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# Modeling the Impact of Warming in Climate Change Economics

Robert S. Pindyck

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## 2.1 Introduction

Any economic analyses of climate change policy must include a model of damages, that is, a relationship that translates changes in temperature (and possibly changes in precipitation and other climate-related variables) to economic losses. Economic losses will, of course, include losses of gross domestic product (GDP) and consumption that might result from reduced agricultural productivity or from dislocations resulting from higher sea levels but also the dollar-equivalent costs of possible climate-related increases in morbidity, mortality, and social disruption. Because of the lack of data and the considerable uncertainties involved, modeling damages is probably the most difficult aspect of analyzing climate change policy. There are uncertainties in other aspects of climate change policy—for example, how rapidly greenhouse gases (GHGs) will accumulate in the atmosphere absent an abatement policy, to what extent and how rapidly temperature will increase, and the current and future costs of abatement—but damages from climate change is the area we understand the least. It must be modeled, but it is important to understand the uncertainties involved and their policy implications.

Most quantitative economic studies of climate change policy utilize a “damage function” that relates temperature change directly to the levels

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of real GDP and consumption. Future consumption, for example, is taken to be the product of a loss function and “but-for consumption,” that is, consumption in the absence of any warming. With no warming, the loss function is equal to 1, but as the temperature increases, the value of the loss function decreases. This approach is reasonably simple in that any projected path for temperature can be directly translated into an equivalent path for consumption. In other words, consumption at time  $t$  depends on temperature at time  $t$ . Given a social utility function that “values” consumption, one can then evaluate a particular policy (assuming we know its costs and can project its effects on GHG concentrations and temperature).

In a recent paper (Pindyck 2009), I have argued that on both theoretical and empirical grounds, the economic impact of warming should be modeled as a relationship between temperature change and the *growth rate* of GDP as opposed to the level of GDP. This means that warming can have a permanent impact on future GDP and consumption. It makes the analysis somewhat more complicated, however, because consumption at some future date depends not simply on the temperature at that date, but instead on the entire path of temperature and, thus, the path of the growth rate of consumption, up to that date. The issue I address in this chapter is the extent to which these two different approaches to modeling damages—temperature affecting consumption directly versus temperature affecting the growth rate of consumption—differ in terms of their policy implications.

This issue must be addressed in the context of uncertainty, which is at the heart of climate change policy. It is difficult to justify the immediate adoption of a stringent abatement policy based on an economic analysis that focuses on “most likely” scenarios for increases in temperature and economic impacts and uses consensus estimates of discount rates and other relevant parameters.<sup>1</sup> But one could ask whether a stringent policy might be justified by a cost-benefit analysis that accounts for a full distribution of possible outcomes.

In Pindyck (2009), I showed how probability distributions for temperature change and economic impact could be inferred from climate science and economic impact studies and incorporated in the analysis of climate change policy. The framework I used, which I use again here, is based on a simple measure of “willingness to pay” (WTP): the fraction of consumption  $w^*(\tau)$  that society would be willing to sacrifice, now and throughout the future, to ensure that any increase in temperature at a specific horizon  $H$ ,  $\Delta T_H$ , is limited to  $\tau$ . It is important to understand the limitations of this approach. Whether the reduction in consumption corresponding to some  $w^*(\tau)$  is *sufficient* to limit warming to  $\tau$  is a separate question that is not addressed; in effect, WTP applies to the “demand” side of policy analysis.

1. *The Stern Review* (Stern 2007) argues for a stringent abatement policy, but as Nordhaus (2007), Weitzman (2007), Mendelsohn (2008), and others point out, it makes assumptions about temperature change, economic impact, abatement costs, and discount rates that are outside the consensus range.

The advantage of this approach, however, is that there is no need to project GHG emissions and atmospheric concentrations or estimate abatement costs. Instead the focus is on uncertainties over temperature change and its economic impact.

My earlier paper was based on what I called the current “state of knowledge” regarding global warming and its impact. I used information on the distributions for temperature change from scientific studies assembled by the Intergovernmental Panel on Climate Change (IPCC; 2007a,b,c) and information about economic impacts from recent integrated assessment models (IAMs) to fit displaced gamma distributions for these variables. But unlike existing IAMs, I modeled economic impact as a relationship between temperature change and the growth rate of consumption as opposed to its level. I examined whether “reasonable” values for the remaining parameters (e.g., the starting growth rate and the index of risk aversion) can yield values of  $w^*(\tau)$  well above 3 percent for small values of  $\tau$ , which might support stringent abatement. I also used a counterfactual—and pessimistic—scenario for temperature change: under business as usual (BAU), the atmospheric GHG concentration immediately increases to twice its pre-Industrial level, which leads to an (uncertain) increase in temperature at the horizon  $H$ , and then (from feedback effects or further emissions) a gradual further doubling of that temperature increase.

In this chapter, I use the same displaced gamma distributions for temperature change and economic impact, but I compare two alternative damage models—a direct impact of temperature change on consumption versus a growth rate impact. I calibrate and “match” the two models by matching estimates of GDP/temperature change pairs from the group of IAMs at a specific horizon. I then calculate and compare WTPs for both models based on expected discounted utility, using a constant relative risk aversion (CRRA) utility function.

I find that for either damage model, the resulting estimates of  $w^*(\tau)$  are generally below 2 percent or 3 percent, even for  $\tau$  around 2 or 3°C. This is because there is limited weight in the tails of the calibrated distributions for  $\Delta T$  and its impact. Larger estimates of WTP result for particular combinations of parameter values (e.g., an index of risk aversion close to 1 and a low initial GDP growth rate), but overall, the results are consistent with moderate abatement. A direct impact generally yields a larger WTP than a growth rate impact, and the sign and extent of the difference varies with changes in parameter values. Overall, there are no substantial differences between the two models in terms of policy implications.<sup>2</sup>

2. As with my earlier study, I ignore the implications of the opposing irreversibilities inherent in climate change policy and the value of waiting for more information. Immediate action reduces the largely irreversible build up of GHGs in the atmosphere, but waiting avoids an irreversible investment in abatement capital that might turn out to be at least partly unnecessary, and the net effect of these irreversibilities is unclear. For a discussion of the interaction of uncertainty and irreversibility, see Pindyck (2007).

The next section discusses the probability distribution and dynamic trajectory for temperature change. Section 2.3 discusses the two alternative ways of modeling the economic impact of higher temperatures and the corresponding probability distributions that capture uncertainty over that impact. Section 2.4 explains the calculation of willingness to pay. Numerical results are presented and discussed in sections 2.5 and 2.6, and section 2.7 concludes.

## 2.2 Temperature

According to the IPCC (2007c), under BAU, that is, no abatement policy, growing GHG emissions would likely lead to a doubling of the atmospheric CO<sub>2</sub>e concentration relative to the pre-Industrial level by the end of this century. That, in turn, would cause an increase in global mean temperature that would “most likely” range between 1.0°C to 4.5°C, with an expected value of 2.5° to 3.0°C. The IPCC report indicates that this range, derived from a “summary” of the results of twenty-two scientific studies the IPCC surveyed, represents a roughly 66 to 90 percent confidence interval, that is, there is a 5 to 17 percent probability of a temperature increase above 4.5°C.

The twenty-two studies also provide rough estimates of increases in temperature at the outer tail of the distribution. In summarizing them, the IPCC translated the implied outcome distributions into a standardized form that makes the studies comparable and created graphs showing multiple outcome distributions implied by groups of studies. Those distributions suggest that there is a 5 percent probability that a doubling of the CO<sub>2</sub>e concentration relative to the pre-Industrial level would lead to a global mean temperature increase of 7°C or more and a 1 percent probability that it would lead to a temperature increase of 10°C or more. I fit a three-parameter displaced gamma distribution for  $\Delta T$  to these 5 percent and 1 percent points and to a mean temperature change of 3.0°C. This distribution conforms with the distributions summarized by the IPCC. Finally, I assume (consistent with the IPCC’s focus on temperature change at the end of this century) that the fitted distribution for  $\Delta T$  applies to a 100-year horizon  $H$ .

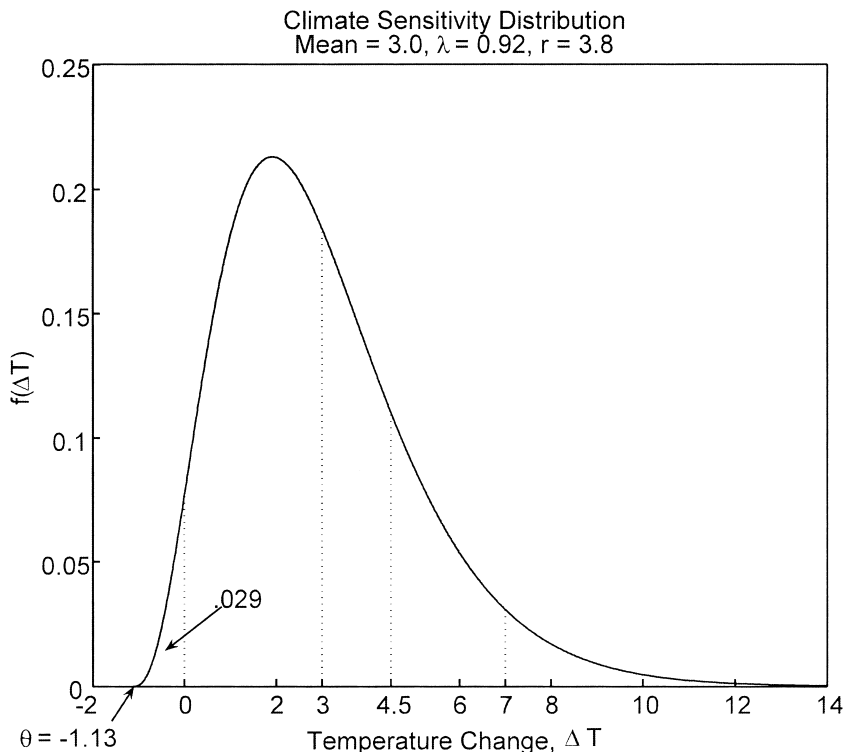
### 2.2.1 Displaced Gamma Distribution

The displaced gamma distribution is given by

$$(1) \quad f(x; r, \lambda, \theta) = \frac{\lambda^r}{\Gamma(r)} (x - \theta)^{r-1} e^{-\lambda(x-\theta)}, \quad x \geq \theta,$$

where  $\Gamma(r) = \int_0^\infty s^{r-1} e^{-s} ds$  is the gamma function. The moment generating function for equation (1) is

$$M_x(t) = E(e^{tx}) = \left( \frac{\lambda}{\lambda - t} \right)^r e^{t\theta}.$$



**Fig. 2.1** Distribution for temperature change

Thus the mean, variance and skewness (around the mean) are  $E(x) = r/\lambda + \theta$ ,  $V(x) = r/\lambda^2$ , and  $S(x) = 2r/\lambda^3$ , respectively.

Fitting  $f(x; r, \lambda, \theta)$  to a mean of 3°C, and the 5 percent and 1 percent points at 7°C and 10°C, respectively, yields  $r = 3.8$ ,  $\lambda = 0.92$ , and  $\theta = -1.13$ . The distribution is shown in figure 2.1. It has a variance and skewness around the mean of 4.49 and 9.76, respectively. Note that this distribution implies that there is a small (2.9 percent) probability that a doubling of the CO<sub>2</sub>e concentration will lead to a *reduction* in mean temperature, consistent with several of the scientific studies. The distribution also implies that the probability of a temperature increase of 4.5°C or greater is 21 percent.

### 2.2.2 Trajectory for $\Delta T_t$

Recall that this fitted distribution for  $\Delta T$  pertains to the 100-year horizon  $H$ . To allow for possible feedback effects or further emissions, I assume that  $\Delta T_t \rightarrow 2\Delta T_H$  as  $t$  gets large. As summarized in Weitzman (2009), the simplest dynamic model relating  $\Delta T_t$  to the GHG concentration  $G_t$  is the differential equation

$$(2) \quad \frac{d\Delta T}{dt} = m_1 \left[ \frac{\ln(G_t/G_0)}{\ln 2} - m_2 \Delta T_t \right].$$

Making the conservative (in the sense that it would lead to a higher WTP) assumption that  $G_t$  immediately (i.e., at  $t = 0$ ) doubles to  $2G_0$ ,  $\Delta T_t = \Delta T_H$  at  $t = H$ , and  $\Delta T_t \rightarrow 2\Delta T_H$  as  $t \rightarrow \infty$ , implies that  $\Delta T_t$  follows the trajectory

$$(3) \quad \Delta T_t = 2\Delta T_H \left[ 1 - \left( \frac{1}{2} \right)^{t/H} \right].$$

Thus if  $\Delta T_H = 5^\circ\text{C}$ ,  $\Delta T_t$  reaches  $2.93^\circ\text{C}$  after 50 years,  $5^\circ\text{C}$  after 100 years,  $7.5^\circ\text{C}$  after 200 years, and then gradually approaches  $10^\circ\text{C}$ .

This is illustrated in figure 2.2, which shows a trajectory for  $\Delta T$  when it is unconstrained (and  $\Delta T_H$  happens to equal  $5^\circ\text{C}$ ) and when it is constrained so that  $\Delta T_H \leq \tau = 3^\circ\text{C}$ . Note that even when constrained,  $\Delta T_H$  is a random variable and (unless  $\tau = 0$ ) will be less than  $\tau$  with probability 1; in figure 2.2, it happens to be  $2.5^\circ\text{C}$ . If  $\tau = 0$ , then  $\Delta T = 0$  for all  $t$ .

### 2.3 Impact of Warming

Most economic studies of climate change assume that  $\Delta T$  has a *direct impact* on GDP (or consumption), modeled via a “loss function”  $L(\Delta T)$ , with  $L(0) = 1$  and  $L' < 0$ . Thus GDP at some horizon  $H$  is  $L(\Delta T_H)\text{GDP}_H$ , where  $\text{GDP}_H$  is but-for GDP in the absence of warming. This “direct impact” approach has been used in all of the integrated assessment models that I am aware of. However, there are reasons to expect warming to affect the *growth rate* of GDP as opposed to the level. At issue is how these two alternative approaches to modeling the impact of warming—direct versus growth rate—differ in their implications for estimates of willingness to pay to limit warming.

#### 2.3.1 Direct Impact

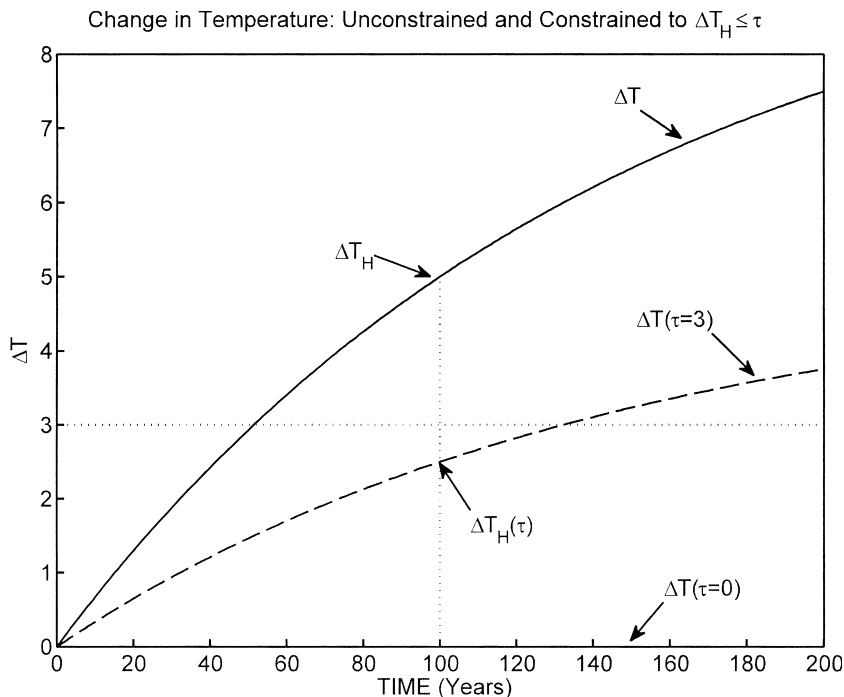
The most widely used loss function has been the inverse quadratic. For example, the recent version of the Nordhaus (2008) Dynamic Integrated model of Climate and the Economy (DICE) uses the following loss function:

$$L = \frac{1}{[1 + \pi_1 \Delta T + \pi_2 (\Delta T)^2]}.$$

Weitzman (2008) introduced the exponential loss function, which is very similar to the inverse quadratic for small values of  $\Delta T$  but allows for greater losses when  $\Delta T$  is large:

$$(4) \quad L(\Delta T) = \exp[-\beta(\Delta T)^2].$$

I will use this loss function of equation (4) when calculating WTP under the direct impact assumption.



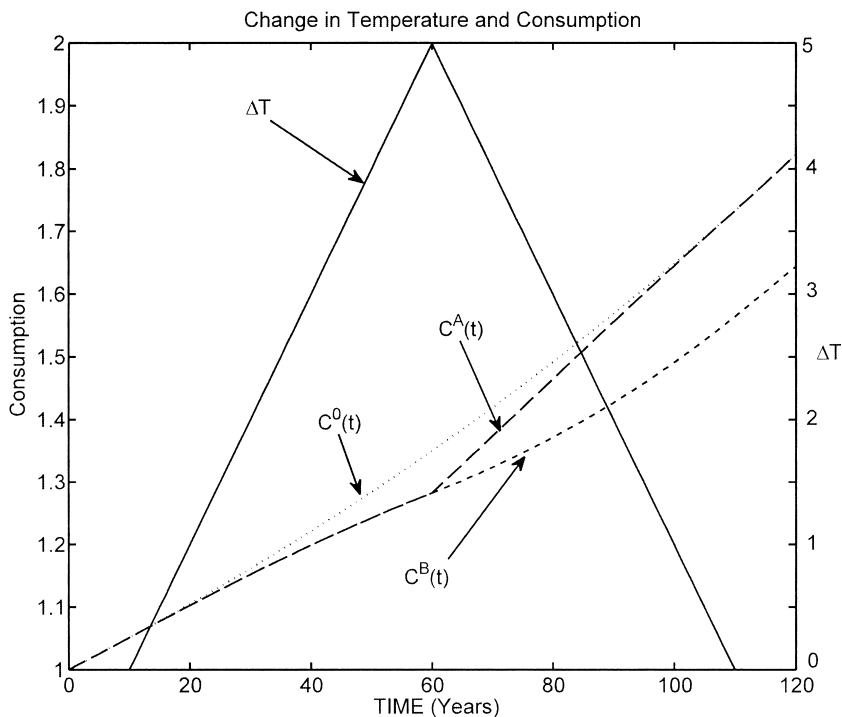
**Fig. 2.2** Temperature change: Unconstrained and constrained so  $\Delta T_H \leq \tau$

To introduce uncertainty over the impact of warming, I will treat the parameter  $\beta$  as a random variable that, like temperature change, can be described by a 3-parameter displaced gamma distribution. Although the IPCC does not provide standardized distributions for lost GDP corresponding to any particular  $\Delta T$  as it does for climate sensitivity, it does survey the results of several IAMS. As discussed in the following, I use the information from the IPCC along with other studies to infer means and confidence intervals for  $\beta$ .

### 2.3.2 Growth Rate Impact

There are three reasons to expect warming to affect the growth rate of GDP as opposed to the level. First, some effects of warming are likely to be permanent: for example, destruction of ecosystems from erosion and flooding, extinction of species, and deaths from health effects and weather extremes. If warming affected the level of GDP directly, for example, as per equation (4), it would imply that if temperatures rise but later fall, for example, because of stringent abatement or geoengineering, GDP could return to its but-for path with no permanent loss. This is not the case, however, if  $\Delta T$  affects the growth rate of GDP.





**Fig. 2.3 Example of economic impact of temperature change**

*Note:* Temperature increases by  $5^{\circ}\text{C}$  over fifty years and then falls to original level over next fifty years.  $C^A$  is consumption when  $\Delta T$  reduces level,  $C^B$  is consumption when  $\Delta T$  reduces growth rate, and  $C^0$  is consumption with no temperature change.

Suppose, for example, that temperature increases by  $0.1^{\circ}\text{C}$  per year for fifty years and then decreases by  $0.1^{\circ}\text{C}$  per year for the next fifty years. Figure 2.3 compares two consumption trajectories:  $C_t^A$ , which corresponds to the loss function of equation (4), and  $C_t^B$ , which corresponds to the following growth rate loss function:

$$(5) \quad g_t = g_0 - \gamma \Delta T_t$$

The example assumes that without warming, consumption would grow at 0.5 percent per year—trajectory  $C_t^0$ —and both loss functions are calibrated so that at the maximum  $\Delta T$  of  $5^{\circ}\text{C}$ ,  $C^A = C^B = .95C^0$ . Note that as  $\Delta T$  falls to zero,  $C_t^A$  reverts to  $C_t^0$ , but  $C_t^B$  remains permanently below  $C_t^0$ .

Second, resources needed to counter the impact of higher temperatures would reduce those available for research and development (R&D) and capital investment, reducing growth. Adaptation to rising temperatures is equivalent to the cost of increasingly strict emission standards, which, as Stokey (1998) has shown with an endogenous growth model, reduces the rate of return on capital and lowers the growth rate. As a simple example,

suppose total capital  $K = K_p + K_a(T)$ , with  $K'_a(T) > 0$ , where  $K_p$  is directly productive capital and  $K_a(T)$  is capital needed for adaptation to the temperature  $T$  (e.g., stronger retaining walls and pumps to counter flooding, new infrastructure and housing to support migration, more air conditioning and insulation, etc.). If all capital depreciates at rate  $\delta_K$ ,  $\dot{K} = \dot{K}_p + \dot{K}_a = I - \delta_K K - K'_a(T)\dot{T}$  so that the rate of growth of  $K_p$  is reduced, and, thus, the rate of growth of output is reduced.

Third, there is empirical support for a growth rate effect. Using historical data on temperatures and precipitation over the past fifty years for a panel of 136 countries, Dell, Jones, and Olken (2008) have shown that higher temperatures reduce GDP growth rates but not levels. The impact they estimate is large—a decrease of 1.1 percentage points of growth for each 1°C rise in temperature—but significant only for poorer countries.<sup>3</sup>

To calculate WTP when  $\Delta T$  affects the growth rate of GDP, I assume that in the absence of warming, real GDP and consumption would grow at a constant rate  $g_0$ , but warming will reduce this rate according to equation (5). This simple linear relation was estimated by Dell, Jones, and Olken (2008), and can be viewed as at least a first approximation to a more complex loss function. I introduce uncertainty by making the parameter  $\gamma$ , like  $\beta$ , a random variable drawn from a displaced gamma distribution.

### 2.3.3 Distributions for $\beta$ and $\gamma$

To compare the effects of a direct versus growth rate impact on estimates of WTP, we need to fit and “match” the distributions for  $\beta$  and  $\gamma$ . This is done as follows.

Using information from a number of IAMs, I fit the three parameters in a displaced gamma distribution for  $\beta$  in the exponential-quadratic loss function of equation (4). I then translate this into an equivalent distribution for  $\gamma$  using the trajectory for GDP and consumption implied by equation (5) for a temperature change-impact combination projected to occur at horizon  $H$ . From equations (3) and (5), the growth rate is  $g_t = g_0 - 2\gamma\Delta T_H [1 - (1/2)^{t/H}]$ . Normalizing initial consumption at 1, this implies

$$(6) \quad C_t = e^{\int_0^t g(s) ds} = \exp\left[-\frac{2\gamma H \Delta T_H}{\ln(1/2)} + (g_0 - 2\gamma\Delta T_H)t + \frac{2\gamma H \Delta T_H}{\ln(1/2)}(1/2)^{t/H}\right].$$

Thus,  $\gamma$  is obtained from  $\beta$  by equating the expressions for  $C_H$  implied by equations (4) and (6):

3. “Poor” means below-median purchasing power parity (PPP)-adjusted per capita GDP. Using World Bank data for 209 countries, “poor” by this definition accounts for 26.9 percent of 2006 world GDP, which implies a roughly 0.3 percentage point reduction in world GDP growth for each 1°C rise in temperature. In a follow-on paper, Dell, Jones, and Olken (2009) estimate a model that allows for adaptation effects so that the long-run impact of warming is smaller than the short-run impact. They find a long-run decrease of 0.51 percentage points of growth for each 1°C rise in temperature, but again only for poorer countries.

$$(7) \quad \exp\left[-\frac{2\gamma H\Delta T_H}{\ln(1/2)} + (g_0 - 2\gamma\Delta T_H)H + \frac{\gamma H\Delta T_H}{\ln(1/2)}\right] = \exp[g_0 H - \beta(\Delta T_H)^2]$$

so that  $\beta$  and  $\gamma$  have the simple linear relationship

$$(8) \quad \gamma = \frac{1.79\beta\Delta T_H}{H}.$$

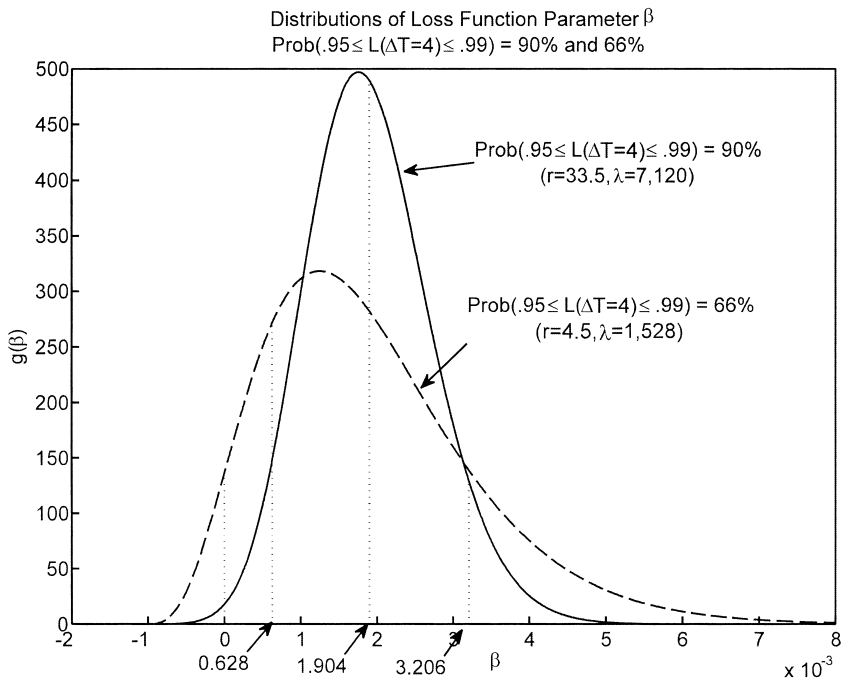
#### *Distribution for $\beta$*

To fit a displaced gamma distribution for  $\beta$ , I utilize the IPCC's survey of several IAMs. This information from the IPCC, along with other studies, allow me to infer means and confidence intervals for  $\beta$ . These IAMs yield a rough consensus regarding possible economic impacts: for temperature increases up to 4°C, the "most likely" impact is from 1 percent to at most 5 percent of GDP. (Of course, this consensus might arise from the use of similar ad hoc damage functions in various IAMs.) Of interest is the outer tail of the distribution for this impact. There is some chance that a temperature increase of 3°C or 4°C would have a much larger impact, and we want to know how that affects WTP.

Based on its survey of impact estimates from four IAMs, the IPCC (2007a, 17) concludes that "global mean losses could be 1–5% of GDP for 4°C of warming."<sup>4</sup> In addition, Dietz and Stern (2008) provide a graphical summary of damage estimates from several IAMs, which yield a range of 0.5 percent to 2 percent of lost GDP for  $\Delta T = 3^\circ\text{C}$  and 1 percent to 8 percent of lost GDP for  $\Delta T = 5^\circ\text{C}$ . I treat these ranges as "most likely" outcomes and use the IPCC's definition of "most likely" to mean a 66 to 90 percent confidence interval. Using the IPCC range and, to be conservative, assuming it applies to a 66 percent confidence interval, I take the mean loss for  $\Delta T = 4^\circ\text{C}$  to be 3 percent of GDP and the 17 percent and 83 percent confidence points to be 1 percent of GDP and 5 percent of GDP, respectively. We can then use equation (4) to get the mean, 17 percent, and 83 percent values for  $\beta$ , which I denote by  $\bar{\beta}$ ,  $\beta_1$  and  $\beta_2$ , respectively. For example,  $.97 = e^{-\bar{\beta}(4)^2}$  so that  $\bar{\beta} = .00190$ . Likewise,  $\beta_1 = .000628$  and  $\beta_2 = .00321$ . Fitting a displaced gamma distribution to these numbers yields  $r = 4.5$ ;  $\lambda = 1,528$ ; and  $\theta = \bar{\beta} - r/\lambda = -.00105$ .

Figure 2.4 shows the fitted distribution for  $\beta$ . Also shown is the fitted distribution when "most likely" is taken to mean a 90 percent confidence interval so that  $\beta_1$  and  $\beta_2$  instead apply to the 5 and 95 percent confidence points.

4. The IAMs surveyed by the IPCC include Hope (2006), Mendelsohn et al. (1998), Nordhaus and Boyer (2000), and Tol (2002). For a recent overview of economic impact studies, see Tol (2009).



**Fig. 2.4** Distributions for loss function parameter  $\beta$

*Distribution for  $\gamma$*

The mean, 17 percent, and 83 percent values for  $\beta$  applied to a  $\Delta T_H = 4^\circ\text{C}$  at a horizon  $H = 100$  years, so from equation (8),  $\gamma = .0716\beta$ . Thus, the mean, 17 percent, and 83 percent values for  $\gamma$  are, respectively,  $\bar{\gamma} = .0001360$ ,  $\gamma_1 = .0000450$ , and  $\gamma_2 = .0002298$ . Now suppose  $f(x; r, \lambda, \theta)$  is the displaced gamma distribution for  $x$ , and we want the distribution  $f(y; r_1, \lambda_1, \theta_1)$  for  $y = ax$ . We can make use of the fact that the expectation, variance, and skewness of  $x$  and of  $y$  are related as follows:  $E(y) = aE(x) = ar/\lambda + a\theta$ ,  $V(y) = a^2V(x) = a^2r/\lambda^2$ , and  $S(y) = a^3S(x) = 2a^3r/\lambda^3$ . This implies that  $\theta_1 = a\theta$ ,  $r_1 = r$ , and  $\lambda_1 = \lambda/a$ . Thus, the matched distribution for  $\gamma$  will be the same as that for  $\beta$ , except that  $\lambda_1 = 1528/.0716 = 21,340$  and  $\theta_1 = .0716(-.00105) = -.0000752$ . The distribution for  $\gamma$ , shown graphically in Pindyck (2009), will have the same shape as the distribution for  $\beta$  but a different scaling.

**2.4 Willingness to Pay**

Given the distributions for  $\Delta T$  and  $\beta$  or  $\gamma$ , I posit a CRRA social utility function:

$$(9) \quad U(C_t) = \frac{C_t^{1-\eta}}{(1-\eta)},$$

where  $\eta$  is the index of relative risk aversion (and  $1/\eta$  is the elasticity of intertemporal substitution). Social welfare is measured as the expected sum over time of discounted utility:

$$(10) \quad W = E \int_0^{\infty} U(C_t) e^{-\delta t} dt.$$

where  $\delta$  is the rate of time preference, that is, the rate at which utility is discounted. Note that this rate is different from the *consumption* discount rate, which in the Ramsey growth context would be  $R_t = \delta + \eta g_t$ . If  $\Delta T$  affects consumption directly, then  $R_t = \delta + \eta g_0$  and does not change over time. If  $\Delta T$  affects the growth rate of consumption, then  $R_t = \delta + \eta g_0 - 2\eta\gamma\Delta T_H[1 - (1/2)^{t/H}]$ , so  $R_t$  falls over time as  $\Delta T$  increases.<sup>5</sup>

For both the direct and growth rate impact models, I calculate the fraction of consumption—now and throughout the future—society would sacrifice to ensure that any increase in temperature at a specific horizon  $H$  is limited to an amount  $\tau$ . That fraction,  $w^*(\tau)$ , is the measure of willingness to pay.<sup>6</sup>

#### 2.4.1 WTP: Direct Impact

Using equation (3), if  $\Delta T_H$  and  $\beta$  were known, social welfare would be given by

$$(11) \quad W = \int_0^{\infty} U(C_t) e^{-\delta t} dt = \frac{1}{1-\eta} \int_0^{\infty} e^{\rho_0 - \rho_1 t - 2\rho_0(1/2)^{t/H} + \rho_0(1/2)^{2t/H}} dt,$$

where

$$(12) \quad \rho_0 = 4(\eta - 1)\beta(\Delta T_H)^2,$$

$$(13) \quad \rho_1 = (\eta - 1)g_0 + \delta.$$

Suppose society sacrifices a fraction  $w(\tau)$  of present and future consumption to keep  $\Delta T_H \leq \tau$ . With uncertainty over  $\Delta T_H$  and  $\beta$ , social welfare at  $t = 0$  is

$$(14) \quad W_1 = \frac{[1 - w(\tau)]^{1-\eta}}{1-\eta} E_{0,\tau} \int_0^{\infty} e^{\tilde{\rho}_0 - \tilde{\rho}_1 t - 2\tilde{\rho}_0(1/2)^{t/H} + \tilde{\rho}_0(1/2)^{2t/H}} dt,$$

where  $E_{0,\tau}$  denotes the expectation at  $t = 0$  over the distributions of  $\Delta T_H$  and  $\beta$  conditional on  $\Delta T_H \leq \tau$ . (Tildes are used to denote that  $\rho_0$  and  $\rho_1$  are

5. If  $2\eta\gamma\Delta T_H > \delta + \eta g_0$ ,  $R_t$  becomes negative as  $\Delta T$  grows. This is entirely consistent with the Ramsey growth model, as pointed out by Dasgupta, Mäler, and Barrett (1999).

6. The use of WTP as a welfare measure goes back at least to Debreu (1954), was used by Lucas (1987) to estimate the welfare cost of business cycles, and was used in the context of climate change (with  $\tau = 0$ ) by Heal and Kriström (2002) and Weitzman (2008).

functions of two random variables.) If no action is taken to limit warming, social welfare would be

$$(15) \quad W_2 = \frac{1}{1 - \eta} E_0 \int_0^\infty e^{\tilde{\rho}_0 t - \tilde{\rho}_1 t - 2\tilde{\rho}_0(1/2)^{t/H} + \tilde{\rho}_0(1/2)^{2t/H}} dt,$$

where  $E_0$  again denotes the expectation over  $\Delta T_H$  and  $\beta$  but now with  $\Delta T_H$  unconstrained. Willingness to pay to ensure that  $\Delta T_H \leq \tau$  is the value  $w^*(\tau)$  that equates  $W_1(\tau)$  and  $W_2$ .<sup>7</sup>

Given the distributions  $f(\Delta T)$  and  $g(\beta)$  for  $\Delta T_H$  and  $\beta$ , respectively, denote by  $M_\tau(t)$  and  $M_\infty(t)$  the time- $t$  expectations

$$(16) \quad M_\tau(t) = \frac{1}{F(\tau)} \int_{\theta_T \theta_\beta}^\tau e^{\tilde{\rho}_0 t - \tilde{\rho}_1 t - 2\tilde{\rho}_0(1/2)^{t/H} + \tilde{\rho}_0(1/2)^{2t/H}} f(\Delta T)g(\beta)d\Delta Td\beta$$

and

$$(17) \quad M_\infty(t) = \int_{\theta_T \theta_\beta}^\infty e^{\tilde{\rho}_0 t - \tilde{\rho}_1 t - 2\tilde{\rho}_0(1/2)^{t/H} + \tilde{\rho}_0(1/2)^{2t/H}} f(\Delta T)g(\gamma)d\Delta Td\gamma,$$

where  $\tilde{\rho}_0$  and  $\tilde{\rho}_1$  are given by equations (12) and (13),  $\theta_T$  and  $\theta_\beta$  are the lower limits on the distributions for  $\Delta T$  and  $\beta$ , and  $F(\tau) = \int_{\theta_T}^\tau f(\Delta T)d\Delta T$ . Thus,  $W_1(\tau)$  and  $W_2$  are

$$(18) \quad W_1(\tau) = \frac{[1 - w(\tau)]^{1-\eta}}{1 - \eta} \int_0^\infty M_\tau(t)dt \equiv \frac{[1 - w(\tau)]^{1-\eta}}{1 - \eta} G_\tau$$

and

$$(19) \quad W_2 = \frac{1}{1 - \eta} \int_0^\infty M_\infty(t)dt \equiv \frac{1}{1 - \eta} G_\infty.$$

Setting  $W_1(\tau)$  equal to  $W_2$ , WTP is given by

$$(20) \quad w^*(\tau) = 1 - \left( \frac{G_\infty}{G_\tau} \right)^{1/(1-\eta)}.$$

The solution for  $w^*(\tau)$  depends on the distributions for  $\Delta T$  and  $\gamma$ , the horizon  $H = 100$  years, and the parameters  $\eta$ ,  $g_0$ , and  $\delta$  (values for which are discussed in the following). We will examine how  $w^*$  varies with  $\tau$ ; the cost of abatement should be a decreasing function of  $\tau$ , so given estimates of that cost, one could use these results to determine abatement targets.

#### 2.4.2 WTP: Growth Rate Impact

If  $\Delta T_H$  instead affects the growth rate of consumption as in equation (5), and if  $\Delta T_H$  and  $\gamma$  were known, social welfare would be

7. I calculate WTP using a finite horizon of 500 years. After some 200 years, the world will likely exhaust the economically recoverable stocks of fossil fuels so that GHG concentrations will fall. In addition, so many other economic and social changes are likely that the relevance of applying CRRA expected utility over more than a few hundred years is questionable.

$$(21) \quad W = \int_0^{\infty} U(C_t) e^{-\delta t} dt = \frac{1}{1 - \eta} \int_0^{\infty} e^{\omega_0 - \omega_1 t - \omega_0 (1/2)^{t/H}} dt.$$

where

$$(22) \quad \omega_0 = 2(\eta - 1) \frac{\gamma H \Delta T_H}{\ln(1/2)},$$

$$(23) \quad \omega_1 = (\eta - 1)(g_0 - 2\gamma \Delta T_H) + \delta.$$

If society sacrifices a fraction  $w(\tau)$  of present and future consumption to keep  $\Delta T_H \leq \tau$  and there is uncertainty over  $\Delta T_H$  and  $\gamma$ , social welfare at  $t = 0$  is

$$(24) \quad W_1(\tau) = \frac{[1 - w(\tau)]^{1-\eta}}{1 - \eta} E_{0,\tau} \int_0^{\infty} e^{\tilde{\omega}_0 - \tilde{\omega}_1 t - \tilde{\omega}_0 (1/2)^{t/H}} dt.$$

If no action is taken to limit warming, social welfare would be

$$(25) \quad W_2 = \frac{1}{1 - \eta} E_0 \int_0^{\infty} e^{\tilde{\omega}_0 - \tilde{\omega}_1 t - \tilde{\omega}_0 (1/2)^{t/H}} dt.$$

Once again, WTP is the value  $w^*(\tau)$  that equates  $W_1(\tau)$  and  $W_2$ . Defining  $M_\tau(t)$  and  $M_\infty(t)$  as before, but with  $g(\gamma)$  instead of  $g(\beta)$ , equations (18), (19), and (20) again apply.

## 2.5 Results

Willingness to pay is essentially a measure of the demand side of policy—the maximum amount society would be willing to sacrifice to obtain the benefits of limited warming. The case for an actual GHG abatement policy will depend on the cost of that policy as well as the benefits. The framework I use does not involve estimates of abatement costs—I only estimate WTP as a function of  $\tau$ , the abatement-induced limit on any increase in temperature at the horizon  $H$ . Clearly the amount and cost of abatement needed will decrease as  $\tau$  is made larger, so I consider a stringent abatement policy to be one for which  $\tau$  is “low,” which I take to be at or below the expected value of  $\Delta T$  under a BAU scenario, that is, about 3°C, and  $w^*(\tau)$  is “high,” that is, at least 3 percent. At issue in this chapter is the extent to which estimates of WTP depend on whether  $\Delta T$  is assumed to affect the level of consumption directly versus the growth rate of consumption.

In addition to the distributions for  $\Delta T$  and the impact parameters  $\beta$  or  $\gamma$ , WTP depends on the values for the index of relative risk aversion  $\eta$ , the rate of time discount  $\delta$ , and the base level real growth rate  $g_0$ . To explore the case for a stringent abatement policy, I make conservative assumptions about  $\eta$ ,  $\delta$ , and  $g_0$  in the sense of choosing numbers that would lead to a higher WTP.

The finance and macroeconomics literature has estimates of  $\eta$  ranging from 1.5 to 6 and estimates of  $\delta$  ranging from .01 to .04. The historical real growth rate  $g$  ranges from .02 to .025. It has been argued, however, that for intergenerational comparisons  $\delta$  should be close to zero on the grounds that society not should value the well-being of our great-grandchildren less than our own. Likewise, while values of  $\eta$  well above 2 may be consistent with the (relatively short horizon) behavior of investors, we might use lower values for intergenerational welfare comparisons. Because I want to determine whether current assessments of uncertainty over temperature change and its impact generate a high enough WTP to justify stringent abatement, I will stack the deck in favor of our great-grandchildren and use relatively low values of  $\eta$  and  $\delta$ : around 2 for  $\eta$  and 0 for  $\delta$ . Also, WTP is a decreasing function of the base growth rate  $g_0$ , so I will set  $g_0 = .02$ , the low end of the historical range.

### 2.5.1 No Uncertainty

It is useful to begin by considering a deterministic world in which the trajectory for  $\Delta T$  and the impact of that trajectory are known with certainty. Then (18) and (19) for the direct impact case would simplify to

$$(26) \quad W_1 = \frac{[1 - w(\tau)]^{1-\eta}}{1 - \eta} \int_0^\infty e^{\rho_0 - \rho_1 t - 2\rho_0(1/2)^{t/H} + \rho_0(1/2)^{2t/H}} dt,$$

$$(27) \quad W_2 = \frac{1}{1 - \eta} \int_0^\infty e^{\rho_0 - \rho_1 t - 2\rho_0(1/2)^{t/H} + \rho_0(1/2)^{2t/H}} dt,$$

where now  $\bar{\beta}$ , the mean of  $\beta$ , replaces  $\beta$  in equation (12) for  $\rho_0$ . (I will use the means of  $\beta$  and  $\gamma$  as their certainty-equivalent values.) Likewise, equations (24) and (25) for the case of a growth rate impact would simplify to

$$(28) \quad W_1(\tau) = \frac{[1 - w(\tau)]^{1-\eta}}{1 - \eta} \int_0^\infty e^{\omega_0 - \omega_1 t - \omega_0(1/2)^{t/H}} dt,$$

$$(29) \quad W_2 = \frac{1}{1 - \eta} \int_0^\infty e^{\omega_0 - \omega_1 t - \omega_0(1/2)^{t/H}} dt,$$

where now the mean  $\bar{\gamma}$  replaces  $\gamma$  in equations (22) and (23) for  $\omega_0$  and  $\omega_1$ .

For both impact models, I calculate the WTP to keep  $\Delta T$  zero for all time, that is,  $w^*(0)$ , over a range of values for  $\Delta T$  at the horizon  $H = 100$ . For this exercise, I set  $\eta = 2$ ,  $\delta = 0$ , and  $g_0 = .020$ . The results are shown in figure 2.5, where  $w_c^*(0)$  applies to the case where  $\Delta T$  affects  $C$  directly, and  $w_g^*(0)$  applies to the case where  $\Delta T$  affects the growth rate of  $C$ .

The graph says that if, for example,  $\Delta T_H = 6^\circ\text{C}$ ,  $w_c^*(0)$  is about .03, and  $w_g^*(0)$  is about .022. Thus, if  $\Delta T$  affects consumption directly, society should be willing to give about 3 percent of current and future consumption to keep  $\Delta T$  at zero instead of  $6^\circ\text{C}$ . But if  $\Delta T$  affects the growth rate of con-



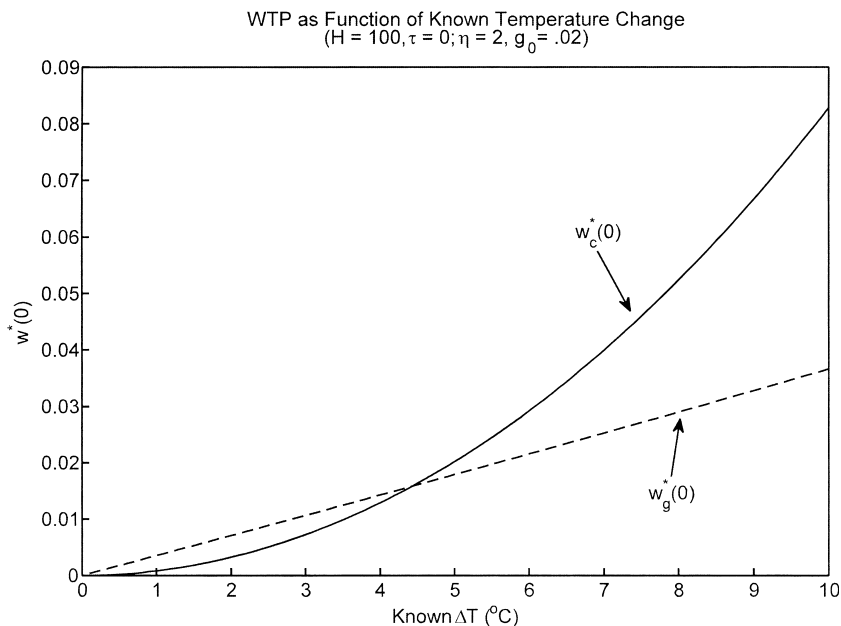


Fig. 2.5 WTP, known temperature change:  $\eta = 2$ ,  $g_0 = .020$ , and  $\delta = 0$

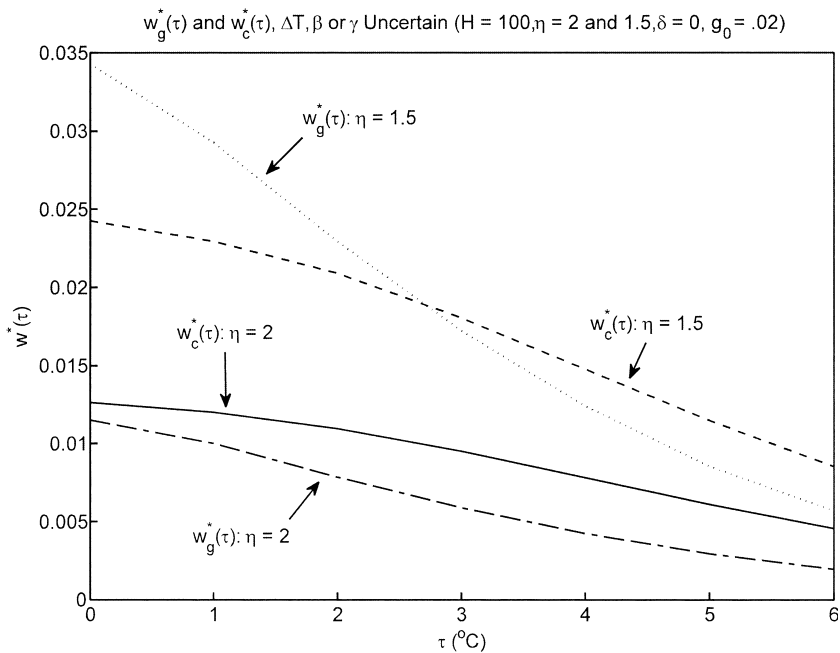
sumption, the willingness to pay is only about 2.2 percent. (Remember that the “known  $\Delta T$ ” applies to time  $t = H$ .  $\Delta T_t$  follows the trajectory given by equation [3].)

Note that both  $w_c^*(0)$  and  $w_g^*(0)$  become much larger as the *known*  $\Delta T_H$  becomes larger than  $8^\circ\text{C}$ ; such temperature outcomes, however, have low probability. In addition, these curves have different shapes:  $w_c^*(0)$  is a convex function of  $\Delta T_H$ , while  $w_g^*(0)$  is a (nearly) linear function of  $\Delta T_H$ .<sup>8</sup> This means that for small changes in temperature, a growth rate impact model will yield a slightly higher WTP, but for very large changes in temperature, the direct impact model yields much larger WTPs. Whether this difference matters for estimates of WTP under uncertainty depends on the probability distributions for  $\Delta T_H$  and  $\beta$  and  $\gamma$ . With sufficient probability mass in the right-hand tails of the distributions, the two impact models should yield different numbers for WTP. We explore this in the following.

8. To see that  $w_c^*(0)$  is a convex function of  $\Delta T_H$ , note that if  $\tau = 0$ , equations (26) and (27) imply that

$$w_c^*(0) = 1 - \left[ \rho \int_0^\infty e^{-\rho t - 4(1-\eta)\beta \Delta T_H \psi(t)} dt \right]^{1/(1-\eta)}$$

where  $\psi(t) = [1 - (1/2)^{t/H}]^2$ . Just differentiate to see that  $dw_c^*/d\Delta T_H > 0$  for all values of  $\Delta T_H$  and  $\beta$ , and  $d^2w_c^*/d\Delta T_H^2 > 0$  for sufficiently small values of  $\Delta T_H$  and  $\beta$  (in our case, as long as  $\Delta T_H < 15.8^\circ\text{C}$ ). Similarly, we can show that  $dw_g^*/d\Delta T_H > 0$  and  $d^2w_g^*/d\Delta T_H^2$  is a small negative number (in our case  $-.000063$ ), a curvature small enough so that in figure 2.5,  $w_g^*(0)$  appears linear.



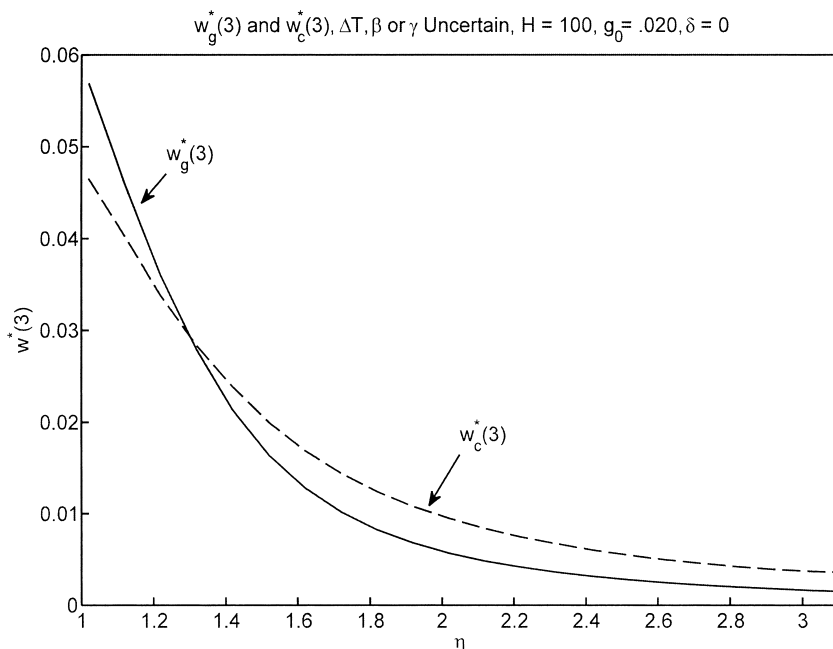
**Fig. 2.6** WTP, both  $\Delta T$  and  $\gamma$  uncertain:  $\eta = 2$  and  $1.5$ ,  $g_0 = .020$ , and  $\delta = 0$

2.5.2 Uncertainty over Temperature and Economic Impact

I now allow for uncertainty over both  $\Delta T$  and the relevant impact parameter (either  $\beta$  or  $\gamma$ ), using the calibrated distributions for each. Willingness to pay is given by equations (16) to (20) for the direct impact model and equations (24) and (25) for the growth rate impact. The calculated values of WTP as are shown as functions of  $\tau$  in figure 2.6 for  $\delta = 0$ ,  $g_0 = .020$ , and  $\eta = 2$  and  $1.5$ . Note that if  $\eta = 2$ , WTP is always less than 1.5 percent, even for  $\tau = 0$ . To obtain a WTP above 2 percent requires a lower value of  $\eta$ . As figure 2.6 shows, if  $\eta = 1.5$ ,  $w^*(\tau)$  reaches about 3 percent for  $\tau$  around 0 or 1°C, but only when the impact of warming occurs through the growth rate of consumption. When the impact is direct,  $w^*$  is always below 2.5 percent.

Because relatively large values of WTP can only be obtained for small values of  $\eta$ , the top two lines in figure 2.6 have the greatest policy relevance. But note that when  $\eta = 1.5$ , the difference between  $w_g^*(\tau)$  and  $w_c^*(\tau)$  is only significant for  $\tau$  below 2°C. It seems unlikely that a politically and economically feasible policy would be adopted that would prevent any warming, or limit it to 1 or even 2°C. If we believe that a “feasible” policy is one that limits  $\Delta T$  to its expected value of around 3°C, then as figure 2.6 shows, the direct and growth rate impact models give similar values for WTP.

On the other hand, what if we take the view that the “correct” value of  $\eta$  is less than 1.5? Figure 2.7 shows the dependence of WTP on the index of risk

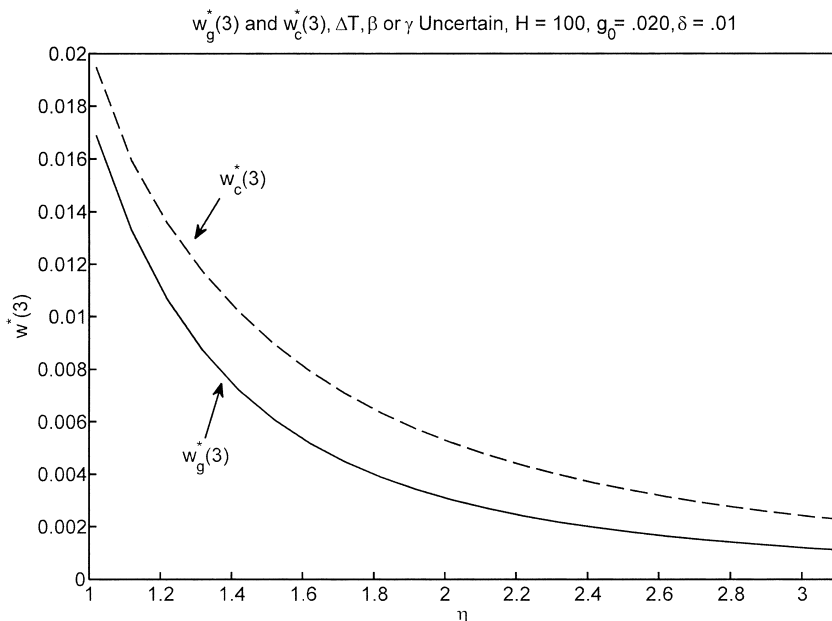


**Fig. 2.7** WTP versus  $\eta$  for  $\tau = 3$ :  $g_0 = .020$  and  $\delta = 0$

aversion,  $\eta$ . It plots  $w^*(3)$ , that is, the WTP to ensure  $\Delta T_H \leq 3^\circ\text{C}$  at  $H = 100$  years, for  $g_0 = .02$ , as a function of  $\eta$ . Although  $w^*(3)$  is below 2 percent for values of  $\eta$  above 1.5, it approaches 5 percent as  $\eta$  is reduced to 1 (the value used in Stern 2007). The reason is that while future utility is not discounted (because  $\delta = 0$ ), future consumption is implicitly discounted at the initial rate  $\eta g_0$ . If  $\eta$  is made smaller, potential losses of future consumption have a larger impact on WTP. Also, as discussed further in the following,  $w_c^*(3) > (<)w_g^*(3)$  when  $\eta > (<)1.3$ .

These estimates of WTP are based on zero discounting of future utility. While there may be an ethical argument for zero discounting,  $\delta = 0$  is outside the range of estimates of the rate of time preference obtained from consumer and investor behavior. However, estimates of WTP above 3 percent depend critically on this assumption of  $\delta = 0$ . Figure 2.8 again plots  $w_c^*(3)$  and  $w_g^*(3)$ , but this time with  $\delta = .01$ . Note that for either impact model, discounting future utility, even at a very low rate, will considerably reduce WTP. With  $\delta = .01$ ,  $w^*(3)$  is again below 2 percent for all values of  $\eta$ , and for either impact model.

The results so far indicate that for either impact model, large values of WTP require fairly extreme combinations of parameter values. However, these results are based on distributions for  $\Delta T_H$ ,  $\beta$ , and  $\gamma$  that were calibrated to studies in the IPCC's 2007 (2007a,c) report and concurrent economic

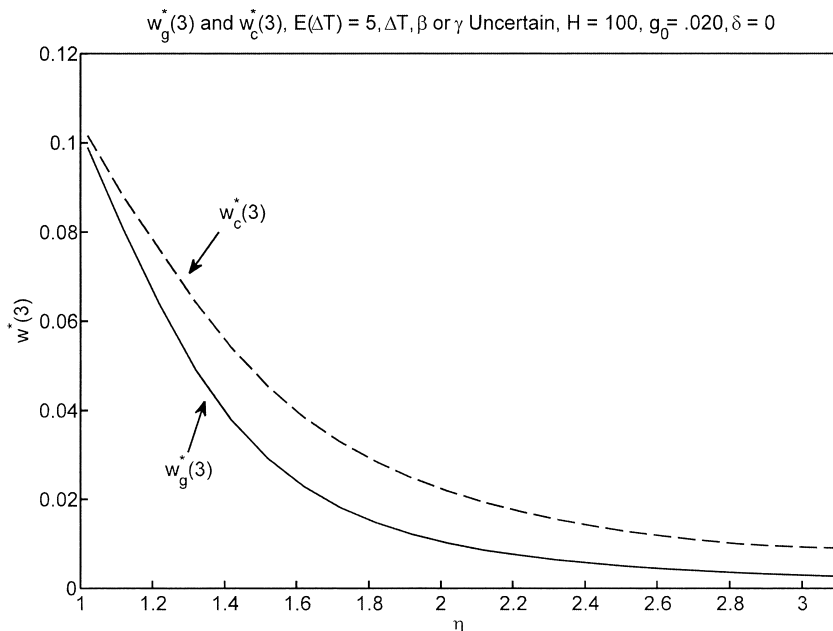


**Fig. 2.8** WTP versus  $\eta$  for  $\tau = 3: g_0 = .020$  and  $\delta = .01$

studies, and those studies were done several years prior to 2007. More recent studies suggest that “most likely” values for  $\Delta T$  in 2100 might be higher than the 1.0°C to 4.5°C range given by the IPCC. For example, a recent report by Sokolov et al. (2009) suggests an expected value for  $\Delta T$  in 2100 of around 4 to 5°C, as opposed to the 3.0°C expected value that I used. Thus, I recalculate WTP for both impact models, for both  $\delta = 0$  and .01, but this time shifting the distribution for  $\Delta T_H$  to the right so that it has a mean of 5°C, corresponding to the upper end of the 4 to 5°C range in Sokolov et al. (2009). (The other moments of the distribution remain unchanged, and  $H$  is again 100 years).

The results are shown in figures 2.9 and 2.10. Now if  $\delta = 0$  and  $\eta$  is below 1.5,  $w^*(3)$  is above 3 percent when the impact of  $\Delta T$  occurs through the growth rate, and above 4 percent when the impact is direct, and reaches around 10 percent if  $\eta = 1$ . Even if  $\delta = .01$ ,  $w_c^*(3)$  exceeds 4 percent when  $\eta = 1$  (although  $w_g^*[3]$  only reaches 2.5 percent). Thus, there are parameter values and plausible distributions for  $\Delta T$  that yield a large WTP. Those parameter values and distributions are outside the current consensus range, but that may change as new studies of warming and its impact become available.

As figures 2.7 to 2.10 show, for either value of  $\delta$ ,  $w_c^*(3)$  is usually higher than  $w_g^*(3)$ , and when  $\delta = .01$  it is considerably higher. In the Ramsey growth context, the consumption discount rate is  $\delta + \eta g_r$ , so even if  $\delta = 0$ , future



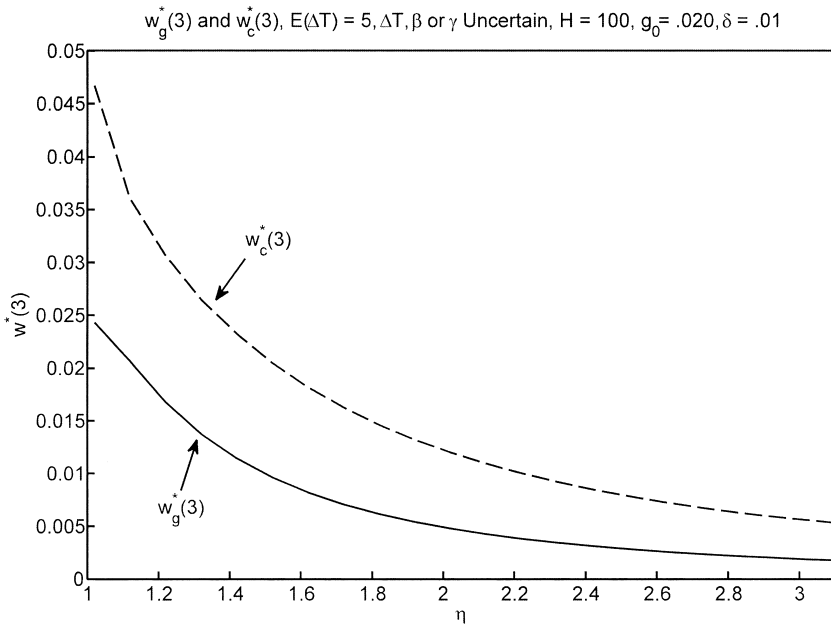
**Fig. 2.9** WTP versus  $\eta$  for  $\tau = 3$ :  $E(\Delta T_H) = 5^\circ\text{C}$ ,  $g_0 = .020$ ,  $\delta = 0$

consumption (although not utility) is discounted (less so for small values of  $\eta$ ). When  $\Delta T$  affects consumption directly, the loss of consumption is greater at shorter horizons (but smaller at long horizons), making  $w_c^*(3) > w_g^*(3)$ . (In figure 2.7,  $w_c^*[3] < w_g^*[3]$  when  $\eta < 1.3$  because with a low consumption discount rate, the larger long-run reduction in consumption from a growth rate impact overwhelms the smaller short-run impact, even in expected value terms.)

## 2.6 Modeling and Policy Implications

The integrated assessment models that I am aware of all relate temperature change to the level of real GDP and consumption. As we have seen, this will often yield a higher WTP—and thus yield higher estimates of optimal GHG abatement—than will a model that relates temperature change to the growth rate of GDP and consumption. How important is the difference, and what do these results tell us about modeling?

In Pindyck (2009), using a model that related temperature change to the growth rate of consumption, I found that for temperature and impact distributions based on the IPCC and “conservative” parameter values (e.g.,  $\delta = 0$ ,  $\eta = 2$ , and  $g_0 = .02$ ), WTP to prevent even a small increase in temperature is around 2 percent or less, which is inconsistent with the immediate adop-



**Fig. 2.10** WTP versus  $\eta$  for  $\tau = 3$ :  $E(\Delta T_H) = 5^\circ\text{C}$ ,  $g_0 = .020$ ,  $\delta = .01$

tion of a stringent GHG abatement policy. To what extent do those results change when temperature change directly affects the level of consumption? And more broadly, what are the policy implications of the results in this chapter?

### 2.6.1 Implications for Modeling

The difference in WTPs for a direct versus a growth rate impact is largest for large temperature changes and for higher consumption discount rates. As we saw in figure 2.5 for the case of no uncertainty,  $w_c^*(0)$  is a convex function of  $\Delta T$  and thus becomes increasingly greater than  $w_g^*(0)$  as  $\Delta T$  gets larger. Likewise, when there is uncertainty but the *expected* temperature change is increased from  $3^\circ\text{C}$  to  $5^\circ\text{C}$ , the difference between  $w_c^*(3)$  and  $w_g^*(3)$  becomes larger. And note from figures 2.9 and 2.10 that the difference between  $w_c^*(3)$  and  $w_g^*(3)$  is proportionally larger when the consumption discount rate ( $\delta + \eta g_0$ ) is larger, that is, when  $\eta$  is larger or when  $\delta$  is .01 rather than 0.

If the consumption discount rate is large (i.e., if  $\eta$  is large or  $\delta > 0$ ), almost any model will yield estimates of WTP and optimal abatement levels that are small. This is simply the result of discounting over long horizons (greater than fifty years). That is why model-based analyses that call for stringent abatement policies assume  $\delta = 0$  and relatively low values for  $\eta$ . (Stern [2007, 2008], for example, uses  $\delta = 0$  and  $\eta = 1$ .) Thus, if we limit our analyses to

the low end of the consensus range for  $\eta$  (around 1.5), even with  $\delta = 0$ , the choice of impact model will matter if evolving climate science studies yield increasingly large estimates of expected temperature change.

Which impact model—direct versus growth rate—should one use for modeling? A direct impact model is simpler, easier to understand, and perhaps easier to estimate or calibrate. But as I have argued at the beginning of this chapter, there are strong theoretical and empirical arguments that favor the growth rate impact. Until new studies demonstrate otherwise, it seems to me that it is difficult to make the case for a direct impact.

### 2.6.2 Implications for Policy

The results in this chapter supplement those in Pindyck (2009) in terms of implications for policy. We can summarize those implications as follows.

First, although the direct impact model often yields higher estimates of WTP, it is still the case that using temperature and impact distributions based on the IPCC (2007a,c) and concurrent economic studies, for most parameter values our WTP estimates are still too low to support a stringent GHG abatement policy. Of course, these estimates do not suggest that no abatement is optimal. For example, a WTP of 2 percent of GDP is in the range of cost estimates for compliance with the Kyoto Protocol.<sup>9</sup>

In addition to the effects of discounting discussed in the preceding, our low estimates of WTP are due to the limited weight in the tails of the distributions for  $\Delta T$  and the impact parameter  $\beta$  or  $\gamma$ . The probability of a realization in which  $\Delta T \geq 4.5^\circ\text{C}$  in 100 years *and* the impact parameter is 1 standard deviation above its mean is less than 5 percent. An even more extreme outcome in which  $\Delta T = 7^\circ\text{C}$  (and the impact parameter is 1 standard deviation above its mean) would imply about a 9 percent loss of GDP in 100 years for a growth rate impact, but the probability of an outcome this bad or worse is less than 1 percent. And this low-probability loss of GDP in 100 years would involve much smaller losses in earlier years.

Second, although these estimates of WTP are consistent with the current consensus regarding future warming and its impact as summarized in IPCC (2007a,b,c) that consensus may be wrong, especially with respect to the tails of the distributions. Indeed, based on recent studies, that consensus may already be shifting toward more dire estimates of warming and its impact. As we saw from figures 2.9 and 2.10, shifting the temperature distribution to the right so that  $E(\Delta T_H)$  is  $5^\circ\text{C}$  instead of  $3^\circ\text{C}$  results in substantially higher estimates of WTP. Thus, if the consensus (or “state of knowledge”) shifts toward a higher expected value for the amount of warming, or more mass in the tails of the distribution, WTP might increase enough to justify more aggressive abatement policies.

9. See the survey of cost studies by the Energy Information Administration (1998) and the more recent country cost studies surveyed in IPCC (2007b).

## 2.7 Conclusions

If we are to use economic models to evaluate GHG abatement policies, how should we treat the impact of possible future increases in temperature? One could argue that we simply do not (and cannot) know much about that impact because we have had no experience with substantial amounts of warming, and there are no models or data that can tell us much about the impact of warming on production, migration, disease prevalence, and a variety of other relevant factors. Instead, I have taken existing IAMs and related models of economic impact at face value and treated them analogously to the climate science models that are used to predict temperature change or its probability distribution. In this way, I obtained a (displaced gamma) distribution for an impact parameter that relates temperature change to consumption or to the growth rate of consumption.

We have seen that in most cases, a direct impact yields a higher WTP than a growth rate impact. The reason is that when  $\Delta T$  affects consumption directly, the loss of consumption is greater at short horizons (but smaller at long horizons). Consumption discounting can give these short-horizon effects more weight. Even if future utility is not discounted ( $\delta = 0$ ), the consumption discount rate ( $\delta + \eta g_0$ ) is still positive and can be large if  $\eta$  is large.

Overall, I would argue that the choice of a direct versus growth rate impact should be based on the underlying economics, and the growth rate specification has both theoretical and empirical support. But even with a direct impact model, using temperature and impact distributions based on the IPCC (2007a,b,c) and concurrent economic studies, for most parameter values our WTP estimates are still too low to support a stringent GHG abatement policy. Of course, there are parameter values and plausible distributions for  $\Delta T$  that yield a large WTP—and those that can yield a much smaller WTP. In particular, if the rate of time preference,  $\delta$ , is 1 or 2 percent, WTP will generally be very low. On the other hand, if  $\delta = 0$ , a shift in the temperature change distribution such that  $E(\Delta T_H)$  is 5°C or a shift in the accepted value of  $\eta$  to put it close to 1 can lead to a WTP of 6 or 8 percent. Such distributions and parameter values are outside the current consensus range, but that range may change as new studies of warming and its impact are completed and disseminated.

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