

NBER WORKING PAPER SERIES

UNITIZATION OF SPATIALLY CONNECTED RENEWABLE RESOURCES

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Working Paper 16338  
<http://www.nber.org/papers/w16338>

NATIONAL BUREAU OF ECONOMIC RESEARCH  
1050 Massachusetts Avenue  
Cambridge, MA 02138  
September 2010

We thank seminar participants at UC San Diego, Association of Environmental and Resource Economists Annual Meeting, Property and Environment Research Center, and UC Santa Barbara. Funding was provided by the Paul Allen Family Foundation. The views expressed herein are those of the authors and do not necessarily reflect the views of the National Bureau of Economic Research.

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NBER Working Paper No. 16338  
September 2010  
JEL No. Q22

**ABSTRACT**

Spatial connectivity of renewable resources induces a spatial externality in extraction. We explore the consequences of decentralized spatial property rights in the presence of spatial externalities. We generalize the notion of unitization - developed to enhance cooperative extraction of oil and gas fields - and apply it to renewable resources which face a similar spatial commons problem. We find that unitizing a common pool renewable resource can yield first-best outcomes even when participation is voluntary, provided profit sharing rules can vary by participant.

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The collapse of many of the world's fisheries (Worm et al. 2006; Myers and Worm 2003; Jackson et al. 2001) has led to the search for policy approaches to prevent further collapse and, perhaps, recover depleted stocks (Worm et al. 2009). The failure of traditional regulation structures to halt this collapse has led economists to propose various property-rights based approaches including Individual Tradeable Quotas (ITQs), which allocate units of harvest, and Territorial User Rights Fisheries (TURFs), which allocate units of space to private firms, cooperatives, or fishermen.<sup>1</sup> Economists argue that appropriate assignment of rights internalizes externalities and facilitates stewardship, leading to sustainability through a profit motive.<sup>2</sup> In the United States, there is growing policy interest in ocean zoning and marine spatial planning, further motivating our inquiry. Yet for spatially connected resources, the spatial commons problem may persist, even when spatial property rights (TURFs) are assigned, monitored, enforced, and perpetual (Janmaat 2005). This occurs because most harvested species of fish exhibit large geographic scales of movement in some part of their life cycle. While enlarging TURFs can help internalize spatial externalities, White and Costello (2010) find that the spatial scale required to internalize dispersal may be several hundreds or thousands of square kilometers.<sup>3</sup> Ocean allocations of that size to a single owner are unlikely, and as such, consideration of coordination (or the lack thereof) between multiple owners of a spatially connected stock becomes paramount.

While compelling, the problem of spatial externalities in a common pool is not new. Multiple owners of mineral rights to an oil or gas field, where adjacent owners have an incentive to over-invest in capital and extract at too rapid a rate, has similar (though not identical) characteristics. A well-known solution in that context is unitization, where landowners are contractually obligated to pool profits to minimize redundant drilling and extraction effort.<sup>4</sup>

We generalize the concept of unitization as a possible solution to the spatial renewable resource problem. The idea is that by sharing profits, each owner has an interest in the profits of other owners, and is thus less likely to over-harvest her own patch for personal gain if it would harm her neighbor. The conditions under which this system works to solve the commons problem is amenable to bioeconomic analysis, and is made possible only by leveraging recent advances in the theory of spatial bioeconomics.

We stress that this is not simply a theoretical exercise, as there are several examples of such institutions that have arisen organically from historical communal use of spatially connected renewable resources.<sup>5</sup> For example, the sakuraebi (a small pink shrimp) fishery of Japan is an example of a profit-sharing system across TURFs that was introduced to alleviate inefficiencies associated with decentralized harvest by three separate TURFs within Suruga Bay. While the introduction of the TURF system had promoted rationalization within each of the three TURFs, stock dispersal and heterogeneity had led to stringent competition between TURFs; this competition went so far as to include on and off-shore violence (Uchida and Wilen 2004). Ten years of this destructive behavior led the shrimp fishermen to form the Sakuraebi Harvesters' Association (SHA) to coordinate harvest between the individual TURFs. The SHA manages fishing activity on a daily basis, and as a result, only half the fleet will be engaged in fishing on any given day. From the landed sales, a percentage fee is collected by the SHA, with the remaining revenue net of fixed costs divided among boat captains and crew members (Uchida and Baba 2008).

Another spatial fishery of note is the fishing cooperatives of Baja California, Mexico, a collection of small community-based cooperative fisheries that primarily target spiny lobster and abalone. Several of these fisheries in the Vizcaino Peninsula region have formed

a federation (Fedecoop) to coordinate harvest across the spatial fisheries. Each of the 9 members of Fedecoop contribute a 30% profit share to the federation, which in turn provides benefits for the individual cooperatives. While not a spatially defined fishery, the Chignik salmon fishery of Alaska featured a short-lived cooperative whereby roughly 20% of license holders participated in fishing, while the remaining members were idle. Revenues were then returned to cooperative members based on a pre-determined formula, such that fishing members received \$63,000 and non-fishing members received \$23,000 (Costello and Deacon 2007).<sup>6</sup>

While sharing institutions have emerged in ad hoc examples, no comprehensive theory exists to help guide the design of these institutions across spatial property rights owners. For example, can first-best efficient harvest be achieved with unitization? How does the structure of profit sharing affect the achievement of first-best outcomes? How would design depend on the biological or economic characteristics of the fishery? Is contractual obligation required? Or can the unitization scheme be designed to incentivize participation? We address these questions below.

This work incorporates a general framework of harvest decisions where a number of owners make decentralized decisions regarding spatially explicit resource use. The general renewable resource model we consider is both dynamic and spatial; resources grow and disperse. Spatial connectivity among resource “patches” (e.g. fish/larval movement) creates a spatial externality.<sup>7</sup> Unsurprisingly, in the absence of coordination, patch owners will tend to overexploit the resident stock. Thus, any discussion of efficiency will have to consider both dynamic and spatial externalities, in addition to strategic behavior between patch owners. The dynamic aspect of the model is in the spirit of existing dynamic optimization models

(Clark 1990), while the spatial aspects build on existing models of “patchy” bioeconomics, e.g. Brown and Roughgarden (1997) Sanchirico and Wilen (1999), Sanchirico and Wilen (2001), Sanchirico and Wilen (2002) Sanchirico and Wilen (2005) and Costello and Polasky (2008). A related literature considers the joint exploitation of a single resource stock by several agents, building on seminal work in Levhari and Mirman (1980) and Munro (1979). This “fish wars” literature identified a persistent externality of one country on another where the resource stock moved across jurisdictions, a phenomenon that has recently been corroborated empirically (McWhinnie 2009). While many of the insights of that literature also apply here, we extend the bioeconomic model to allow for resource production and dispersal in each jurisdiction (i.e. a “metapopulation”) and explore the ability of unitization to correct the ensuing externality across spatial property rights owners.

By exploiting the special structure of our dynamic and spatial game we are able to obtain sharp analytical results of an otherwise intractable problem. Our benchmark case accords with the results of Janmaat (2005) who finds that for spatially connected renewable resources, spatial property rights alone do not yield efficient outcomes, except in trivial cases. We then consider coordination between patch owners via a generalization of unitization. Under unitization, each member contributes a share of her profit to a general pool that is ultimately redistributed across members in a particular way. The details of the levels of contribution and redistribution affect both efficiency and participation; this is the focus of much of our analysis.

If properly designed, unitization acts to mitigate the commons problem. Thus the individual patch owner’s decisions appear more like those of the sole owner. We find that under contractually mandatory participation, unitization can yield first-best outcomes, but

only when all profits are pooled. We show that allowing for endogenous participation in the unitization scheme can still yield first-best outcomes, provided that shares can vary across participants. We proceed by developing an analytical model of spatially-connected renewable resources and deriving results regarding the ability of a well-engineered unitization scheme to achieve efficiency in resource use when participation is mandatory, and when it is voluntary.

## 1 A model of spatial property rights for renewable resources

We require a spatially explicit dynamic bioeconomic model that is analytically tractable yet allows for spatial heterogeneity in economics, biology, and the environment. We build upon the dynamic model structure in Costello and Polasky (2008). Each of  $N$  resource patches, indexed  $i = 1, 2, \dots, N$ , is exclusively managed by a single owner who chooses harvest in her own patch in discrete time periods,  $t = 0, 1, 2, \dots$ . Tenure is assumed to be guaranteed and infinite.<sup>8</sup> While our theory applies to any spatially connected renewable resource, it facilitates exposition to focus on the fishery as an example.

### 1.1 Growth and spatial connectivity

Stock at the beginning of time  $t$  in patch  $i$  is given by  $x_{it}$ . Harvest in each patch  $i$  is a decision variable at each time  $t$  and is given by  $h_{it}$ , and escapement  $e_{it}$  is defined as  $e_{it} = x_{it} - h_{it}$ . Patches are spatially interconnected, e.g. by migrating fish or larvae dispersing via ocean currents. The timing is thus: the present period stock ( $x_{it}$ ) is observed and then harvested

( $h_{it}$ ) resulting in escapement ( $e_{it}$ ). This escapement produces young who disperse according to the following equation of motion:

$$x_{it+1} = \sum_j^N f_j(e_{jt})D_{ji}, \quad (1)$$

where  $f_j(e_{jt})$  is a patch specific growth function that reflects idiosyncracies of patch ecology (e.g. habitat quality) and  $D_{ji}$  is the fraction of resident stock that disperses from patch  $j$  to patch  $i$  each period,  $D_{ji} \geq 0$ ,  $\sum_i^N D_{ji} = 1$ , where  $D_{jj} \leq 1$  reflects self-retention (Mitarai et al. 2009).<sup>9</sup> The initial stock in patch  $i$  is  $x_{i0}$ . The function  $f_i(e)$  is assumed to have the standard properties for all  $i$ :  $f'_i(e) > 0$ ,  $f''_i(e) < 0$ , and  $f_i(0) = 0$ .

## 1.2 Economic returns

In addition to patch specific heterogeneity in production and dispersal, we allow for differential economic returns. The current period profit from harvesting  $h_{it}$  from patch  $i$  at time  $t$  is given by the harvest model:<sup>10</sup>

$$\Pi_{it} = (p_i - c_i)h_{it} \quad (2)$$

$$= b_i(x_{it} - e_{it}), \quad (3)$$

where  $p_i$  and  $c_i$  are patch-specific prices and marginal harvest costs, we define as marginal profit  $b_i \equiv p_i - c_i$ , and make use of the identity  $h_{it} \equiv x_{it} - e_{it}$ . By assuming  $b_i > 0 \forall i$ , we ensure that some harvest would always be (at least myopically) profitable in every patch. Before considering the problem faced by decentralized patch owners under unitization,



the next section derives two key results for comparison: the sole owner solution and the uncoordinated, decentralized solution.

## 2 Benchmark results

### 2.1 *The sole owner*

Consider the benchmark case where a sole owner simultaneously manages all  $N$  interconnected resource patches. Even for a sole owner, this poses a formidable challenge as it generalizes the standard renewable resource harvesting problem to account for spatial interconnections (via  $D_{ji}$ ) among an arbitrarily large collection of patches. By imposing a modest amount of structure on this problem, we will be able to derive closed form analytical results. We thus restrict attention to interior solutions where some harvest occurs in each patch. While corner solutions (where some patches are optimally left unharvested or are harvested to extinction) are a theoretical possibility (see Costello and Polasky (2008)), we assume that conditions are such that some positive but non-extinguishing harvest is optimal:  $x_{it} > h_{it} > 0 \forall i, t$ . We also adopt a benign assumption about dispersal:

**Assumption 1.** *There is some out-of-patch dispersal:  $D_{ii} < 1, \forall i$ .*

This assumption simply requires that patches are in fact spatially-connected, such that some of the larvae from patch  $i$  will disperse to patch  $j$ . A violation of this assumption (so  $D_{ii} = 1$ ) trivializes the problem by eliminating spatial connectivity, whereby the sole owner solves a series of  $N$  unconnected standard renewable resource harvesting problems.

The sole owner's objective is to maximize the discounted net present value of profit

(Equation 2) across all patches and all time. Letting  $\mathbf{x}_t$  denote the vector  $[x_{1t} \dots x_{Nt}]$ , the sole owner's dynamic programming equation is:

$$V_t(\mathbf{x}_t) = \max_{\mathbf{e}_t} \sum_{i=1}^I b_i(x_{it} - e_{it}) + \delta V_{t+1}(\mathbf{x}_{t+1}), \quad (4)$$

which is subject to the biological constraints (Equation 1), and a discount factor  $\delta \leq 1$ .

Differentiating with respect to escapement gives the following necessary condition for an interior solution:

$$-b_i + \delta \sum_{j=1}^N \frac{\partial V_{t+1}(\mathbf{x}_{t+1})}{\partial x_{jt+1}} \frac{\partial x_{jt+1}}{\partial e_{it}} = 0 \quad \forall i, \quad (5)$$

where the first term captures the marginal cost of increasing escapement (and thus decreasing harvest) in the current period, and the second captures the marginal benefit in future payoffs to all patches from that increase in escapement. Because all patches are owned by the same harvester, spillovers from dispersal from each patch are fully internalized.

This complicated dynamic optimization problem has a special structure, called “state independent control,” for which the first-order conditions are independent of stock,  $x_{it}$  (Costello and Polasky 2008). This allows us to separate the problem temporally, and implies that escapement is location-specific, but time-independent (Proposition 1 in Costello and Polasky (2008)). This result accords with, but extends, existing resource models with perfectly elastic demand for which a bang-bang solution is implemented to achieve an optimal escapement. Because optimal escapement in patch  $i$  is constant, additional units of stock are simply harvested, so the shadow value on stock is simply its net price:  $\frac{\partial V_{t+1}(\mathbf{x}_{t+1})}{\partial x_{jt+1}} = b_j \quad \forall j$ . The final term,  $\frac{\partial x_{jt+1}}{\partial e_{it}}$  equals  $f'_i(e_{it})D_{ij}$  by rewriting Equation 1 in terms of  $x_{jt+1}$  and differenti-

ating with respect to  $e_{it}$ . Thus, what would otherwise be an extremely complicated spatial temporal optimization problem has a first order condition that compactly reduces to:

$$-b_i + \delta \sum_{j=1}^N b_j f'_i(e_{it}^{SO}) D_{ij} = 0 \quad \forall i. \quad (6)$$

The optimal level of escapement under a sole owner  $e_{it}^{SO}$  will trade off the present benefit of harvest against the sum of future growth and dispersal to all patches, yielding a spatially modified golden rule for spatially-connected renewable resources:

$$f'_i(e_{it}^{SO}) = \frac{b_i}{\delta \sum_{j=1}^N b_j D_{ij}} \quad \forall i. \quad (7)$$

By the concavity of  $f_i(e_i)$ ,  $e_{it}^{SO}$  is thus decreasing in own price ( $b_i$ ) and increasing in the discount factor,  $\delta$ . Note that Equation 7 collapses to the familiar golden rule of resource economics in the absence of space:  $f'(e) = 1/\delta$ . While Equation 7 provides a useful benchmark, the remainder of this paper is devoted to the case of decentralized ownership of these resource patches.

## 2.2 Uncoordinated Spatial Ownership

The other benchmark case we will require is uncoordinated, decentralized ownership of the  $N$  patches. When coordination is absent, each of the  $N$  patch owners maximizes her patch-specific returns, taking as given the behavior of connected patch owners. The dynamic programming equation for owner  $i$  is:

$$V_{it}(\mathbf{x}_t) = \max_{e_{it}} b_i(x_{it} - e_{it}) + \delta V_{it+1}(\mathbf{x}_{t+1}). \quad (8)$$

Owner  $i$ 's choice must now account for the effect of all other patch owners' decisions on her value function. The necessary condition for owner  $i$  is:

$$-b_i + \delta \left[ \frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{1t+1}} \frac{\partial x_{1t+1}}{\partial e_{it}} + \frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{2t+1}} \frac{\partial x_{2t+1}}{\partial e_{it}} + \dots + \frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{Nt+1}} \frac{\partial x_{Nt+1}}{\partial e_{it}} \right] = 0, \text{ or } (9)$$

$$-b_i + \delta \sum_{j=1}^N \frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{jt+1}} \frac{\partial x_{jt+1}}{\partial e_{it}} = 0. (10)$$

Consider a Cournot-style model where each owner simultaneously chooses her own escapement taking all other escapements as given. Fixing  $e_{jt+1}$  implies  $\frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{jt+1}} = 0 \forall j \neq i$ . This follows because owner  $j$  simply harvests the additional stock down to  $e_{jt+1}$ , leaving no residual profit for capture by owner  $i$ . This useful observation implies that the necessary condition for owner  $i$  reduces to:

$$-b_i + \delta \frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{it+1}} \frac{\partial x_{it+1}}{\partial e_{it}} = 0. (11)$$

Because this remains a state independent control problem,  $\frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{it+1}} = b_i$  and  $\frac{\partial x_{it+1}}{\partial e_{it}} = f'_i(e_{it})D_{ii}$  by differentiating Equation 1.<sup>11</sup> The best response function of owner  $i$  simply reduces to:

$$-b_i + \delta b_i f'_i(e_{it}) D_{ii} = 0. (12)$$

Importantly, owner  $i$ 's choice is independent of other owners' escapements. Rewriting the necessary condition, Equation 12, gives the following uncoordinated escapement rule  $e_{it}^{\mathcal{UC}}$  for owner  $i$ :

$$f'_i(e_{it}^{\mathcal{UC}}) = \frac{1}{\delta D_{ii}}. (13)$$

Because owner  $i$ 's best response is independent of  $e_{jt}$  ( $j \neq i$ ), Equation 13 defines a unique subgame perfect Nash equilibrium vector of escapements for each owner under decentralized ownership. This result leads to the following first proposition regarding the efficiency of spatial property rights in the absence of coordination.

**Proposition 1.** *Under Assumption 1,  $e_{it}^{UC} < e_{it}^{SO}$ .*

*Proof.* By Equation 7 we have  $f'_i(e_{it}^{SO}) = \frac{1}{\delta D_{ii} + \delta \sum_{j \neq i}^N (b_j/b_i) D_{ij}} < \frac{1}{\delta D_{ii}} = f'_i(e_{it}^{UC})$ . Because  $f'_i(e) > 0$  and  $f''_i(e) < 0$ ,  $e_{it}^{UC} < e_{it}^{SO}$ .  $\square$

The magnitude of the difference between the sole owner and uncoordinated equilibria will depend on the extent of the spatial externality, captured by the out-dispersal term in the denominator  $\delta \sum_{j \neq i}^N (b_j/b_i) D_{ij}$ . The larger is this term, the larger is the wedge between the sole owner's escapement in that patch and that which is chosen by the uncoordinated owner.<sup>12</sup> To the extent that uncoordinated harvest is inefficiently excessive (see Proposition 1), coordination will be required to align incentives across spatial rights holders. While it is true that uncoordinated spatial property rights may fail to completely solve the commons problem, it is likely that the owners themselves would also recognize this fact, and take steps to coordinate. We address this topic below, beginning with a simple, yet powerful coordinating mechanism.

### 3 Unitization

We have shown that even with well defined and enforced spatial property rights, uncoordinated owners will typically not achieve economically efficient resource use (Proposition

1). Coordination may be induced by a Coasian bargaining solution or by other mechanisms requiring side payments between users. Real world examples of spatial property rights in renewable resources may involve hundreds of interconnected patches, and thus the number of side payments would quickly become large ( $\frac{N(N-1)}{2}$ ).<sup>13</sup> We thus focus on unitization as a simple budget balanced, fully internal mechanism with no required side payments.

### 3.1 Unitization

Consider a unitization scheme where each owner makes a *contribution*  $0 \leq \alpha_i \leq 1$  of her profits to a pool.<sup>14</sup> *Dividend*  $0 \leq \gamma_i \leq 1$  of this aggregate pool is then redistributed to patch  $i$ , such that  $\sum_i^N \gamma_i = 1$ .<sup>15</sup> A particular unitization scheme is defined by  $\{\boldsymbol{\alpha}, \boldsymbol{\gamma}\}$ , where  $\boldsymbol{\alpha} = [\alpha_1, \alpha_2, \dots, \alpha_N]$  and  $\boldsymbol{\gamma} = [\gamma_1, \gamma_2, \dots, \gamma_N]$ . For the first part of our analysis, we adopt the following assumption regarding participation in unitization:

**Assumption 2.** *All  $N$  owners are contractually obligated to participate in the unitization scheme,  $\{\boldsymbol{\alpha}, \boldsymbol{\gamma}\}$ .*

Under Assumption 2, patch owners are legally bound to participate in the unitization scheme, as is typically the case for mineral rights owners in unitized oil and gas fields. If  $\alpha_i = 0 \forall i$ , no profit sharing occurs, and thus the resource is not unitized and owners are uncoordinated. If  $\alpha_i = 1 \forall i$ , then all profits are shared (as is the case for unitized oil and gas fields); subsequent redistribution to each owner is governed by  $\boldsymbol{\gamma}$ . In the general case ( $0 < \alpha_i < 1$ ) each individual owner chooses escapement conditional on  $\alpha_i$  and  $\gamma_i$ , taking other owners' decisions as given.<sup>16</sup>

The dynamic programming equation for patch owner  $i$  is given by:

$$V_{it}(\mathbf{x}_t) = \max_{e_{it}} (1 - \alpha_i)b_i(x_{it} - e_{it}) + \alpha_i\gamma_i \sum_{j=1}^N b_j(x_{jt} - e_{jt}) + \delta V_{it+1}(\mathbf{x}_{t+1}) \quad (14)$$

with necessary condition:

$$-(1 - \alpha_i)b_i - \alpha_i\gamma_i b_i + \delta \sum_{j=1}^N \frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{jt+1}} \frac{\partial x_{jt+1}}{\partial e_{it}} = 0. \quad (15)$$

Because owner  $i$  takes all  $e_{jt}$  ( $j \neq i$ ) as given, from the perspective of owner  $i$ , owner  $j$  immediately harvests any additional stock down to the given escapement level yielding marginal value,  $b_j$ . That value accrues to owner  $i$  based on the dividend, and we obtain:

$$\frac{\partial V_{it+1}(\mathbf{x}_{t+1})}{\partial x_{jt+1}} = \gamma_i b_j \quad \forall i, j. \text{ Combining this along with differentiation of Equation 1 gives owner}$$

$i$ 's best response function:

$$-(1 - \alpha_i)b_i - \alpha_i\gamma_i b_i + \delta \left( (1 - \alpha_i)b_i f'_i(e_{it}) D_{ii} + \alpha_i\gamma_i \sum_{j=1}^N b_j f'_i(e_{it}) D_{ij} \right) = 0, \quad (16)$$

which remains independent of any other owner's escapement decision. The left hand terms represents the current period marginal cost of increasing escapement:  $(1 - \alpha_i)$  forgone private harvest value, and  $\alpha_i\gamma_i$  share of the foregone harvest value. The right term represents the marginal benefit: discounted private  $(1 - \alpha_i)$  and pooled  $(\alpha_i\gamma_i)$  share of future value of marginal growth and dispersal of the resource.

Thus, we can immediately write the resulting optimal escapement rule  $e_{it}^{\{\alpha, \gamma\}}$  as a function of the unitization scheme  $\{\alpha, \gamma\}$  as follows:

$$f'_i(e_{it}^{\{\alpha, \gamma\}}) = \frac{(1 - \alpha_i)b_i + \alpha_i\gamma_i b_i}{\delta((1 - \alpha_i)b_i D_{ii} + \alpha_i\gamma_i \sum_{j=1}^N b_j D_{ij})}. \quad (17)$$

Equation 17 defines a unique subgame perfect Nash equilibrium vector of escapements for each owner under unitization scheme  $\{\alpha, \gamma\}$ .<sup>17</sup> How does the profile of escapements under

unitization compare to the profile under a sole owner of the spatially connected renewable resource? It turns out that the escapement under unitization is inefficiently low (i.e. harvest is excessive) in all patches, as is formalized below:

**Proposition 2.** *Under Assumptions 1-2 and provided  $\alpha_i < 1$ ,  $e_i^{\{\alpha, \gamma\}} < e_i^{SO}$ ,  $\forall i$ .*

*Proof.* Per Equations 7 and 17, this requires that  $\frac{(1-\alpha_i)b_i + \alpha_i\gamma_i b_i}{\delta((1-\alpha_i)b_i D_{ii} + \alpha_i\gamma_i \sum_{j=1}^N b_j D_{ij})} > \frac{b_i}{\delta \sum_{j=1}^N b_j D_{ij}}$ . Rearranging, this requires  $\frac{(1-\alpha_i)b_i \sum_{j=1}^N b_j D_{ij}}{b_i(1-\alpha_i)b_i D_{ii}} > 1$ , or simply that  $\frac{\sum_{j=1}^N b_j D_{ij}}{b_i D_{ii}} > 1$ , which trivially holds, and thus  $e_i^{\{\alpha, \gamma\}} < e_i^{SO}$ .  $\square$

While Proposition 2 shows that unitization leads to inefficient harvest levels, it seems intuitive that sharing a larger fraction of profits would enhance efficiency because larger contributions lead owners to take more account of the spatial externality. This intuition is formalized below:

**Proposition 3.** *Under Assumptions 1-2, an increase in contribution  $0 < \alpha_i < 1$  leads to an increase in the efficiency of the fishery.*

*Proof.* Proposition 2 implies  $f'_i(e_i^{\{\alpha, \gamma\}}) > f'_i(e_i^{SO})$ . Next, we show that  $\frac{de_i}{d\alpha_i} > 0$ . By the implicit function theorem and Equation 17,  $\frac{de_i}{d\alpha_i} = -\frac{b_i\gamma_i \sum_{j \neq i}^N D_{ij}}{\delta[(1-\alpha_i)b_i D_{ii} + \alpha_i\gamma_i \sum_{j=1}^N b_j D_{ij}]^2 f''_i(e_i^{\{\alpha, \gamma\}})}$ . By the concavity of  $f_i(\cdot)$ ,  $\frac{de_i}{d\alpha_i} > 0$ . We next show that total fishery profits are increasing in escapement  $e_i$  when  $e_i < e_i^{SO}$  and regardless of  $e_j$ . The total fishery present value (assuming the steady-state is reached after the initial period) for a given vector of escapements  $e_1, e_2, \dots, e_N$  is given by:

$$\pi(e_1, e_2, \dots, e_N) = \sum_{i=1}^N b_i(x_{i0} - e_i) + \frac{\delta}{1-\delta} \sum_{i=1}^N b_i(x_i - e_i) \quad (18)$$



The change in fishery present value due to a change in escapement in one patch  $e_i$  is given by:

$$\frac{d\pi}{de_i} = -b_i + \frac{\delta}{1-\delta} \left( \sum_{j=1}^N b_j f'_i(e_i) D_{ij} - b_i \right) \quad (19)$$

which is independent of  $e_j, \forall j \neq i$ . The present value of the fishery is maximized when Equation 19 is equal to zero, which yields escapement identical to the sole owner escapement  $e_i^{SO}$  defined in 7. For  $e_i < e_i^{SO}$ ,  $f'_i(e_i) > f'_i(e_i^{SO})$ , and thus  $\frac{d\pi}{de_i} > 0$ . Finally, the change in total fishery present value due to a change in contribution  $\alpha_i$  is simply given by  $\frac{d\pi}{d\alpha_i} = \frac{d\pi}{de_i^{\{\alpha, \gamma\}}} \frac{de_i^{\{\alpha, \gamma\}}}{d\alpha_i} > 0$ .

□

The intuition underlying Proposition 3 is that an increase in the contribution increases the dependence of owner  $i$ 's profits on the performance of spatially connected owners. Thus, owner  $i$  will place more weight on how her escapement affects the profits of her neighbors.

We have shown that escapement under “partial” unitization (when  $\alpha_i < 1 \forall i$ ) is inefficiently low and that increasing the contribution  $\alpha_i$  increases the efficiency of the fishery. This raises the question: How efficient is full unitization ( $\alpha_i = 1 \forall i$ )? Let  $e_i^{\mathcal{F}}$  be the escapement chosen by each owner under full unitization. The following proposition shows that this escapement level will be equivalent to the first-best.

**Proposition 4.** *Under Assumptions 1-2, the subgame perfect Nash equilibrium escapement under full unitization ( $\alpha_i = 1 \forall i$ ) is identical to the economically efficient sole owner's escapement,  $e_i^{\mathcal{F}} = e_i^{SO}, \forall i$ .*

*Proof.* Setting  $\alpha_i = 1$  in Equation 17 yields the following escapement rule under full unitization:

$$f'_i(e_i^{\mathcal{F}}) = \frac{b_i}{\delta \sum_{j=1}^N b_j D_{ij}}. \quad (20)$$

The result follows by inspection of Equations 20 and 7. □

This intuitive yet powerful result seems to solve our efficiency problem: simply constraining all users to fully share profits yields economic efficiency. Under full unitization, each owner chooses the escapement in her patch that maximizes the joint return of all patches, which is precisely the decision that a sole owner would make. This derivation yields an additional useful result:

**Corollary 1.** *Under Assumptions 1 - 2 and full unitization  $\alpha_i = 1$ , the efficiency of unitization is independent of the dividend  $\gamma_i \forall i$ .*

*Proof.* This result follows from the fact that Equation 20 is independent of  $\gamma_i$ . □

Provided that all patch owners are mandated to participate in the scheme, each patch owner's escapement choice is identical to the first-best choice, regardless of the dividend. However, while the intensive margin decision of escapement is independent of the dividend, the extensive margin decision to participate will clearly depend on this dividend. In the following section, we consider the effects of unitization when participation is voluntary.

## 4 Unitization with Endogenous Participation

In oil and gas unitization in the United States, participation is typically mandatory. Mineral rights holders in unitized oil and gas fields are required to share profits in a fully unitized manner ( $\alpha_i = 1 \forall i$ ). We have shown that a similar legal obligation might solve the spatial externality problem present for spatially connected renewable resource owners. But we ask whether contractual obligation is necessary for efficiency. Here we endogenize participation decisions in order to determine if unitization need be mandatory in order to produce a first-best efficient outcome.

### 4.1 Repeated play by patch owners

To explore the individual rationality of participation in the unitization scheme  $\{\alpha, \gamma\}$ , we couch our bioeconomic model as an infinitely repeated Prisoner's Dilemma game with  $N$  members. The relevant per-period payoffs are given below:

$$\Pi_i^C = \gamma_i \sum_{j=1}^N b_j(x_j^{\mathcal{F}} - e_j^{\mathcal{F}}), \quad (21)$$

$$\Pi_i^N = b_i(x_i^{\mathcal{F}} - e_i^{\mathcal{UC}}), \quad (22)$$

$$\Pi_i^D = b_i(x_i^{\mathcal{UC}} - e_i^{\mathcal{UC}}). \quad (23)$$

$\Pi_i^C$  represents the shared profit of cooperation when all players choose the fully efficient escapement levels  $e_i^{\mathcal{F}}$ .  $\Pi_i^N$  represents  $i$ 's profit from defecting and choosing  $e_i^{\mathcal{UC}}$  while the other owners play  $e_{j \neq i}^{\mathcal{F}}$ . Finally,  $\Pi_i^D$  represents  $i$ 's profit when all owners choose their uncoordinated escapement,  $e_i^{\mathcal{UC}}$ , i.e. when everyone defects.

There are many potential strategies to consider, and we adopt a Nash reversion strategy to punish defectors. Under this punishment strategy, any defector is punished forever by all

other owners reverting to  $e_i^{\mathcal{UC}}$ . Here, if owner  $i$  defects during period  $t$ , she will enjoy the fruits of her defection in that first period, and will be ‘punished’ by every other owner defecting in the subsequent periods. Thus, we can calculate the dynamic benefits of cooperation and defection as follows. The present value of profits from cooperation forever are the discounted sum of  $\Pi_i^C$ :

$$\begin{aligned} J_i^C &= \Pi_i^C + \sum_{t=1}^{\infty} \delta^t \Pi_i^C \\ &= \frac{1}{1-\delta} \gamma_i \sum_{j=1}^N b_j (x_j^{\mathcal{F}} - e_j^{\mathcal{F}}). \end{aligned} \tag{24}$$

Defection amounts to choosing the uncoordinated escapement of  $e_i^{\mathcal{UC}}$ , which leads to a steady-state defection stock of  $x_i^{\mathcal{UC}}$ . Thus, the present value of profit to owner  $i$  from defecting is:

$$\begin{aligned} J_i^D &= \Pi_i^N + \sum_{t=1}^{\infty} \delta^t \Pi_i^D \\ &= b_i (x_i^{\mathcal{F}} - e_i^{\mathcal{UC}}) + \frac{\delta}{1-\delta} b_i (x_i^{\mathcal{UC}} - e_i^{\mathcal{UC}}). \end{aligned} \tag{25}$$

The first term represents the first period benefit of defection (choosing the uncoordinated level of escapement while every other owner is still playing cooperatively), while the second represents the discounted stream of benefits from the steady-state uncoordinated equilibrium. Given the history of play, each owner will consider her profit taking as given the escapement of other owners. In essence, owners will consider the short-term benefits of defection versus the long-term difference in profits between sharing a cooperative equilibrium and going it alone. If we find conditions under which  $J_i^C \geq J_i^D$  for all owners  $i$ , then unitization is efficient and supportable as a subgame perfect Nash Equilibrium. Whether this occurs will depend

on the design of the unitization scheme. Because efficiency requires  $\alpha_i = 1 \forall i$  (Proposition 4), we focus on the importance of the set of dividends  $\boldsymbol{\gamma} = [\gamma_1, \gamma_2, \dots, \gamma_N]$ .

## 4.2 Patch-specific dividends

We leverage the fact that our unitization scheme allows the dividends  $\gamma_i$  to vary across patch owners. The key question here is: Does a set of dividends exist that 1) encourages full participation and 2) is feasible? In considering this question, the result in Corollary 1 becomes crucial. Because harvest efficiency by each patch owner is independent of  $\gamma_i$ , we can consider the minimum  $\gamma_i$ , denoted  $\hat{\gamma}_i$ , such that patch owner  $i$  would prefer cooperation (equation 24) to defection (equation 25). As long as  $\sum_i^N \hat{\gamma}_i \leq 1$ , the share structure is feasible and yields first-best efficiency for the fishery.

From Equation 24 and Equation 25, the minimum dividend  $\hat{\gamma}_i$  for owner  $i$  requires:

$$\frac{1}{1-\delta} \hat{\gamma}_i \sum_{j=1}^N b_j (x_j^{\mathcal{F}} - e_j^{\mathcal{F}}) = b_i (x_i^{\mathcal{F}} - e_i^{\mathcal{UC}}) + \frac{\delta}{1-\delta} b_i (x_i^{\mathcal{UC}} - e_i^{\mathcal{UC}}). \quad (26)$$

Solving for  $\hat{\gamma}_i$  gives the indifferent dividend for patch  $i$ :

$$\hat{\gamma}_i = \frac{b_i ((1-\delta)x_i^{\mathcal{F}} + \delta x_i^{\mathcal{UC}} - e_i^{\mathcal{UC}})}{\sum_{j=1}^N b_j (x_j^{\mathcal{F}} - e_j^{\mathcal{F}})}. \quad (27)$$

To explore the determinants of  $\hat{\gamma}_i$ , we will adopt the following approach. Consider a spatially connected renewable resource with  $N$  patch owners, and focus on two such owners, labeled  $i$  and  $j$ . What characteristics of these patch owners lead to high, or low, values of  $\hat{\gamma}_i$  and  $\hat{\gamma}_j$ ? To answer this question, we isolate effects by holding in common all characteristics between patches  $i$  and  $j$ , save one. We define the following conditions:

**Condition 1.** Patches  $i$  and  $j$  have “equi-inflow” if  $D_{ki} = D_{kj}$  for all  $k$ .

**Condition 2.** Patches  $i$  and  $j$  have “equi-price” if  $b_i = b_j$ .

**Condition 3.** Patches  $i$  and  $j$  have “equi-production” if  $f_i(e) = f_j(e)$ .

**Condition 4.** Patches  $i$  and  $j$  have “equi-retention” if  $D_{ii} = D_{jj}$ .

We are interested in comparing  $\hat{\gamma}_i$  to  $\hat{\gamma}_j$ . We begin by noting that the denominator for  $\hat{\gamma}_i$  from Equation 27 is the same as the denominator for  $\hat{\gamma}_j$ . Whether  $\hat{\gamma}_i \leq \hat{\gamma}_j$  requires considering only the numerators:

$$b_i((1 - \delta)x_i^{\mathcal{F}} + \delta x_i^{\mathcal{UC}} - e_i^{\mathcal{UC}}) \leq b_j((1 - \delta)x_j^{\mathcal{F}} + \delta x_j^{\mathcal{UC}} - e_j^{\mathcal{UC}}) \quad (28)$$

We derive and will subsequently make use of the following lemmas:

**Lemma 1.** Under Conditions 3 and 4,  $e_i^{\mathcal{UC}} = e_j^{\mathcal{UC}}$ .

*Proof.* This follows from inspection of Equation 13, and invoking Conditions 3 and 4.  $\square$

**Lemma 2.** Under Condition 1,  $x_i^{\mathcal{F}} = x_j^{\mathcal{F}}$  and  $x_i^{\mathcal{UC}} = x_j^{\mathcal{UC}}$ .

*Proof.* Equation 1 implies that  $x_i = f_1(e_1)D_{1i} + f_2(e_2)D_{2i} + \dots + f_N(e_N)D_{Ni}$  and  $x_j = f_1(e_1)D_{1j} + f_2(e_2)D_{2j} + \dots + f_N(e_N)D_{Nj}$ . For any set of escapements  $e_1, e_2, \dots, e_N$ , these are equal by Condition 1.  $\square$

These facts give rise to the following propositions regarding the characteristics of patches that determine the dividend required to induce voluntary participation.

**Proposition 5.** Suppose that Conditions 1, 3, and 4 hold, and  $b_i > b_j$ , then  $\hat{\gamma}_i > \hat{\gamma}_j$ .

*Proof.* Under the assumed Conditions, Lemmas 1 and 2 hold, so the only difference in the numerator is  $b_i$  and  $b_j$ . The result  $\hat{\gamma}_i > \hat{\gamma}_j$  follows trivially.  $\square$

**Proposition 6.** *Suppose that Conditions 1, 2 and 3 hold, and  $D_{ii} > D_{jj}$ , then  $\hat{\gamma}_i < \hat{\gamma}_j$ .*

*Proof.* By Lemma 2 and Condition 2, comparing the numerator requires only comparing  $-e_i^{\mathcal{UC}} \leq -e_j^{\mathcal{UC}}$ . From Equation 13, and invoking Condition 3 and the assumption about retention,  $e_j^{\mathcal{UC}} < e_i^{\mathcal{UC}}$ , and therefore,  $\hat{\gamma}_i < \hat{\gamma}_j$ .  $\square$

**Proposition 7.** *Suppose that Conditions 1, 2, and 4 hold, and  $f'_i(\bar{e}) > f'_j(\bar{e}) \forall \bar{e}$ , then  $\hat{\gamma}_i < \hat{\gamma}_j$ .*

*Proof.* By Lemma 2 and Condition 2, only need to compare  $-e_i^{\mathcal{UC}} \leq -e_j^{\mathcal{UC}}$ . From Equation 13, and invoking Condition 4 and the assumption about growth,  $e_j^{\mathcal{UC}} < e_i^{\mathcal{UC}}$ , and therefore,  $\hat{\gamma}_i < \hat{\gamma}_j$ .  $\square$

The intuition underlying Proposition 5 is straightforward: patches with a higher price or lower marginal cost of harvest (higher  $b_i$ ) require a larger dividend  $\gamma_i$  of total fishery profits to discourage defection. Proposition 6 hinges on the fact that patches with less self-retention (smaller  $D_{ii}$ ) will harvest to a lower level of escapement when defecting, making initial defection more profitable relative to patches with higher self-retention. Proposition 7 reveals a counterintuitive result on the minimum dividend required to entice patch owners into the unitization scheme. In contrast to Proposition 5 which found that more economically productive patches require larger dividends, Proposition 7 shows that more biologically productive patches (higher  $f'_i(\bar{e}) \forall \bar{e}$ ) require smaller dividends to encourage participation. This result follows from the fact that patches with higher productivity will choose higher levels of escapement when defecting, decreasing the benefit of initial defection and thus requiring a smaller dividend to entice cooperation.

In order for the dividend structure described by Equation 27 to be feasible, the individual dividends must sum to less than unity:

$$\frac{\sum_{i=1}^N b_i((1-\delta)x_i^{\mathcal{F}} + \delta x_i^{\mathcal{MC}} - e_i^{\mathcal{MC}})}{\sum_{j=1}^N b_j(x_j^{\mathcal{F}} - e_j^{\mathcal{F}})} \leq 1. \quad (29)$$

This leads to our next proposition regarding the efficiency of unitization under voluntary participation:

**Proposition 8.** *Under Assumption 1, there exists a discount factor  $\tilde{\delta} < 1$  such that for any  $\delta \geq \tilde{\delta}$ , full unitization with endogenous participation is supportable, and first-best, economically efficient harvest can be achieved.*

*Proof.* The denominator of Equation 29 is simply the first-best value of the fishery in steady state. If  $\delta = 1$ , the numerator is equal to the value of the fishery in the absence of unitization, and as this is less than the first-best value of the fishery, the ratio in Equation 29 is strictly less than one. On the other hand, if  $\delta = 0$ , the numerator is strictly greater than the denominator, as  $e_i^{\mathcal{MC}} < e_i^{\mathcal{F}}$  and the ratio is strictly greater than one. Thus, by the intermediate value theorem, there exists some  $0 < \tilde{\delta} < 1$  such that the ratio in Equation 29 is equal to one. For  $\delta \geq \tilde{\delta}$ , the dividend given by Equation 27 is feasible and full participation with full unitization is supportable, yielding first-best outcomes per proposition 4.  $\square$

This finalizes our main result: by generalizing the concept of unitization, we have shown that fully efficient exploitation can be voluntarily achieved by completely self-interested patch owners and that this result does not require infinite patience.



#### 4.2.1 Alternative strategy considerations

Our result relies on Nash reversion as a means to punish defectors. It may be worth considering punishment strategies other than Nash reversion. One shortcoming of Nash reversion is that it is not renegotiation proof (Van Damme 1989) and punishers may have an incentive to ‘let bygones be bygones’ and allow a defector back into the cooperative and resume profit sharing. An extension that considers the potential of renegotiation proof strategies (such as Bhat and Huffaker (2007) and Cave (1987)) or more sophisticated punishment strategies (as in Tarui et al. (2008)) in unitized spatially connected renewable resources may prove insightful.

#### 4.2.2 Practical considerations

In the above analysis, the dividend was allowed to vary across patches. However, as a practical matter, such varying shares may be difficult for owners to agree upon. Fish harvested in patch  $i$  may come from larvae produced by stock in patch  $j$ , which may make agreement on unit shares difficult to come by. Wiggins and Libecap (1985) and Libecap and Wiggins (1985) detail contracting issues in oil unitization, emphasizing the difficulties of unit share agreement as a result of imperfect information. The biological systems underlying renewable resources may make the process of agreeing on unit shares even more contentious.<sup>18</sup>

## 5 Conclusions

Spatial connectivity of renewable resources induces a spatial externality in extraction. For this reason, spatial property rights alone are insufficient to solve the commons problem. We

generalize the notion of unitization, developed to coordinate extraction of common oil and gas fields, to spatially connected renewable resources. This coordination mechanism is framed within a spatial bioeconomic model with a patchy “metapopulation.” Patch owners then compete in a dynamic game because owner  $i$ ’s harvest affects all other owners in subsequent periods. Our main result is that unitization can serve to coordinate spatial property rights owners. If designed properly, first-best harvest can be achieved, even in cases when the resource would be completely destroyed in the absence of unitization. The unitization scheme relies on two instruments: an owner-specific *contribution* (the fraction of profits an owner must yield to the common pool) and an owner-specific *dividend* (the fraction of the pool redistributed to the owner). By allowing the unitization scheme to vary by participant (e.g., as a function of patch-specific biological productivity or economic returns), the mechanism can induce voluntary participation by all spatial property rights owners.

The special structure of our difference game allows us to obtain sharp analytical results, but the analysis is not without caveats. There is an implicit assumption throughout the paper that the sole owner would achieve socially efficient harvest. While common in the bioeconomics literature, this is somewhat of a heroic assumption, but it does reduce the complexity of our problem. Incorporating other features such as ecological benefits or varying discount rates into the spatial bioeconomic model presented here may prove interesting.<sup>19</sup> Considering harvest incentives under a more general economic model may also be fruitful, as would considering the case of spatial reserves under spatial property rights. For example, might a patch owner find it optimal to pay another patch owner to completely shutdown harvest in her patch (Costello and Kaffine 2010)? While we have focused on spatial property rights over renewable resources, this unitization scheme might apply more generally.

For example, if property rights are assigned on the basis of allowable fish catch (individual transferable quotas (ITQs)), owners may benefit from coordination on harvest via a unitization mechanism. Owners of ITQ in the crab fishery in New Zealand coordinate via a mechanism similar to this where owners contribute quota share to a cooperative (“Crabco”) and profits are redistributed differentially to participants at the end of the season (Soboil and Craig 2008).

While the unitization scheme presented here yields first-best outcomes under mandatory participation and can yield first-best outcomes under voluntary participation, practical considerations may constrain implementation, and unitization structures with less than full participation and less than full unitization may maximize the value of spatial renewable resource extraction.

## Notes

<sup>1</sup>For example, the 2007 reauthorization of the Magnuson-Stevens Fishery Conservation and Management Act allows for various tradeable property schemes. A recent study (Costello, Gaines, and Lynham 2008) suggests that ITQs have been successful in slowing fishery collapse.

<sup>2</sup>See Hannesson (2004) for an excellent discussion of attempts to privatize the ocean with ITQ's and spatial rights. Examples of formalized spatial property right systems include TURFs in Chile, community cooperatives in Japan and Mexico, and the 200 mile Exclusive Economic Zones (EEZs) established by the Law of the Sea; a famous informal example occurs in the Maine lobster fishery where harbor 'gangs' exercise de facto spatial rights (Acheson 1988).

<sup>3</sup>For example, for spiny lobster, substantial losses (relative to optimal management) were still found even with TURF alongshore widths of 100km, principally due to larval transport by ocean currents and not because of adult movement. This stands in sharp contrast to the size of existing TURFs in Chile and Japan (discussed extensively in Cancino, Uchida, and Wilen (2007)) which may extend less than 1 km alongshore.

<sup>4</sup>The problem of unitization and contracting between users of a nonrenewable common pool resource has been studied in depth for the oil industry in a series of papers by Libecap and Wiggins (Libecap and Wiggins (1984), Wiggins and Libecap (1985), Libecap and Wiggins (1985)). They examine the contracting success, and frequently the failure, of private firms drilling the same common oil field. They generally find that heterogeneity plays a key role in thwarting the success of contracts to lessen rent dissipation and overproduction.

<sup>5</sup>We focus here on examples of profit sharing *across* spatial units of ownership, as opposed to profit sharing *within* spatially defined units of ownership. Within a spatially-defined unit of ownership (i.e. a TURF), profit-sharing can be used to induce cooperation between multiple harvesters. For example, profits are pooled among cooperative members within the walleye pollack fishery of the Nishi region of Japan and redistributed to TURF members (Uchida and Watanobe 2008). The loco fisheries in Chile’s TURF system also use partial revenue pooling mechanisms within a TURF to mitigate race-to-fish incentives (Uchida and Wilen 2005). Within the deep sea crab fishery of New Zealand, quota owners have “invested” their quota shares within Crabco, the sole company involved in the crab fishing operation. Profits are returned to investors based on the share invested in the company (Mincher 2008).

<sup>6</sup>The cooperative was disbanded by a court ruling that held that the cooperative was illegal on the grounds that it was illegal for a fisherman to profit from a right to fish without undertaking any actual fishing activity.

<sup>7</sup>This feature is present at some life-history stage for many commercially viable species.

<sup>8</sup>See Costello and Kaffine (2008) for a discussion of how uncertain tenure affects harvest incentives for renewable resources.

<sup>9</sup>The parameter  $D_{ji}$  captures larval dispersal across space and will be species-specific.

<sup>10</sup>We leave the exploration of decentralized spatial bioeconomic models with stock effects to future work.

<sup>11</sup>State independence of the control variable also implies that the open loop and feedback control rules are identical. This result was established, and coined *state separability* for continuous time models by Dockner, Geichtinger, and Jorgensen (1985).

<sup>12</sup>We make a few notes about Proposition 1 when Assumption 1 does not hold. If  $f'_i(0) \leq$

$\frac{1}{\delta D_{ii}}$ , the optimal escapement is  $e_{it}^{UC} = 0$  by the non-negativity constraint on  $e_{it}$ . On the other hand, if  $D_{ij} = 0$  for  $i \neq j$ , the optimal escapement is equivalent to the economically efficient sole owner's. Without dispersal, each owner controls a self-contained fiefdom and property rights can be assigned confidently without concern for coordination or cooperation; efficient harvest will occur for owners solely interested in their own profits. However, as noted in the introduction, larval dispersal in fisheries is typically larger than practical spatial property right assignments to individual users.

<sup>13</sup>A small example is in Baja California where the 9 spatial property rights owners in the cooperative “Fedecoop” would require 36 separate annual side payments. A large example is in Chile where 453 permanent TURFs exist for harvesting an abalone-like snail, which could require  $> 100,000$  side payments.

<sup>14</sup>Consistent with our assumption that profits (rather than, e.g., revenues) are shared, Libecap and Smith (1999) argue that production and cost shares must coincide to induce efficiency in unitization contracts for oil and gas extraction.

<sup>15</sup>In practice, the redistribution may not be entirely pecuniary. For example, in Chile and Japan profit sharing partly pays for science, monitoring, and enforcement. For oil and gas, coordination is undertaken by a “unit operator” a concept that has been adopted (in principle, not in name) in some fisheries, e.g. the Chignik Salmon Cooperative (Deacon, Parker, and Costello 2008).

<sup>16</sup>Heintzelman, Salant, and Schott (2009) consider a similar profit sharing solution for homogenous agents harvesting a common property resource and find that coordinating can improve economic outcomes.

<sup>17</sup>Note that equilibrium profile of escapements under the three cases we consider (sole

owner, uncoordinated owners, and unitization) are all independent of the state, and are thus constant over time. We henceforth suppress time subscripts for ease of exposition.

<sup>18</sup>Libecap and Wiggins (1984) argue that the difficulties of agreeing on a complete unitization contract led many oil fields to adopt prorationing, which created some margins for rent dissipation, but was easier to reach agreement on.

<sup>19</sup>Clark and Munro (1980) consider the case of varying discount factor when the sole owner deviates from the social discount factor. They find that corrective taxes may be necessary to ensure economically efficient behavior.

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