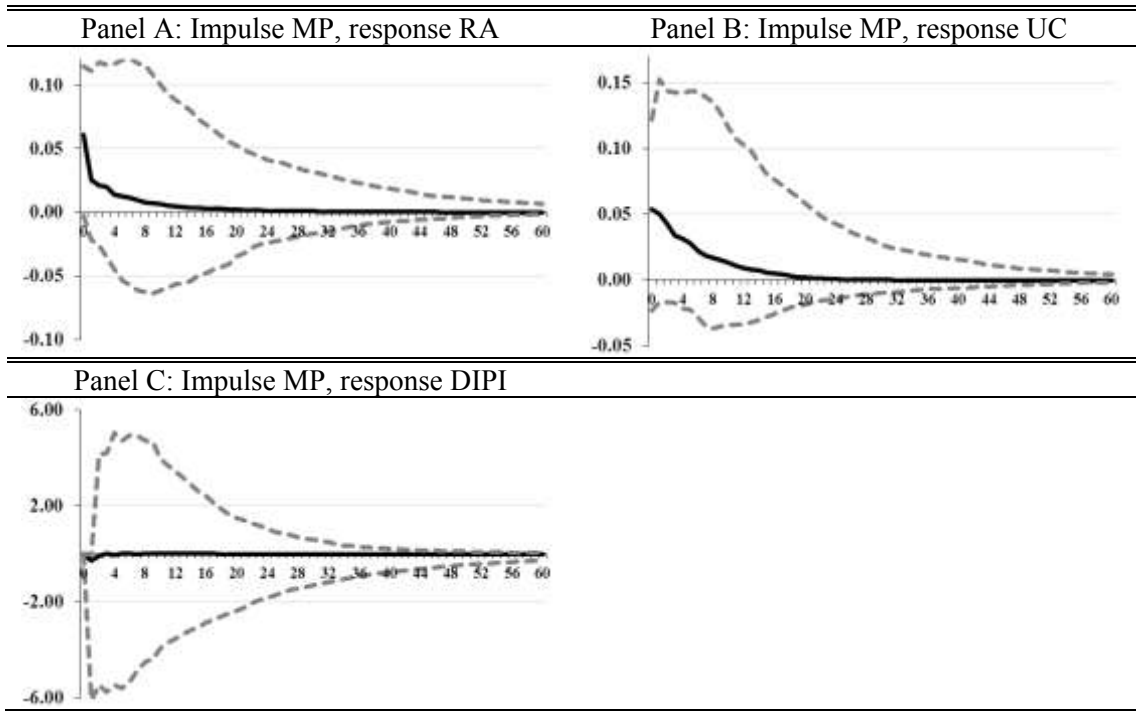
Notes: Estimated structural impulse-response functions (black lines) and 90% bootstrapped confidence intervals (grey dashed lines) for the model with 3 lags (selected by), based on 1000 replications. Four restrictions are derived from high frequency data. Panels on the left present results of Model 1 (BC and MP do not respond instantaneously to RA), panels on the right present results of Model 2 (BC and MP do not respond instantaneously to UC).

**Figure 7: Identification using high-frequency futures**



Notes: Estimated structural impulse-response functions (black lines) and 90% bootstrapped confidence intervals (grey dashed lines) for the model with 3 lags (selected by), based on 1000 replications. Panels on the left present results of Model 3, panels on the right present results of Model 4. Both models assume zero contemporaneous responses of the BC shocks to the other variables. Model 3 (Model 4) assumes that monetary policy does not instantaneously react to RA (UC).

**Figure 8: Identification using daily futures**



Notes: Estimated impulse-response functions to “cleansed” MP surprise (black lines) and 90% bootstrapped confidence intervals (grey dashed lines).

## Appendix: The VIX and Risk

To obtain intuition on how the VIX is related to the actual (“physical”) expected variance of stock returns and to risk preferences, we analyze a one-period discrete state economy. Imagine a stock return distribution with three different states  $x_i$ , as follows:

Good state:  $x_g = \mu + a$  with probability  $(1 - p)/2$ ,

Bad state :  $x_b = \mu - a$  with probability  $(1 - p)/2$ ,

Crash state:  $x_c = c$  with probability  $p$ ,

where  $\mu > 0$ ,  $a > 0$  and  $p > 0$  are parameters to be determined. We set them to match moments of US stock returns - the mean, the variance (standard deviation) and the skewness - while fixing the crash return at an empirically plausible number.

The mean is given by:

$$\bar{X} = \frac{1-p}{2} x_g + \frac{1-p}{2} x_b + pc = (1-p)\mu + pc. \quad (1)$$

The variance is given by:

$$V \equiv \sigma^2 = \frac{1-p}{2} (\mu + a - \bar{X})^2 + \frac{1-p}{2} (\mu - a - \bar{X})^2 + p(c - \bar{X})^2 \quad (2)$$

and the skewness ( $Sk$ ) by:

$$V^{\frac{3}{2}} Sk = \frac{1-p}{2} (\mu + a - \bar{X})^3 + \frac{1-p}{2} (\mu - a - \bar{X})^3 + p(c - \bar{X})^3. \quad (3)$$

Consider an investor with power utility over wealth in a one-period world, so that in equilibrium she invests her entire wealth in the stock market:

$$U(\tilde{W}) = E \left[ \frac{(W_0 \tilde{R})^{1-\gamma}}{1-\gamma} \right], \quad (4)$$

where  $\tilde{R}$  is the gross return on the stock market,  $W_0$  is initial wealth and  $\gamma$  is the coefficient of relative risk aversion.

The “pricing kernel” in this economy is given by marginal utility, denoted by  $m$ , and is proportional to  $\tilde{R}^{-\gamma}$ . Hence, the stochastic part of the pricing kernel moves inversely with the return on the stock market. When the stock market is down, marginal utility is relatively high and vice versa.



The physical variance of the stock market is exogenous in this economy, and is simply given by  $V$ . This variance is computed using the actual probabilities. The VIX represents the “risk-neutral” conditional variance. It is computed using the so-called “risk-neutral probabilities,” which are simply probabilities adjusted for risk.

In particular, for a general state probability  $\pi_i$  for state  $i$ , the risk-neutral probability is:

$$\pi_i^{RN} = \pi_i \frac{m_i}{E[m]} = \pi_i \frac{R_i^{-\gamma}}{E[m]}. \quad (5)$$

So, for a given  $\gamma$ , we can easily compute the risk-neutral probabilities since  $R_i = x_i + 1$ .

For an economy with  $K$  states, the risk-neutral variance is then given by:

$$VIX^2 = \sum_{i=1}^K \pi_i^{RN} (x_i - \bar{X})^2 \quad (6)$$

and the variance premium is:

$$VP = VIX^2 - V = \sum_{i=1}^K (\pi_i^{RN} - \pi_i)(x_i - \bar{X})^2. \quad (7)$$

In our economy, the risk-neutral probability puts more weight on the crash state and the crash state induces plenty of additional variance, rendering the variance premium positive. The higher is risk aversion, the more weight the crash state gets, and the higher the variance premium will be. The expression for the variance premium has a particularly simple form:

$$VP = (\pi_g^{RN} - \frac{1-p}{2})(x_g - \bar{X})^2 + (\pi_b^{RN} - \frac{1-p}{2})(x_b - \bar{X})^2 + (\pi_c^{RN} - p)(x_c - \bar{X})^2 \quad (8)$$

where  $\pi_g^{RN} = \frac{1-p}{2} \frac{(\mu+a+1)^{-\gamma}}{E[m]}$ ,  $\pi_b^{RN} = \frac{1-p}{2} \frac{(\mu-a+1)^{-\gamma}}{E[m]}$  and  $\pi_c^{RN} = p \frac{(c+1)^{-\gamma}}{E[m]}$ .

### *Numerical Examples*

Suppose the statistics to match are as follows:  $\bar{X} = 10\%$ ,  $\sigma = 15\%$ , both on an annualized basis; and  $Sk = -1$  on a monthly basis. We set  $c = -25\%$  (a monthly number). This crash return is in line with the stock market collapses in October 1987 and October 2008. The implied crash probability to match the skewness coefficient of -1 is given by  $p = 0.5\%$ . With a monthly investment horizon, the crash probability implies a crash every 200 months, or roughly once every two decades. Panel A of Appendix Table 1

provides, for different values of the coefficient of relative risk aversion  $\gamma$ , the values for the VIX on an annualized basis in percent (VIX), the log of the VIX on a monthly basis (LVIX), i.e.,  $\log(\text{VIX}/\sqrt{12})$ , the annualized variance premium (VP), and our risk aversion proxy computed on a monthly basis (RA), i.e.,  $\log(\text{VIX}^2/12 - \sigma^2/12)$ . Note that the variance premium and our risk aversion measure are monotonically increasing in the coefficient of relative risk aversion  $\gamma$ .

In structural models,  $\gamma$  is typically assumed to be time-invariant, and the time variation in the variance premium is generated through different mechanisms. For example, in Drechsler and Yaron (2011), who formulate a consumption-based asset pricing model with recursive preferences, the variance premium is directly linked to the probability of a “negative jump” to expected consumption growth. The analogous mechanism in our simple economy would be to decrease the skewness of the return distribution by increasing the crash probability  $p$ . This obviously represents “risk” instead of “risk aversion”. Yet, it is the interaction of risk aversion and skewness that gives rise to large readings in our risk aversion proxy. To illustrate, let us consider an example with lower skewness. Setting skewness equal to -2 requires a higher crash probability of  $p = 1\%$ . Panel B of Appendix Table 1 shows that the VIX increases, and increases more the higher the coefficient of relative risk aversion, both in absolute and in relative terms. The variance premium roughly doubles for all  $\gamma$  levels, whereas our risk aversion proxy increases by about 0.7.

In Bekaert and Engstrom (2010), when a recession becomes more likely, the representative agent also becomes more risk averse through a Campbell-Cochrane (1999)-like external habit formulation. The recession fear then induces high levels of the VIX. We can informally illustrate such a mechanism in our one-period model. Imagine that the utility function is over wealth relative to an exogenous benchmark wealth level  $W_{bm}$ . Normalizing the initial wealth  $W_0$  to 1, the pricing kernel is now given by  $(\tilde{R} - W_{bm})^{-\gamma}$ , and the coefficient of relative risk aversion is  $\gamma \tilde{R}/(\tilde{R} - W_{bm})$ . Consequently, risk aversion is state dependent and increases as  $\tilde{R}$  decreases towards the benchmark level. It is easy to see how a dynamic version of this economy, for instance with a slow-

moving  $W_{bm}$ , could generate risk aversion that is changing over time as return realizations change the distance between actual wealth and the benchmark wealth level.

To illustrate this mechanism, Panel C considers three different benchmark levels for  $W_{bm}$  (0.05, 0.25 and 0.5) with  $\gamma$  fixed at 4 and  $Sk = -1$ , implying  $p = 0.5\%$ . The second column shows expected relative risk aversion in the economy (CRRA), weighting the three possible realizations for risk aversion with the actual state probabilities. The other columns are as in the panels above. Clearly, for  $W_{bm} = 0$ ,  $CRRA = 4$  and we replicate the values in Panel A for  $\gamma = 4$ . Keeping  $\gamma$  fixed and increasing  $W_{bm}$ , effective risk aversion increases. For example, CRRA increases from 4.21 to 7.97 as  $W_{bm}$  increases from 0.05 to 0.5. The VIX increases from 17.87 to 27.93 and our risk aversion proxy RA increases from 2.06 to 3.83. In sum, our risk aversion measure monotonically increases with true risk aversion in the underlying economy.

**Appendix Table 1: The VIX and Risk Aversion**

Panel A: Varying $\gamma$ , $Sk = -1$ , $p = 0.5\%$					
Parameters	VIX	LVIX	VP	RA	
$Sk = -1, \gamma = 2$	15.987	1.529	0.003	0.936	
$Sk = -1, \gamma = 4$	17.612	1.626	0.008	1.960	
$Sk = -1, \gamma = 6$	20.139	1.760	0.018	2.711	
Panel B: Varying $\gamma$ , $Sk = -2$ , $p = 1\%$					
Parameters	VIX	LVIX	VP	RA	
$Sk = -2, \gamma = 2$	16.908	1.585	0.006	1.624	
$Sk = -2, \gamma = 4$	19.841	1.745	0.017	2.643	
$Sk = -2, \gamma = 6$	24.075	1.939	0.036	3.386	
Panel C: Varying $W_{bm}$ , $\gamma = 4$ , $Sk = -1$ , $p = 0.5\%$					
Parameters	CRRA	VIX	LVIX	VP	RA
$\gamma = 4, W_{bm} = 0$	4.000	17.612	1.626	0.008	1.960
$\gamma = 4, W_{bm} = 0.05$	4.209	17.868	1.641	0.009	2.061
$\gamma = 4, W_{bm} = 0.25$	5.323	19.598	1.733	0.016	2.584
$\gamma = 4, W_{bm} = 0.50$	7.968	27.934	2.087	0.056	3.835

Notes: Values of the VIX on an annualized basis in percent (VIX), the log of the VIX on a monthly basis (LVIX), the annualized variance premium (VP), and our proxy for risk aversion on a monthly basis (RA) for different values of the underlying parameters, while keeping the crash return  $c$  fixed at -25%. In Panel A, the varying parameter is the coefficient of relative risk aversion  $\gamma$  while skewness  $Sk$  is fixed at -1. In Panel B, skewness  $Sk$  is fixed at -2. Panel C computes, for  $\gamma$  fixed at 4 and  $Sk$  fixed at -1, expected risk aversion (CRRA) and the other four variables for different values of the benchmark wealth level  $W_{bm}$ .